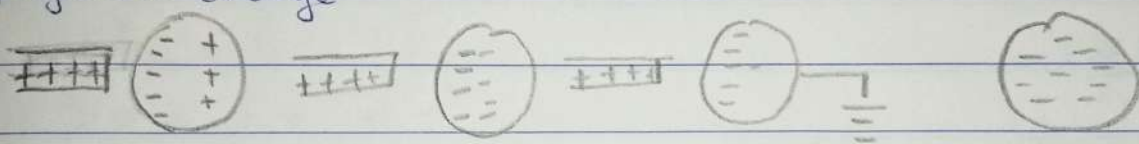


Chima - Dim Eberedukwu
19/mhs01/127 MBBS

16. A positively charged rubber rod will be brought near a neutral (uncharged) conducting sphere that is insulated so that there is no conducting path to the ground. The repulsive force between the electrons in the rod and those in the sphere cause a redistribution of charges on the sphere. That, some protons move to the side of the sphere far from the rod. The region of the sphere nearest the positively charged rod has excess negative charge. Then a grounded conducting wire is then connected to the sphere. Then the wire to the ground is then removed, the conducting sphere is left with an excess of induced negative charge.



$$76 \quad q_1 + q_2 = 5 \times 10^{-5} \text{ C}$$

$$F = \frac{k q_1 q_2}{r^2}$$

$$1 = \frac{9 \times 10^9 \times (5 \times 10^{-5} - q_2) q_2}{2^2}$$

$$4 = 9 \times 10^9 \times (5 \times 10^{-5} - q_2) q_2$$

$$4 = (4.5 \times 10^5 - 9 \times 10^9 q_2) q_2$$

$$4 = (4.5 \times 10^5 q_2 - 9 \times 10^9 q_2^2)$$

$$9 \times 10^9 q_2^2 - 4.5 \times 10^5 q_2 + 4 = 0$$

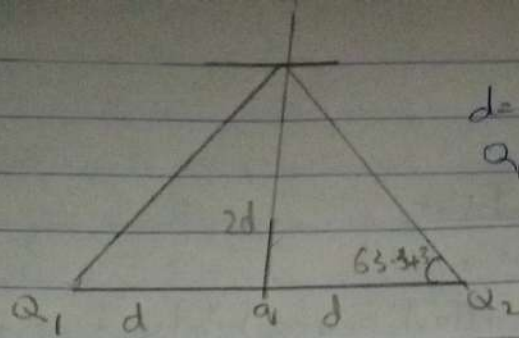
$$q_2 = 3.84 \times 10^{-5} \text{ C}$$

Since it's a quadratic equation

$$q_1 = 1.156 \times 10^{-5} \text{ C}$$

$$\therefore q_1 = 1.156 \times 10^{-5} \text{ C} \quad \text{and} \quad q_2 = 3.84 \times 10^{-5} \text{ C}$$

1c



$$d = 0.5$$

$$Q_1 = Q_2 = 8 \times 10^{-6} \text{ C}$$

$$\sqrt{0.5^2 + 1^2} = 1.12 \text{ (pythagoras theorem)}$$

$$E_p = E_{Q_1} + E_{Q_2} + E_q$$

$$E_{Q_1} = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{1.12^2} = 57600 \text{ N/C}$$

$$E_{Q_2} = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{1.12^2} = 57600 \text{ N/C}$$

$$E_q = \frac{kQ}{r^2} = \frac{9 \times 10^9 \times q}{1} = 9 \times 10^9 \times q \text{ N/C}$$

	θ	X component	Y component
57600 N/C	63.43°	57600 cos 63.43 = -25764	57600 sin 63.43 = 51516.8
57600 N/C	63.43	57600 cos 63.43 = +25764	57600 sin 63.43 = 51516.8
$9 \times 10^9 q \text{ N/C}$	90°	$9 \times 10^9 q \cos 90$ = 0	$9 \times 10^9 q \sin 90$ = $9 \times 10^9 q$
		$E_{fx} = 0$	$E_{fy} = 103033.6 + 9 \times 10^9 q$

$$\text{Point P} = 0$$

$$E_{\text{net}} = \sqrt{0^2 + (103033.6 + 9 \times 10^9 q)^2}$$

$$0 = 0 + 103033.6 + 9 \times 10^9 q$$

$$\frac{9 \times 10^9 q}{9 \times 10^9} = \frac{-103033.6}{9 \times 10^9}$$

$$q = -1.144817778 \times 10^{-5}$$

$$q = -11.4 \times 10^{-6}$$

$$q = -11.4 \times 10^{-6} \text{ N/C}$$

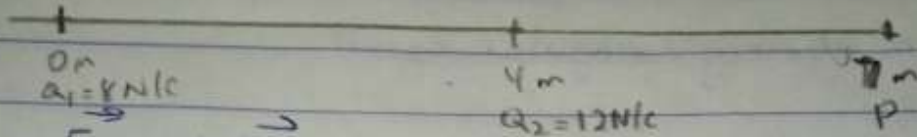
2 Electric field

It is a region of space in which an electric charge will experience an electric force

Electric field intensity

It is defined as the force per unit charge

2i



$$\vec{E}_p = \vec{E}_{q_1} + \vec{E}_{q_2}$$

$$E_{q_1} = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{7^2} = \frac{72}{49} = 1.47 \text{ N/C}$$

$$E_{q_2} = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{3^2} = \frac{108}{9} = 12 \text{ N/C}$$

$$\vec{E}_p = \vec{E}_{q_1} + \vec{E}_{q_2}$$

$$E_p = 1.47 + 12$$

$$E_p = 13.5 \text{ N/C}$$

2ii

$$E_{q_1} = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{3^2} = 8 \text{ N/C}$$

$$E_{q_2} = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{5^2} = 4.32 \text{ N/C}$$

	x-component	y-component
90	$8 \cos 90 = 0$	$8 \sin 90 = 8$
36.87	$4.32 \cos 36.87 = 3.46$	$4.32 \sin 36.87 = 2.59$
	$X_{\text{comp}} = 3.46$	$Y_{\text{comp}} = 10.59$

$$\text{magnitude} = \sqrt{(3.46)^2 + (10.59)^2}$$

$$= \sqrt{124.16}$$

$$E_a = 11.14 \text{ N/C}$$

No 4

4. Magnetic flux is a measurement of the total magnetic field which passes through a given area. It is a useful tool for helping describe the effects of the magnetic force on something occupying a given area.

b cyclotron frequency = angular speed

$$\omega = \frac{qB}{m_p}$$

$$\omega = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\omega = 6.15 \times 10^{10} \text{ rad/s}$$

$6.15 \times 10^{10} \text{ rad/s}$ is the angular speed is often referred to as the cyclotron frequency because the charge particle circulates at this angular frequency or angular speed in the type of accelerator called cyclotron.

5a Biot-savart law

$$dB = \frac{\mu_0}{4\pi} \times \frac{Idl \times r}{r^2}$$

μ_0 is a constant called permeability of free space

$$\mu_0 = 4\pi \times 10^{-7} \text{ T.m/A}$$

5b) Using Biot-savart law, we have

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \varphi}{r^2}$$

$$\sin(\pi - \varphi) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \varphi)}{r^2}$$

- $r^2 = x^2 + y^2$ (pythagoras theorem)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \varphi)}{x^2 + y^2} \quad \dots \text{equ (i)}$$

$$\sin(\pi - \varphi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \dots \text{equ (ii)}$$

Substituting equ (ii) into equ (i)

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

Recall $dl = dy$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{+ equ (iii)}$$

$$B = \frac{\mu_0 I}{4\pi} \left(\frac{2a}{x^2(x^2 + a^2)^{1/2}} \right)$$

$$B = \frac{\mu_0 I}{4\pi x} \left(\frac{2a}{(x^2 + a^2)^{1/2}} \right)$$

Using special integrals

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

$B = \frac{\mu_0 I}{2\pi r}$ Biot-savart law
Show that the magnitude is a straight line

Equ (iii) therefore becomes