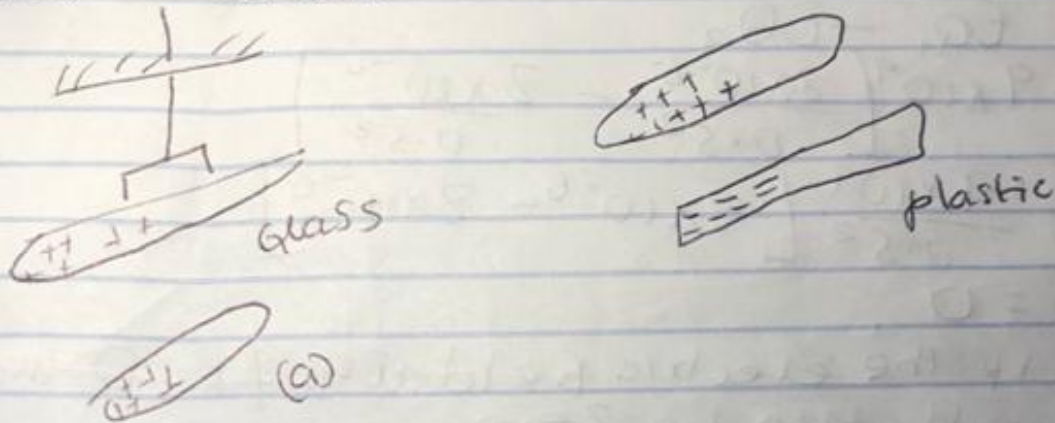


## 1) Question 1

a) Negative charge can be produced when we rub a glass rod with a silk cloth. Here a small amount of negative charge moves from the rod to the silk leaving the rod with a small amount of excess positive charge for better understand



## b) Given

$$q_1 + q_2 = 5.0 \times 10^{-5} \text{ C} \quad \text{--- (1)}$$

$$\text{Electric force } F = 1.0 \text{ N}$$

$$\text{Distance apart } = 2.0$$

$$F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$q_1 q_2 = \frac{F d^2}{9 \times 10^9} = \frac{10 \times 2^2}{9 \times 10^9} = 4.44 \times 10^{-10} \text{ C}$$

$$q_1 = \frac{4.44 \times 10^{-10}}{q_2} \quad \text{--- (2)}$$

$$\frac{4.44 \times 10^{-10}}{q_2} + q_2 = 5.0 \times 10^{-5}$$

$$4.44 \times 10^{-10} + q_2^2 = 5.0 \times 10^{-5} q_2$$

$$q_2^2 - 5.0 \times 10^{-5} q_2 + 4.44 \times 10^{-10} = 0$$

$$q_2 = 3.845 \times 10^{-5} \text{ C or } 1.1545 \times 10^{-5} \text{ C}$$

Eq (1)

$$q_1 + q_2 = 5.0 \times 10^{-5}$$

$$q_1 = 5.0 \times 10^{-5} - 3.845 \times 10^{-5}$$



$$Q = 8.45 \times 10^{-6} \text{ C}$$

c  $d = 0.5 \text{ m}$   
 $Q_1 = Q_2 = 8 \text{ nC}$

$$\begin{aligned} \therefore \vec{E} &= E_{Q_1} - E_{Q_2} \\ &= 9 \times 10^9 \left[ \frac{8 \times 10^{-6}}{0.5^2} - \frac{8 \times 10^{-6}}{0.5^2} \right] \\ &= \frac{9 \times 10^9}{0.5^2} [8 \times 10^{-6} - 8 \times 10^{-6}] \end{aligned}$$

$$E = 0$$

Now if the electric field at a point  $P = 0$  then force will also be zero

Hence  $f = 0$

$$E = 0 \text{ at point } Q$$

### Question 2

a Electric field is defined as a field of force surrounding a charged body. The force

Electric field intensity is defined as the force per unit positive charge of that point

$$E = \frac{F}{q}, \text{ where } F = \text{electric force} - \text{N}$$

$q = \text{charge} - \text{C}$

b Given that

$$Q_1 = 8 \text{ nC}$$

$$Q_2 = 12 \text{ nC}$$

$$r_1 = 4 \text{ m}$$

$$r_2 = 3 \text{ m}$$

$P = ?$



Equation 3 becomes

$$B = \frac{\mu_0 I x}{4\pi} \left[ \frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_0^a$$

$$B = \frac{\mu_0 I x}{4\pi} \left( \frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right)$$

when  $2a$  of the conductor is very great in comparison to its distance  $x$  from point  $P$ , we consider it long

$$\therefore (x^2 + a^2)^{1/2} = a \rightarrow \infty$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

Thus, at all points in a circle of radius  $r$

$$B = \frac{\mu_0 I}{2\pi r}$$

magnitude of magnetic field or flux density  $B$  near a long, straight current carrying conductor

### Question 4

1) Magnetic flux is defined as the strength of magnetic field represent by lines of forces. It is usually represented by the symbols  $\phi$

$$\begin{aligned} B &= \frac{V}{r} \cdot \frac{q}{m} \\ &= \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-11}}{9.1 \times 10^{-31}} \\ &= \frac{5.6 \times 10^{-20}}{9.1 \times 10^{-31}} \\ &= 6.15 \times 10^{10} \text{ rad } s^{-1} \text{ or rad } s^{-1} \end{aligned}$$

c) Cyclotron frequency which is equal or the same thing as angular speed. It is called cyclotron frequency because it is a frequency of an accelerator called cyclotron.

$$E_1 = \frac{Q}{4\pi\epsilon_0 r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{4^2} = 4.5 \times 10^3 \text{ N/C}$$

$$E_2 = \frac{Q}{4\pi\epsilon_0 r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-6}}{3^2} = 12 \times 10^3 \text{ N/C}$$

$$E_p - E_1 + E_2 = 4.5 \times 10^3 + 12 \times 10^3 \Rightarrow 16.5 \times 10^3 \text{ N/C}$$

$$\text{Net charge} = 12 + 8 = 20 \text{ nC}$$

$$F = qE = 20 \times 10^{-6} \times 16.5 \times 10^3 = 0.33 \text{ N}$$

$$Q = \frac{20 \times 10^{-6} \times 9 \times 10^9}{3^2} = 20 \times 10^3 \text{ N/C}$$

To get the electric charge recall that

$$E = \frac{Q}{4\pi\epsilon_0 r^2} = 9 \times 10^9 \times \frac{Q}{r^2}$$

$$Q_p = \frac{E \times r^2}{9 \times 10^9} = \frac{16.5 \times 10^3 \times 9^2}{9 \times 10^9} = 8.98 \text{ nC}$$

$$E_p = \frac{9 \times 10^9 \times 8.98 \times 10^{-6}}{3^2}$$

$$E_p = 89.8 \text{ N/C}$$

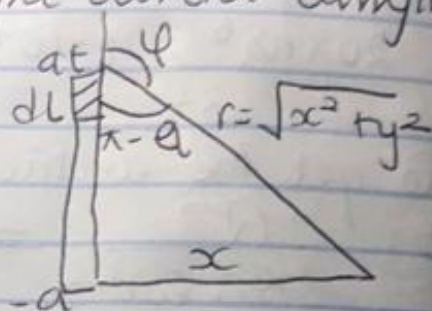


### 5 Question 5

Biot-Savart law is an equation that describes the magnetic field created by a current-carrying wire, and allow you to calculate its strength at various points.

b Magnetic field of a straight current carrying conductor

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \theta}{r^2}$$



$$\sin(\pi - \theta) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl (\pi - \theta)}{r^2}$$

from diagram

$$r^2 = x^2 + y^2$$

$$= dl \frac{(\pi - \theta)}{x^2 + y^2} \quad \text{--- (1)}$$

$$\text{But } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- (11)}$$

putting (11) into (1)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cdot x}{(x^2 + y^2) (x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cdot x}{(x^2 + y^2)^{3/2}}$$

recall  $dl = dy$

$$B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- (3)}$$