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MATRIC NO:- 19/MHS11/111

COURSE :- PHY 102 ASSIGNMENT

Electric field & electric field intensity

Electric field

It is a region of space in which an electric charge will experience an electric force.

Electric field intensity

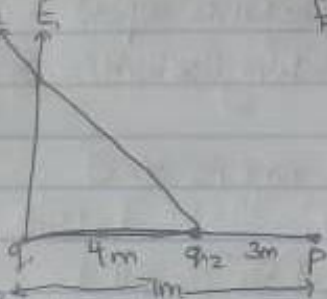
It is the force per unit charge.

$q_1 = 8 \mu\text{C}$  at origin,  $q_2 = 12 \mu\text{C}$  on x-axis at  $x = 4 \text{ m}$

Find electric field at point P on the x-axis at  $x = 7 \text{ m}$

(i) Electric field at a point Q on the y-axis at  $y = 3 \text{ m}$  due to the charges

(i)  $E_1$

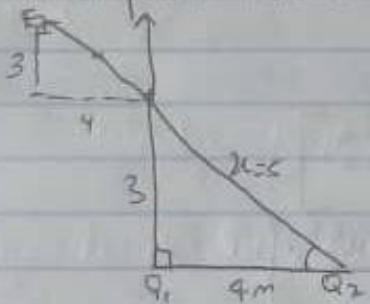


$$E_1 = \frac{kQ_1}{r_1^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{7^2} = 1.469 \text{ N/C} \approx 1.5 \text{ N/C}$$

$$E_2 = \frac{kQ_2}{r_2^2} = \frac{9 \times 10^9 \times 12 \times 10^{-6}}{3^2} = 12 \text{ N/C}$$

$$\Rightarrow E_{\text{net}} = E_1 + E_2 = 1.5 + 12 = 13.5 \text{ N/C}$$

(ii)  $E$  at point Q on the y-axis at  $y = 3 \text{ m}$  due to charge



$$c^2 = a^2 + b^2$$

$$c^2 = 4^2 + 3^2$$

$$c = 5$$

$$E_1 = \frac{kQ_1}{r_1^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{3^2} \quad E_1 = 8 \text{ N/C}$$

$$E_2 = \frac{kQ_2}{r_2^2} = \frac{9 \times 10^9 \times 12 \times 10^{-6}}{5^2} = 4.32 \text{ N/C}$$

| Vector                | Angle         | x-comp                           | y-comp                           |
|-----------------------|---------------|----------------------------------|----------------------------------|
| $E_1 = 8 \text{ N/C}$ | $90^\circ$    | $0 \text{ N/C}$                  | $8 \text{ N/C}$                  |
| $E_2 = 4.32$          | $36.87^\circ$ | $-3.45 \text{ N/C}$              | $2.59 \text{ N/C}$               |
|                       |               | $\Sigma F_x = -3.45 \text{ N/C}$ | $\Sigma F_y = 10.59 \text{ N/C}$ |

$$E_{\text{net}} = \sqrt{E_x^2 + E_y^2}$$

$$E_{\text{net}} = 11.12 \text{ N/C}$$

3. Formulation of identities of charge

(a) Volume charge density  $\rho = \frac{dq}{dv} = dq = \rho dv$

(b) Surface charge density  $\sigma = \frac{dq}{dA} = dq = \sigma dA$

(c) Linear charge density  $\lambda = \frac{dq}{dl} = dq = \lambda dl$

b electric potential difference equation

- due to a single point charge

$$V_B - V_A = \frac{Q}{4\pi\epsilon_0} \left[ \frac{1}{r_B} - \frac{1}{r_A} \right]$$

where  $Q$  = point charge

$V$  = electric potential

$r_B$  = distance of  $Q$  to point  $B$

$r_A$  = distance of  $Q$  to point  $A$

- due to several point charges

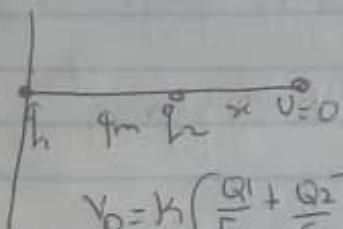
$$V = \frac{1}{4\pi\epsilon_0} \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right] \text{ where } V = \text{electric potential}$$

$Q$  = point charge

$r$  = distance of  $Q$

30 point charge  $Q_1 = 10 \mu\text{C}$   $Q_2 = -2 \mu\text{C}$  along  $x$ -axis  $x=0$   
 $x=4\text{m}$  respectively.

find the position along the  $x$ -axis where  $V=0$



$$V_P = \frac{1}{4\pi\epsilon_0} \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right] \text{ recall } \frac{1}{4\pi\epsilon_0} = 9 \times 10^9$$

$$V_P = k \left[ \frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$V_P = 9 \times 10^9 \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = 9 \times 10^9 \left[ \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4+x} - \frac{2 \times 10^{-6}}{x}$$

$$10 \times 10^{-6} x = (4+x)(-2 \times 10^{-6})$$

$$10 \times 10^{-6} x = -8 \times 10^{-6} - 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = -10 \times 10^{-6} x - 2 \times 10^{-6} x$$

$$10 \times 8 \times 10^{-6} = 8 \times 10^{-6} x$$

$$x = \frac{8 \times 10^{-6}}{8 \times 10^{-6}}$$

$$x = 1$$

$$x = 1$$

$\therefore$  position along the  $x$ -axis is  $1\text{m}$ .  
where  $V=0$



$$V = k \left[ \frac{q_1}{r_1} + \frac{q_2}{r_2} \right]$$

$$0 = \left[ \frac{10 \times 10^{-6}}{4-x} + \frac{-2 \times 10^{-6}}{x} \right],$$

$$\frac{2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4-x}$$

$$[4-x] [2 \times 10^{-6}] = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} - 2 \times 10^{-6} x = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} = 10 \times 10^{-6} x + 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 12 \times 10^{-6} x$$

$$x = \frac{8 \times 10^{-6}}{12 \times 10^{-6}}$$

$$x = 0.67 \text{ m}$$

$\therefore$  position of  $V=0$  is  $0.67 \text{ m}$

### SECTION B

(49) Magnetic flux is defined as the strength of the magnetic field which can be represented by line of forces. It is denoted as  $\phi$

$$\phi = B \cdot dA$$

(45)  $m_e = 9.11 \times 10^{-31} \text{ kg}$ ,  $r = 1.4 \times 10^{-7} \text{ m}$ ;  $B = 3.5 \times 10^{-1} \text{ Wb/m}^2$

Cyclotron frequency = angular speed -  $q = 1.6 \times 10^{-19}$

$$f_B = \frac{qVB}{r} = \frac{m_e v^2}{r}$$

$$MeV = qBr$$

$$v = \frac{qBr}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1} \times 1.4 \times 10^{-7}}{9.11 \times 10^{-31}}$$

$$v = 8.61 \times 10^{-3} \text{ m/s}$$

$$\omega = \frac{v}{r} = \frac{qB}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\omega = 6.14 \times 10^0 \text{ e}^{-1}$$

(46) In Q6 we were given parameters, mass of electron =  $9.11 \times 10^{-31} \text{ kg}$   
radius =  $1.4 \times 10^{-7} \text{ m}$   $B = 3.5 \times 10^{-1} \text{ Wb/m}^2$

And we were asked to find the cyclotron frequency which is the

Same thing as angular speed - It is called cyclotron frequency because it is a frequency of an accelerator called cyclotron.

$\omega = \text{angular speed}$

$\omega = \frac{qB}{m_e}$  Since cyclotron frequency = angular speed  
The cyclotron frequency =  $6.19 \times 10^{14} \text{ s}^{-1}$

having a unit of  $\frac{1}{\text{s}}$  which is the unit of frequency dimensionally.

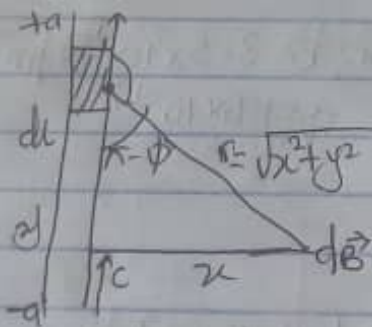
5) Bio-Savart law states that the magnetic field is directly proportional to the product permeability of free space ( $\mu_0$ ) the current (I), the change in length, the radius ~~or~~ and inversely proportional to the square of radius ( $r^2$ ) mathematically -

$$d\vec{B} = \frac{\mu_0 I d\vec{l} \times \hat{r}}{4\pi r^2}$$

where  $\mu_0 = \text{permeability of free space} = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$   
 $r = \text{radius}$

$d\vec{B} = \text{magnetic field}$ ,  $I = \text{steady current}$ ,  $d\vec{l} = \text{length of wire}$   
unit is  $\text{Wb/m}^2$ .

6) magnetic field of a straight current carrying conductor



A section of a straight current carrying conductor.

Applying Bio-Savart law, we find the magnitude of the field ( $B$ ) from the diagram,

$$B = \frac{\mu_0 I}{4\pi} \int_a^b \frac{dl \sin \phi}{r^2}$$

$$\sin(\pi - \phi) = \sin \theta$$

$$B = \frac{\mu_0 I}{4\pi} \int_a^b \frac{dl \sin(\pi - \phi)}{r^2}$$

from the diagram  $r^2 = x^2 + y^2$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \sin(\pi - \phi)}{x^2 + y^2} = \dots \text{--- (i)}$$

$$\text{But } \sin(\pi - \phi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \dots \text{--- (ii)}$$

substitute (ii) into (i)

$$B = \frac{\mu_0 I}{4\pi} \int_a^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

$$dl = dy; \quad B = \frac{\mu_0 I x}{4\pi} \int_a^a \frac{1}{(x^2 + y^2)^{3/2}} dy \dots \text{--- (iii)}$$

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi x} \left( \frac{2a}{(x^2 + a^2)^{1/2}} \right) \because (x^2 + a^2)^{1/2} = a = 0$$

$$B = \frac{\mu_0 I}{2\pi x} = \frac{\mu_0 I}{2\pi r}$$