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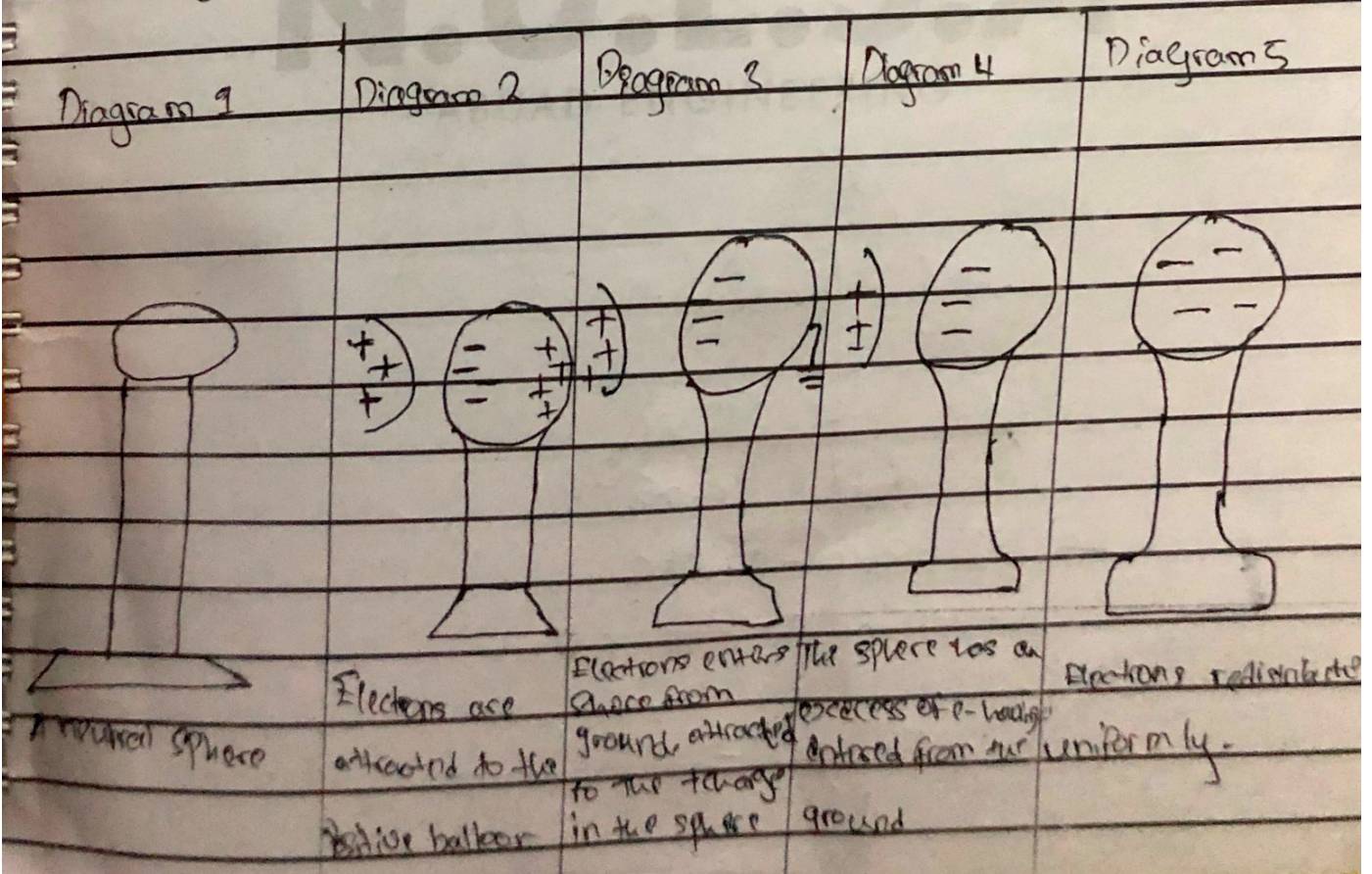
DEPARTMENT: PETROLEUM ENGINEERING

MATRIC NO: 19/ENG07/005

COURSE CODE: PHY 102

~~INDUCTION~~

① If a negatively charged object is used to charge a neutral object by induction, then the neutral object will acquire a positive charge. And if a positively charged object is used to charge. If you understand the induction charging process, you can see why this would always be the case. The object that is brought near will always repel like charges and attract opposite charges. Either way, the object being charged requires a charge that is opposite the charge of the object used to induce the charge. To further illustrate this, the diagram below shows how a positively charged balloon will charge a sphere negatively by induction.



B) $q_1 q_2 = 5.0 \times 10^{-5} \text{ C}, F = 1.0 \text{ N}, r = 2.0 \text{ m}$

$E = 1.0$

$F = k \frac{q_1 q_2}{r^2}$

$q_1 q_2 = \frac{Fr^2}{k}$

$q_1 q_2 = \frac{1.0 \times 20}{9 \times 10^9}$

$q^2 = 2.22 \times 10^{-10}$

$q = \sqrt{2.22 \times 10^{-10}}$

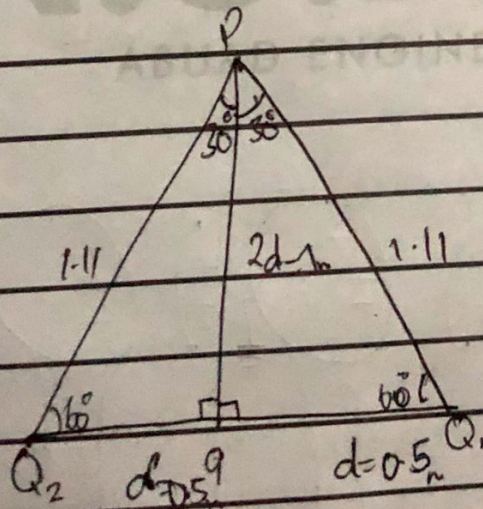
$q = 1.48 \times 10^{-5}$

$(5.0 \times 10^{-5}) - (1.48 \times 10^{-5}) = 3.52 \times 10^{-5}$

$q_1 = 1.48 \times 10^{-5} \text{ C}, q_2 = 3.52 \times 10^{-5} \text{ C}$

or

$q_1 = 3.52 \times 10^{-5} \text{ C}, q_2 = 1.48 \times 10^{-5} \text{ C}$



$Q_1 = Q_2 = 8 \mu\text{C} = 8 \times 10^{-6} \text{ C}$

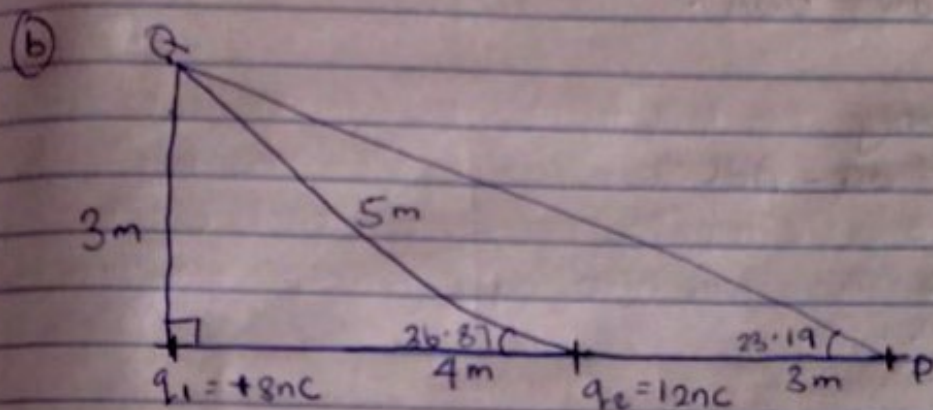
$d = 0.5 \text{ m}, r = \frac{d}{2} = 0.25$

~~$F = k \frac{q_1 q_2}{r^2} = \frac{(8 \times 10^{-6}) \times (8 \times 10^{-6})}{(0.25)^2}$~~

(a) Electric field: It is a region of space in which an electric charge will experience an electric force.

Electric field intensity: It can be defined as the force per unit charge.

$$E = \frac{F(N)}{q_0(C)}$$



$$(i) E_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{7^2} = 1.47$$

$$E_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{3^2} = 12$$

$$= 13.47 \text{ N/C}$$

$$(ii) E_1 = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{9} = 8$$

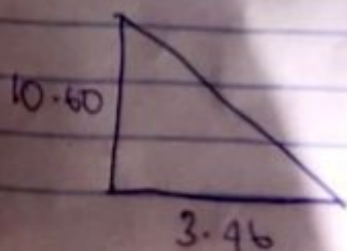
$$E_2 = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{5^2} = 4.32$$

x	y
$8 \times \cos(90)$	$8 \times \sin(90)$
$= 0$	8

$4.32 \times \cos(36.87)$	$4.32 \times \sin(36.87)$
$= 3.46$	2.60

3.46	10.60
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3.46	10.60
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$$x = \sqrt{10.6^2 + 3.46^2} = 11.15 \text{ N/C}$$

1

(3) a)

i) Volume charge density

$$\rho = \frac{dq}{dv} \rightarrow dq = \rho dv$$

ii) Surface charge density

$$\sigma = \frac{dq}{dA} \rightarrow dq = \sigma dA$$

iii) Linear charge density

$$\lambda = \frac{dq}{dl} \rightarrow dq = \lambda dl$$

- (b)

$$dW = F \cdot dl$$

$$F = -q_0 E$$

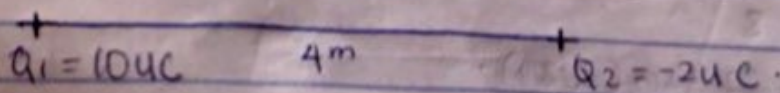
$$dW = -q_0 E dl$$

$$W(A \rightarrow B)_{q_0} = -q_0 \int_A^B E dl$$

$$V_B - V_A = \frac{W(A \rightarrow B)_{q_0}}{q_0} \quad \text{it follows the definition} \quad \equiv$$

$$V_B - V_A = - \int_A^B E dl$$

3c)



$$Q_1 = 10 \mu C \quad Q_2 = -2 \mu C$$

$$V = \frac{1}{4\pi\epsilon_0} \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$\frac{0}{9 \times 10^9} = \frac{10 \times 10^{-6}}{r_1} - \frac{2 \times 10^{-6}}{r_2}$$

$$2r_1 = 10r_2 \quad ; \quad r_1 = 5r_2$$

Referring to the diagram above, the position along the x-axis where $V = 0$ is 5m from $Q_1 = 10\mu C$ and 1m from $Q_2 = -2\mu C$.

4a) Magnetic Flux is defined as the strength of the magnetic field which be ~~represented~~^{represented} by line of force. It is represented by the symbol Φ mathematically given as $\Phi = B \cdot dA$.

b) $m = 9.11 \times 10^{-31} \text{ kg}$, $r = 1.4 \times 10^{-2} \text{ m}$, $B = 3.5 \times 10^{-1} \text{ weber/meter}^2$
cyclotron Frequency = angular speed

$$\omega = \frac{v}{r} = \frac{qB}{m}$$

$$\omega = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}$$

$$\omega = 62222.2222 \text{ T}^{-1}$$

c) We were given parameters such as

i) mass of the electron = $9.11 \times 10^{-31} \text{ kg}$

ii) A radius of $1.4 \times 10^{-2} \text{ m}$.

iii) Magnetic field of $3.5 \times 10^{-1} \text{ weber/meter square}$.

and we were asked to find the cyclotron frequency which is equal the same thing as angular speed. It is called cyclotron frequency because it is a frequency of an accelerator called ~~also~~ cyclotron.

Recall that angular speed is given as $\omega =$ substituting we

$$\text{have } \omega = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}$$

$$= 62222.2222 \text{ T}^{-1}$$

change in length, the radius and the radius (r). It can be represented mathematically by where called permeability of free space. The unit of is weber/meter

$$B = \frac{\mu_0 I}{4\pi} \frac{dl \times r}{r^2}$$

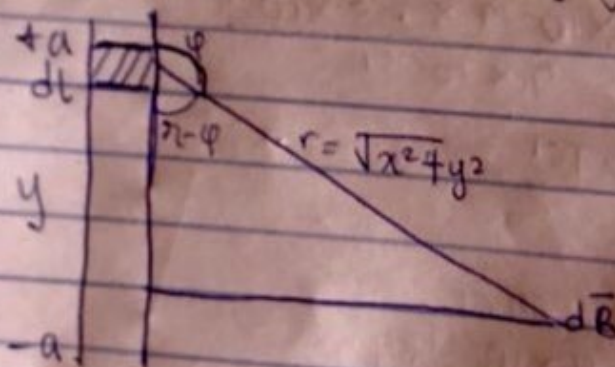
(5) Biot Savart law is an equation that describes the magnetic field by a current-carrying wire, and allows you to calculate it at various points. And we replace the electric field E magnetic field element dB because a moving charge produces field not an electric field.

$$B = \frac{\mu_0 I}{4\pi} \int \frac{d\vec{s} \times \vec{r}}{r^2}$$

Permeability of free space length of segment Radical direction
Distance

$$\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$$

(b) Section of a straight current carrying conductor.



$$B = \frac{\mu_0 I}{4\pi x} \left(\frac{2a}{(x^2 + a^2)^{1/2}} \right)$$

When the length 2a of the conductor is very great in comparison distance x from point P, we consider it infinitely long. That is much larger than x,

$$(x^2 + a^2)^{1/2} \approx a \text{ as } a \rightarrow \infty$$

$$B = \frac{\mu_0 I}{2\pi x}$$

In a physical situation, we have axial symmetry about y-axis. Thus, at points in a circle of radius r , around the conductor, the magnitude of B is

$$B = \frac{\mu_0 I}{2\pi r} \dots \text{--- (1)}$$

Equation (1) defines the magnitude of the magnetic ~~field~~ field of flux B near a long, straight current carrying conductor.

(16)

Given $q_1 + q_2 = 5 \times 10^{-5} \text{ C}$

$$F = \frac{kq_1q_2}{r^2}$$

$$q_1 = 5 \times 10^{-5} \text{ C} - q_2$$

$$\frac{q_1q_2}{k} = \frac{Fr^2}{k} = \frac{1 \times 2^2}{9 \times 10^9} = \frac{4}{9} \times 10^{-9}$$

$$1 = \frac{9 \times 10^9 (5 \times 10^{-5} - q_2)q_2}{2^2}$$

$$4 = 4.5 \times 10^5 q_2 - 9 \times 10^9 q_2^2$$

$$9 \times 10^9 q_2^2 - 4.5 \times 10^5 q_2 + 4 = 0$$

Using : $q_2 = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $a = 9 \times 10^9$ $b = -4.5 \times 10^5$ $c = 4$

$$q_2 = \frac{4.5 \times 10^5 \pm \sqrt{(-4.5 \times 10^5)^2 - 4(9 \times 10^9)(4)}}{2(9 \times 10^9)}$$

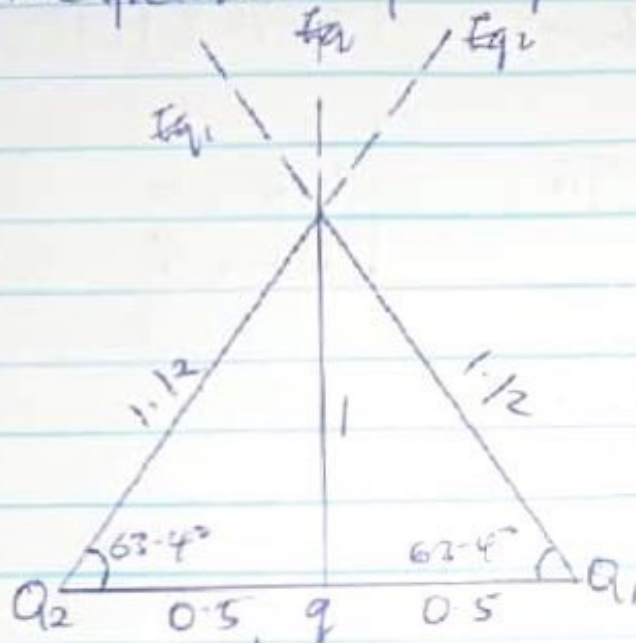
$$q_2 = \frac{4.5 \times 10^5 \pm \sqrt{5.85 \times 10^{10}}}{1.8 \times 10^{10}}$$

$$q_2 = 3.84 \times 10^{-5} \text{ C} \quad \text{OR} \quad q_2 = 1.16 \times 10^{-10} \text{ C}$$

$$q_2 = 0.0000380 \approx 3.8 \times 10^{-5} \text{ C}$$

c. $q_1 = q_2 = 8 \text{ nC}$
 $d = 0.5 \text{ m}$

If electric field at a point P is zero.



$$x^2 = 1^2 + 0.5^2$$

$$\sqrt{x} = \sqrt{1.25}$$

$$x = 1.12$$

$$\tan \theta = \frac{\text{opp}}{\text{adj}}$$

$$\tan \theta = \frac{1}{0.5}$$

$$\tan \theta = 2$$

$$\theta = \tan^{-1}(2)$$

$$\theta = 63.4^\circ$$

$$E_1 = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2}$$

$$E_1 = E_2 = 57397.95918$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times q}{1} = 9 \times 10^9 q$$

Vector	Angle	x-component	y-component
E_1 = 5739795918	63.4°	2570.046785	5132.2658
E_2 5739795918	63.4°	2570.045785	5132.268
$E_3 = 9 \times 10^9 q$	90°	$\cos \theta = 0$ $E_x = 0$	$9 \times 10^9 q$ $E_y = 10$

$$\text{Magnitude} = \sqrt{(E_x)^2 + (E_y)^2}$$

$$E_y = \sqrt{(0)^2 + (10264.52568)^2}$$

Since $E_x = 0$

$$0 = 9 \times 10^9 q + 10264.52568$$

Making q subject of formula.

$$q = \frac{10264.52568}{9 \times 10^9}$$

$$q = 1.140502853 \times 10^{-16}$$

$$q = 11.4 \text{ Mc}$$