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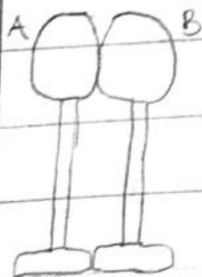
COLLEGE: MEDICINE AND HEALTH SCIENCES

DEPARTMENT: MEDICINE AND SURGERY

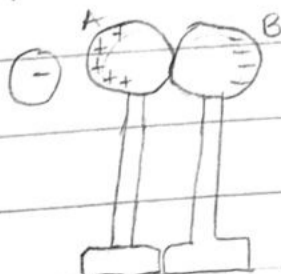
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COURSE: PHY 102

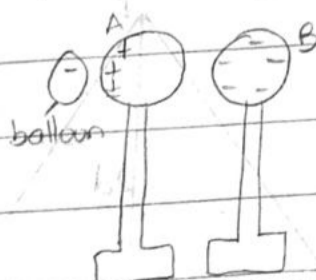
1a. The metal spheres are supported by insulating stands so that any charge acquired by the spheres cannot travel to the ground. The spheres are placed side by side so as to form a two-sphere system. Being made of metal, electrons are free to move between the spheres. If a rubber balloon is charged negatively and brought near the spheres, electrons within the two-sphere system will be induced to move away from the balloon due to the principle that like charges repel. The electrons are repelled by the negatively charged balloon. Subsequently, a mass migration occurs from sphere A to B. This electron migration causes the two-sphere system to be polarized. The two-sphere system is electrically neutral. The movement of electrons out of sphere A and into sphere B separates the negative charge from the positive charge. Therefore, sphere A is positively charged and sphere B is negatively charged. Sphere B is separated from sphere A using the insulating stand. Being pulled further from the balloon, the negative charge likely redistributes itself uniformly about sphere B. Meanwhile, the excess positive charge on sphere A remains located near the negatively charged balloon, consistent with the principle that opposite charges attract. As the balloon is pulled away, there is a uniform redistribution of charge about the surface of both spheres. The distribution occurs as the remaining electrons in sphere A move across the surface of the sphere until the excess positive charge is uniformly distributed.



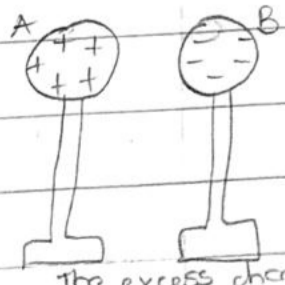
Two metal spheres are mounted on insulating stands



Presence of a -charge induces  $e^-$  to move from A to B. The two spheres are



Sphere B is separated from A using insulating stands. The two spheres have opposite charges



The excess charges distributes itself uniformly over the surfaces of the spheres

b.  $r = 2.0\text{m}; F = 1.0\text{N}; q_1 + q_2 = 5.0 \times 10^{-5}\text{C}$

$$F = \frac{kq_1q_2}{r^2}$$

$$q_1q_2 = \frac{Fr^2}{k}$$

$$= \frac{1 \times 2^2}{9 \times 10^9} = \frac{4}{9 \times 10^9} = 4.44 \times 10^{-10}\text{C}$$

$q_1 + q_2 = 5.0 \times 10^{-5}\text{C}$  — i

$q_1q_2 = 4.44 \times 10^{-10}\text{C}$  — ii

$q_2 = 4.44 \times 10^{-10}$  — iii

$q_1$

Substitute eq (iii) into i

$$q_1 + 4.44 \times 10^{-10} = 5.0 \times 10^{-5}$$

$q_1$

Let  $q_1 = x$

$$\frac{x}{1} + \frac{4.44 \times 10^{-10}}{x} = 5.0 \times 10^{-5}$$

$$\frac{x^2 + 4.44 \times 10^{-10}}{x} = 5.0 \times 10^{-5}$$

$$x^2 + 4.44 \times 10^{-10} = 5.0 \times 10^{-5}x$$

$$x^2 - 5.0 \times 10^{-5}x + 4.44 \times 10^{-10} = 0$$

$$x = 3.85 \times 10^{-5}, \quad x = 1.15 \times 10^{-5}$$

Recall  $x = q_1$

From equation i

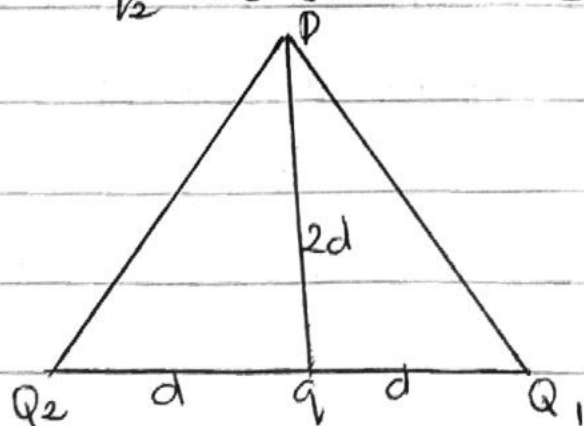
When  $q_1 = 3.85 \times 10^{-5}$

$$q_2 = 5.0 \times 10^{-5} - 3.85 \times 10^{-5} = 1.15 \times 10^{-5}$$

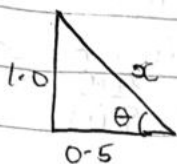
When  $q_1 = 1.15 \times 10^{-5}$

$$q_2 = 5.0 \times 10^{-5} - 1.15 \times 10^{-5} = 3.85 \times 10^{-5}$$

c.



$$d = 0.5 \text{ m}; Q_1 = Q_2 = 8 \mu\text{C} = 8 \times 10^{-6} \text{ C}; P = 0; 2d = 1 \text{ m}$$



$$\alpha^2 = 1^2 + 0.5^2$$

$$\alpha^2 = 1.25$$

$$\alpha = \sqrt{1.25} = \frac{\sqrt{5}}{2}$$

$$\tan \theta = \frac{1}{0.5}$$

$$\tan \theta = 2$$

$$\theta = \tan^{-1}(2)$$

$$\theta = 63.43^\circ$$

$$F_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{\left(\frac{\sqrt{5}}{2}\right)^2} = 57600 \text{ C}$$

$$F_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{\left(\frac{\sqrt{5}}{2}\right)^2} = 57600 \text{ C}$$

$$F_3 = \frac{kq}{r^2} = \frac{9 \times 10^9 \times q}{1^2} = 9 \times 10^9 q \text{ C}$$

Vector	Angle	x-Component	y-Component
57600	$63.43^\circ$	-25781.93	51507.78
57600	$63.43^\circ$	-25781.93	51507.78
$9 \times 10^9 q$	$90^\circ$	0	$9 \times 10^9 q$
		$\Sigma F_x = 0$	$\Sigma F_y = 103015.56 \times 9 \times 10^9 q$

$$E = \sqrt{E_{fx} + E_{fy}}$$

$$0 = \sqrt{(0)^2 + (103015.56 \times 9 \times 10^9 q)^2}$$

$$0 = \sqrt{103015.56 \times 9 \times 10^9 q^2}$$

$$0 = 103015.56 \times 9 \times 10^9 q$$

$$q = \frac{103015.56}{9 \times 10^9}$$

$$q = 1.1446 \times 10^{-5} \text{ C}$$

$$q = 11.45 \times 10^{-6} \text{ C}$$

$$q = 11 \mu\text{C}$$

## 2a Electric field

An electric field is a region of space in which an electric charge will experience an electric force

## Electric field intensity.

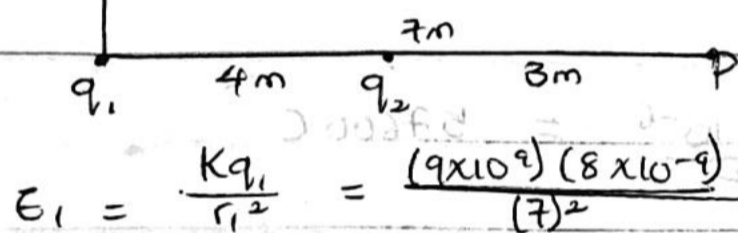
Electric field intensity  $E$  can be defined as the force per unit charge:

$$E = \frac{F(N)}{q_0(C)}$$

bi

$$Q_1 = 8 \text{ nC}$$

$$Q_2 = 12 \text{ nC}$$

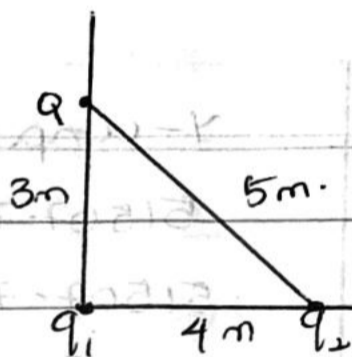


$$E_1 = \frac{Kq_1}{r_1^2} = \frac{(9 \times 10^9)(8 \times 10^{-9})}{(7)^2} = 1.47$$

$$E_2 = \frac{Kq_2}{r_2^2} = \frac{(9 \times 10^9)(12 \times 10^{-9})}{(3)^2} = 12$$

$$E_{\text{net}} = E_1 + E_2 = 1.47 + 12 = 13.47 \approx 13.5 \text{ N/C}$$

ii



$$E_1 = \frac{Kq_1}{r_1^2} = \frac{(9 \times 10^9)(8 \times 10^{-9})}{(3)^2} = 8$$

$$E_2 = \frac{Kq_2}{r_2^2} = \frac{(9 \times 10^9)(12 \times 10^{-9})}{(5)^2} = 4.32$$

$$E_{\text{net}} = E_1 + E_2 = 8 + 4.32 = 12.32 \approx 12.3 \text{ N/C}$$

4a Magnetic flux is defined as the strength of magnetic field represented by lines of force. It is usually represented by  $\Phi$

b.  $m = 9.11 \times 10^{-31} \text{ kg}$ ;  $r = 1.4 \times 10^{-10} \text{ m}$ ;  $B = 3.5 \times 10^{-1} \text{ weber/meter}^2$   
 $q = 1.6 \times 10^{-19} \text{ C}$

$$\text{Cyclotron frequency} = \frac{qB}{m}$$

$$= \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$= \frac{5.6 \times 10^{-20}}{9.11 \times 10^{-31}}$$

$$= 6.15 \times 10^{10} \text{ rad/s.}$$

Biot-Savart Law is an equation that describes the magnetic field created by a current-carrying wire, and allows you to calculate its strength at various points

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \varphi}{r^2}$$

$$\sin(\pi - \varphi) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \varphi)}{r^2}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \varphi)}{x^2 + y^2} \quad - i$$

$$\sin(\pi - \varphi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad - ii$$

Substituting ii into i

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

Recall  $dl = dy$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad - iii$$

Using special integrals

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$\therefore B = \frac{\mu_0 I a}{4\pi} \left[ \frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I a}{4\pi} \left[ \frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right]$$

$$B = \frac{\mu_0 I}{4\pi x} \left( \frac{2a}{(x^2 + a^2)^{1/2}} \right)$$

When the length  $2a$  of the conductor is very great in comparison to its distance  $x$  from point  $P$ , we consider it infinitely long. That is, when  $a$  is much larger than  $x$ ,

$$(x^2 + a^2)^{1/2} \approx a, \text{ as } a \rightarrow \infty$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

In a physical situation, we have axial symmetry about the  $y$ -axis. Thus, at all points in a circle of radius  $r$ , around the conductor, the magnitude of  $B$  is

$$B = \frac{\mu_0 I}{2\pi r}$$