

$$r = \sqrt{y^2 + x^2}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin\theta}{r^2}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dx}{(y^2 + x^2)(y^2 + x^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dx}{(y^2 + x^2)^{3/2}}$$

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{dx}{(y^2 + x^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I}{4\pi x} \left[\frac{xa}{(a^2 + x^2)^{1/2}} \right]$$

$$B = \frac{\mu_0 I}{2\pi x} \left[\frac{a}{(a^2 + x^2)^{1/2}} \right]$$

$$(x^2 + a^2)^{1/2} \approx a$$

$$a \gg x$$

$$B = \frac{\mu_0 I}{2\pi x} \frac{a}{(a^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{2\pi x} \quad x = r$$

$$B = \frac{\mu_0 I}{2\pi r}$$