

$$\frac{5.0 \times 10^{-5} + \sqrt{2.5 \times 10^{-9} - 1.72 \times 10^9}}{2}$$

$$= \frac{5.0 \times 10^{-5} + \sqrt{7.2 \times 10^{-10}}}{2}$$

$$\frac{5.0 \times 10^{-5} + 2.68 \times 10^{-5}}{2}$$

$$\frac{5.0 \times 10^{-5} + 2.68 \times 10^{-5} \text{ or } 5.0 \times 10^{-5} - 2.68 \times 10^{-5}}{2}$$

$$\frac{2.68 \times 10^{-5}}{2} \text{ or } \frac{2.39 \times 10^{-5}}{2}$$

$$\frac{3.84 \times 10^{-5}}{2} \text{ or } \frac{1.16 \times 10^{-5}}{2}$$

(c)  $q_1 = 3.84 \times 10^{-5}$  and  $q_2 = 1.16 \times 10^{-5}$  or vice versa

2a) Electric field is a region of space in which an electric charge will experience a electric force  
 Electric field Intensity can be defined as the force per unit charge.

b)  $E_1 = \frac{9 \times 10^9 \times 8 \times 10^{-4}}{7^2} = 1.5 \text{ N/C}$

$$E_2 = \frac{9 \times 10^9 \times 12 \times 10^{-4}}{3^2} = 12 \text{ N/C}$$

$$E_{\text{net}} = 12 + 1.5 = 13.5 \text{ N/C}$$

$$q/E_1 = \frac{9 \times 10^9 \times 8 \times 10^{-4}}{3^2} = 8 \text{ N/C}$$

$$E_2 = \frac{9 \times 10^9 \times 12 \times 10^{-4}}{5^2} = 4.32 \text{ N/C}$$

$$\frac{9 \times 10^9 \times 12 \times 10^{-4}}{25} = 4.32 \text{ N/C}$$

$$E_x = 3.46 \text{ N/C} \quad E_y = 10.59 \text{ N/C}$$

$$\sqrt{(3.46)^2 + (10.59)^2} = 11.14$$

1st  $E_{\text{net}} = 13.5 \text{ N/C}$

2nd  $E_{\text{net}} = 11.2 \text{ N/C}$



$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \phi}{r^2}$$

$$\sin(\pi - \phi) = \sin \phi$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{r^2}$$

from diagram  $r^2 = x^2 + y^2$  (Pythagoras theorem)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \phi)}{x^2 + y^2}$$

But  $\sin(\pi - \phi) = \frac{y}{\sqrt{x^2 + y^2}} = \frac{y}{(x^2 + y^2)^{1/2}}$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{y}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{y}{(x^2 + y^2)^{3/2}}$$

But  $dl = dy$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{y}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy$$

Using special integrals

$$\int \frac{dy}{(x^2 + y^2)^{3/2}}$$

$$= \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \left[ \frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

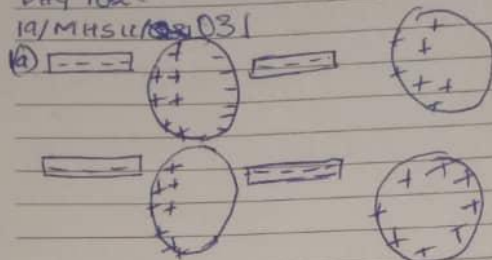
$$B = \frac{\mu_0 I}{4\pi} \left( \frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right)$$

$$B = \frac{\mu_0 I}{4\pi x} \left( \frac{2a}{x^2 + a^2} \right)^{1/2}$$

$(x^2 + a^2)^{1/2} = a$ , as  $a \rightarrow \infty$

$$B = \frac{\mu_0 I}{2\pi x}$$

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(D)  $f = \frac{kq_1q_2}{(r_{12})^2}$

$k = 9 \times 10^9$   
 $F = 10\text{N}$   
 $q_1 = ?$   
 $q_2 = ?$   
 $q_1 + q_2 = 5.0 \times 10^{-5}$

$F = \frac{kq_1q_2}{(r_{12})^2}$   
 $F \times (r_{12})^2 = kq_1q_2$   
 $q_1q_2 = \frac{F(r_{12})^2}{k}$   
 $= \frac{1 \times (0.2)^2}{9 \times 10^9}$   
 $= 4 / 9 \times 10^9$

$q_1q_2 = 4.44 \times 10^{-10}$   
 Since  $q_1 + q_2 = 5.0 \times 10^{-5}$   
 $q_1 = (5.0 \times 10^{-5}) - q_2$   
 $q_1q_2 = 4.4 \times 10^{-10}$   
 $[(5.0 \times 10^{-5}) - q_2] \times q_2 = 4.44 \times 10^{-10}$   
 $= 5.0 \times 10^{-5} q_2 - (q_2)^2 = 4.44 \times 10^{-10}$   
 $\therefore q_2 = 5.0 \times 10^{-5} + 4.44 \sqrt{10^{-10}} = 0$   
 using quadratic formula



$\sqrt{-2.56 \times 10}$   
 size 3  
 $1 = 10 \mu\text{C}$   
 $2 = -20 \mu\text{C}$   
 $2 \times 10^{-9} \text{C}$   
 $4 \pi \epsilon_0 d$   
 $\frac{1}{4 \pi \epsilon_0 d^2}$   
 $\frac{2}{d^2}$   
 $2(4)$   
 $2(16)$   
 $3$   
 $6d + 32$   
 $1d - 4$   
 $b^2 - 4$   
 $2$   
 $(-2)$

4) Magnetic flux? is defined as the strength of the magnetic field which can be represented by line of force. It is represented by the symbol  $\Phi$  mathematically given as  $\Phi = B \cdot dA$

(b)  $m = 9.11 \times 10^{-31} \text{ kg}$ ,  $r = 1.4 \times 10^{-9} \text{ m}$ ,  $B = 3.5 \times 10^{-1} \text{ weber/meter}$

Cyclotron frequency = angular speed

$$\omega = \frac{v}{r} = \frac{qB}{m}$$

$$\omega = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}$$

$$\omega = 62222.2222 \text{ T}^{-1}$$

(c) We were given parameter such as

(i) mass of the electron =  $9.11 \times 10^{-31} \text{ kg}$

(ii) A radius of  $1.4 \times 10^{-9} \text{ m}$

(iii) Magnetic field of  $3.5 \times 10^{-1} \text{ weber/meter square}$  and we were asked to find the cyclotron

frequency which is equal or the same thing as angular speed. It is called cyclotron frequency because it is a frequency of an accelerated charged

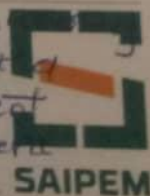
cyclotron. Recall that angular speed is given as

$$\omega = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}$$

$$= 62222.2222 \text{ T}^{-1}$$

(b) State the Biot-Savart law

The Biot-Savart law is based on the following observations for the magnetic field  $\vec{dB}$  at a point  $P$  associated with a length element  $d\vec{l}$  at a wire carrying a steady current



$$(-9.56 \times 10^3)^2 + C = 5$$

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$$1 = 10 \text{ uC}$$

$$2 = -2 \text{ uC}$$

$$2 \times 10^{-9} \text{ C} = 0$$

$$q_1 \epsilon_0 r^2 = 0$$

$$\epsilon_0 (d)^2 = 0$$

$$\frac{2}{d^2} = \frac{10}{4}$$

$$2(4+d)^2 = 10$$

$$2(16+8d+d^2) = 10$$

$$32+16d+d^2 = 5$$

$$32+16d+d^2 - 5 = 0$$

$$27+16d+d^2 = 0$$

$$d^2 + 16d + 27 = 0$$

$$-2d - 4 = 0$$

$$b \pm \sqrt{b^2 - 4ac}$$

$$= \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(27)}}{2(1)}$$