

NAME : OSARO DAVID

DEP : ELECT-ELECT. ENGINEERING

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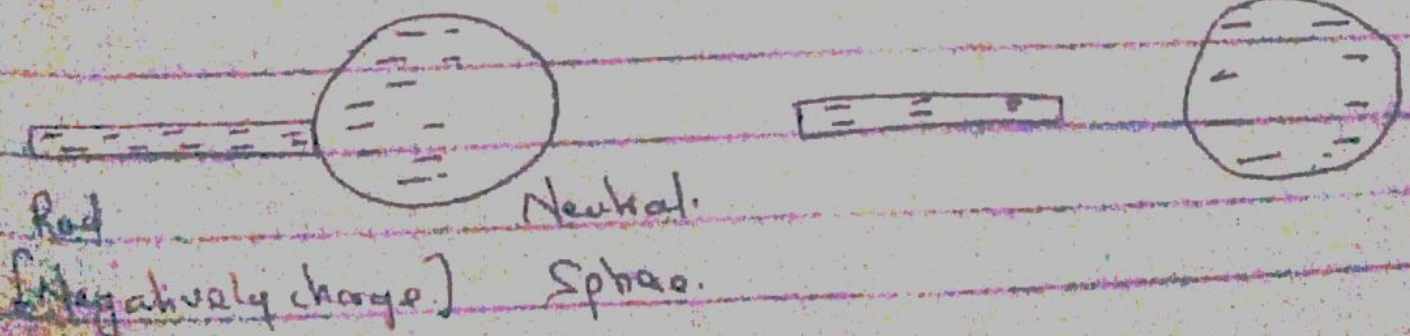
COVID 19 HOLIDAY ASSIGNMENT

1(a)

Consider a neutral conducting sphere that is insulated so there is no conducting path for the charges to leave, then introducing a negatively charged rod brought in contact to the sphere. This makes some electrons to move from the electrons to the sphere, and when the rod is removed the sphere remains negatively charged.

(i).

(ii).



[In contact]

[After contact]

$$1(b) \quad q_1 + q_2 = 5 \times 10^{-5} \text{ C}$$

$$1. \quad F = \frac{k q_1 q_2}{r^2} = k \cdot q_1 \cdot \frac{(5 \times 10^{-5} \text{ C} - q_1)}{r^2}$$

$$F \cdot r^2 = k (5 \times 10^{-5} q_1 - q_1^2)$$

$$\Rightarrow 1 \cdot 2^2 = 9 \times 10^9 (5 \times 10^{-5} q_1 - q_1^2)$$

$$\Rightarrow 4 = 9 \times 10^9 q_1^2 - 4.5 \times 10^5 q_1 + 4 = 0$$

$$q_1 = 3.8 \times 10^{-5} \text{ C} \text{ or } 1.1 \times 10^{-5} \text{ C}$$

$$\therefore q_2 = (5 \times 10^{-5} - q_1)$$

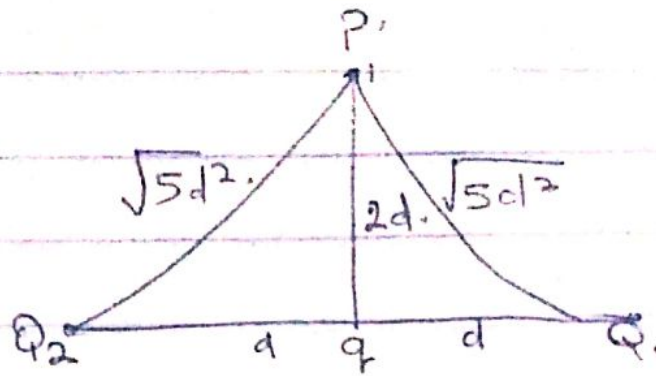
$$= 1.1 \times 10^{-5} \text{ C} \text{ or } 3.89 \times 10^{-5} \text{ C}$$

$$\therefore \text{Answer } q_1 = 3.87 \times 10^{-5} \text{ C} \quad q_2 = 1.1 \times 10^{-5} \text{ C}$$

$$q_1 = 1.1 \times 10^{-5} \text{ C}$$

$$q_2 = 3.87 \times 10^{-5} \text{ C}$$

1(c)



$$\vec{F} = \vec{F}_{12} + \vec{F}_{13} + \vec{F}_{14}$$

Using $x^2 = y^2 + z^2$.

$$PQ = \sqrt{(2d)^2 + d^2} = \sqrt{5d^2}$$

$$0 = \frac{K \cdot Q_2}{(\sqrt{5d^2})^2} + \frac{K \cdot q}{(2d)^2} + \frac{K \cdot Q_1}{(\sqrt{5d^2})^2}$$

$$0 = \frac{Q_2}{5d^2} + \frac{q}{4d^2} + \frac{Q_1}{5d^2}$$

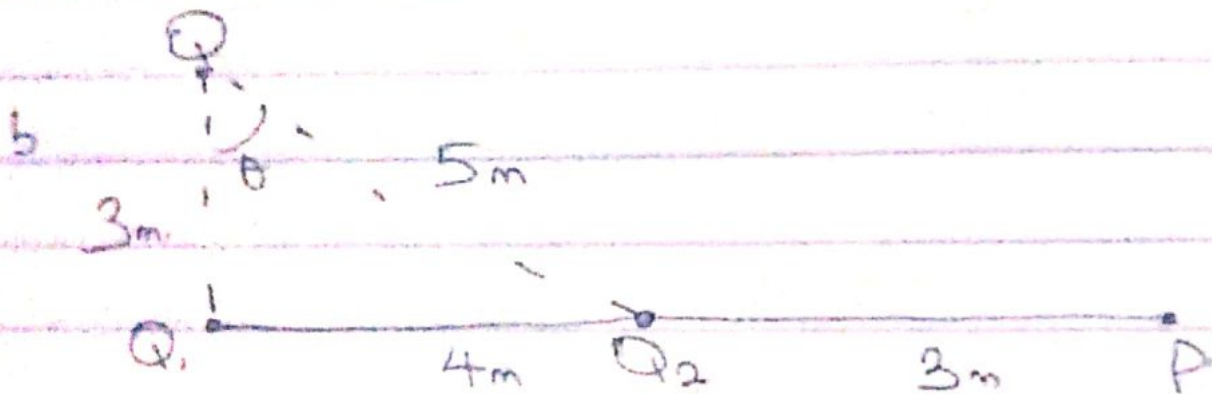
$$\frac{q}{4d^2} = -\frac{1}{5d^2} (Q_2 + Q_1)$$

$$q = -\frac{4d^2}{5d^2} (Q_2 + Q_1)$$

$$= -\frac{4}{5} (1.6 \times 10^{-5})$$

$$= -1.2 \times 10^{-5} \text{ or } -12 \mu\text{C} \quad -11 \mu\text{C}$$

2(a) Electric Field is a region of space where an electric charge can experience an electric force, while Electric Field Intensity is the electric force per unit charge. Mathematically $E = \frac{F(q)}{q_0(c)}$



$$E_{P_1} = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{7} = 1.46 \text{ N/C}$$

$$E_{P_2} = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{9} = 12 \text{ N/C}$$

$$E_{Q_1} = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{9} = 8 \text{ N/C}$$

$$E_{Q_2} = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{25} = 4.32 \text{ N/C}$$

Vector	Angle	x_{com}	y_{com}
E_{p1}	0°	$12 \cos(0)$ $0.9 \cos(0)$	$0.9 \sin(0)$
E_{p2}	0°	$12 \cos(0)$	$0 \sin(0)$
		12	0
		1.46	
		13.46	

$$\therefore \overline{E_p} = \sqrt{(13.46)^2 + 0}$$

$$= \underline{13.46 \text{ N/C}}$$

Vector	Angle	x_{com}	y_{com}
E_{q1}	90°	$8 \cos(90^\circ)$ $= 0$	$8 \sin(90^\circ)$ $= 8$
E_{q2}	45° 53.1°	$4.32 \cos(53.1)$ $= 2.59$	$4.32 \sin(53.1)$ $= 3.45$

$$\Rightarrow 2.59$$

$$11.45$$

$$\therefore \overline{E_q} = \sqrt{(2.59)^2 + (11.45)^2}$$

$$= 11.7 \text{ N/C}$$

3(a).

(i) Volume charge density.

$$\rho = \frac{dQ}{dV} \rightarrow dQ = \rho dV.$$

(ii) Surface charge density.

$$\sigma = \frac{dQ}{dA} \rightarrow dQ = \sigma dA$$

(iii) Linear charge density.

$$\lambda = \frac{dQ}{dL} \rightarrow dQ = \lambda dL.$$

(b) Electric potential difference. is the work done per unit charge against electric forces when a charge is transported from one point to another. Mathematically,

$$V_B - V_A = \frac{W(A \rightarrow B)}{q_0}$$

$$\text{i.e. } dW = F \cdot dL. \quad \text{--- (i)}$$

$$F = -q_0 \cdot E. \quad \text{--- (ii)}$$

$$dW = -q_0 \cdot E \cdot dL.$$

$$W(A \rightarrow B) = -q_0 \int_A^B E \cdot dL \\ = -q_0 \int_A^B \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2} \cdot dr = \frac{1}{4\pi\epsilon_0} \frac{q_0 Q}{r_A} - \frac{1}{4\pi\epsilon_0} \frac{q_0 Q}{r_B}$$

Ans. B(c).

$$V = k \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

when $V = 0$.

$$0 = k \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$k \rightarrow 0$.

$$= \frac{Q_1}{r_1} + \frac{Q_2}{r_2}$$

$$-\frac{Q_1}{r_1} = \frac{Q_2}{r_2}$$

$$Q_2 r_1 = -Q_1 r_2$$

$$r_1 = -\frac{Q_1 r_2}{Q_2}$$

$$r_1 = \frac{-10 \times 10^6 \times 4}{-2 \times 10^6}$$

$$= 20 \text{ m}$$

$$\therefore V = k \left[\frac{10 \times 10^6}{20} + \frac{-2 \times 10^6}{4} \right] = 0$$

\therefore radius is 20m, 4m.

4 (c) A magnetic flux is the strength of magnetic field - centered by lines of force. It is represented by the symbol Φ .

$$(b). \quad W = \frac{qB}{m}$$

$$\text{where } q = 1.6 \times 10^{-19}.$$

$$\therefore W = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.1 \times 10^{-31}}$$

$$= 6.15 \times 10^{10} \text{ rad/s.}$$

5(a). Biot-Savart Law is based on the following observations for the magnetic field $d\vec{B}$ at a point P associated with a length element dl of a wire carrying a steady current I .

(b) Applying the b.o.b Savart law:

$$B = \frac{\mu_0 I}{4\pi} \int_{-y}^y \frac{dl \sin\phi}{r^2} \quad \sin(\pi - \phi) = \sin\phi$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-y}^y \frac{dl \sin(\pi - \phi)}{r^2}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{r^2} \quad \text{--- (i)}$$

$$\text{Since } \sin(\pi - \phi) = \sin\phi = \frac{y}{r} \quad \text{--- (ii)}$$

Substituting eqn (ii) in eqn (i):

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl}{r^2} \cdot \frac{y}{r} = \frac{\mu_0 I y}{4\pi} \int_{-a}^a \frac{dl}{r^3}$$

$$= \frac{\mu_0 I y}{4\pi} \int_{-a}^a \frac{dl}{(a^2 + y^2)^{3/2}}$$

$$B = \frac{4}{4x} \left[\frac{4}{x^2(x^2+9)^{1/2}} \right] \cdot 9$$

$$= \frac{16}{4x} \left(\frac{2 \cdot 9}{x^2(x^2+9)^{1/2}} \right)$$

$$= \frac{16 \cdot 9}{4x} \left(\frac{2 \cdot 9}{(x^2+9)^{1/2}} \right)$$

$$= \frac{16 \cdot 9 \cdot 2 \cdot 9}{4x} = \frac{29 \cdot 9}{x}$$

$$B = \frac{16 \cdot 9 \cdot 2 \cdot 9}{4x}$$

$$B = \frac{16 \cdot 9 \cdot 2 \cdot 9}{4x} = \frac{29 \cdot 9}{x}$$