

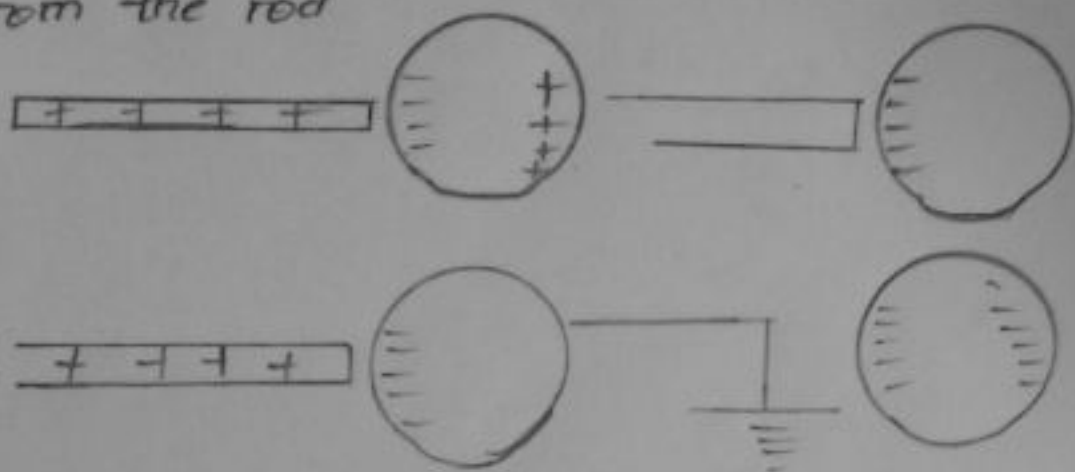
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Course: Phy 102

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1a charging by induction: It can be obtained without touching it by a process called electrostatic induction. Consider a positively charged rod brought near a neutral conducting sphere that is insulated so that there is no conducting path. The repulsive force between the protons in the rod and those in the sphere causes a redistribution of charges on the sphere so that some protons move to the side of the sphere farthest from the rod.



b $k = 9 \times 10^9$

$$q_1 = q_2 = 5 \times 10^{-5} \text{ C}$$

$$F = 1 \text{ N}$$

$d = 2 \text{ m}$ calculate the charge on each sphere?

Recall that

$$k = 9 \times 10^9$$

$$F = \frac{k q_1 q_2}{r^2}$$

$$F = \frac{9 \times 10^9 \times (q_1 q_2 \times 5 \times 10^{-5})}{2^2}$$

$$4 = 9 \times 10^9 \times 5 \times 10^{-5} q_2 + 9 \times 10^9 q_1$$

$$4 = 4.5 \times 10^5 q_2 + 9 \times 10^9 q_1$$

$$9 \times 10^9 q_2 - 4.5 \times 10^5 q_1 + 4 = 0$$

$$q_2 = 0.006038 \text{ C}$$

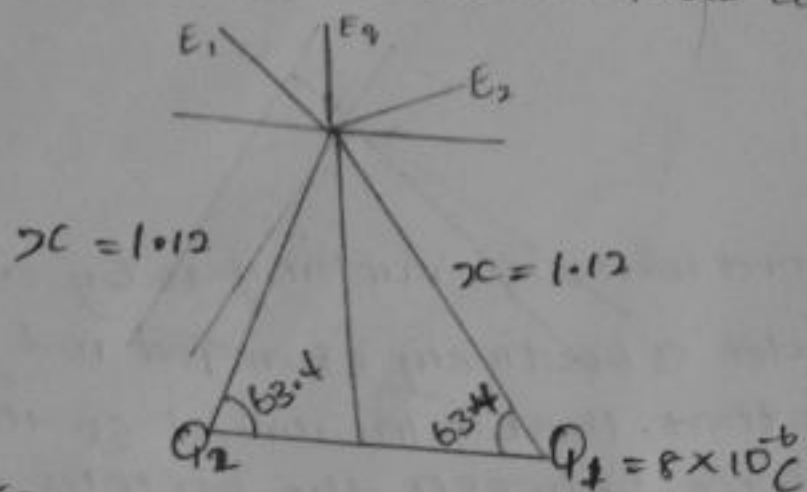
$$q_1 = 1.11 \times 10^{-5} \text{ C}$$

$$q_2 = 3.8 \times 10^{-5} \text{ C}$$

C

$Q_1 = Q_2 = 8 \mu C, d = 0.5$

determine Q if electric field at a point P is zero



$$E_1 = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2} = 5739.795918$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{1.12^2} = 5739.795918$$

$$E_q = \frac{kq}{r^2} = \frac{9 \times 10^9 \times q}{1} = 9 \times 10^9 q$$

$\tan \theta = \frac{opp}{adj} = \frac{1}{0.5} \Rightarrow \theta = \tan^{-1}(2), \theta = 63.4$

$x^2 = 1^2 + 0.15, \sqrt{x^2} = \sqrt{1.25}, x = 1.12$

vector	angle ^o	x-comp	y-comp
$E_1 = 5739.795$	63.4	$E_1 \cos \theta = 2570.045$	5132.262839
$E_2 = 5739.795$	63.4	2570.045	5132.262839
$E_q = 9 \times 10^9 q$	90^o	$E_q \cos \theta = 0$	$9 \times 10^9 q$
		$\Sigma x = 0$	$E_y = 10264.52568$

~~mag~~ magnitude = $\sqrt{(\Sigma x)^2 + (\Sigma y)^2}$

$E_q = \sqrt{(0)^2 + (10264.52568)^2}, \sin E = 0$

$0 = 9 \times 10^9 q + 10264.52568$

making q the subject of the formula

$q = \frac{-10264.52568}{9 \times 10^9}$

$q = 1.14 \times 10^{-6} \Rightarrow q = 1.14 \mu C$

3a) volume charge density, $P = \frac{dQ}{dV} = \rho dV$

surface charge density; $\theta = \frac{dQ}{dA} \Rightarrow n dQ = \theta dA$

Linear charge density $\lambda = \frac{dq}{dl}$ and $Q = \lambda dl$

b. Electric potential difference between two parts in an electric field can be defined as the work done per unit charge against electrical force when a charge is transported from one part to another. It is measured in Volt (V) or joules per coulomb (J/C). It is a scalar quantity.

4a. Section B
Magnetic flux is defined as the strength of the magnetic field which can be represented by line of forces. It is represented by the symbol Φ . Mathematically $\rightarrow \Phi = BA \cos \theta$.

b. $m = 9 \times 10^{-31} \text{ kg}$, $r = 1.4 \times 10^{-7} \text{ m}$, $B = 3.5 \times 10^{-1} \text{ weber / meter}^2$

Cyclotron frequency = angular speed. $\omega = \frac{v}{r} = \frac{qB}{m}$

$$\omega = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}, \quad \omega = 622.2 \text{ r}^{-1}$$

c. mass of the electron = $9.11 \times 10^{-31} \text{ kg}$.

radius of $1.4 \times 10^{-7} \text{ m}$, magnetic field of $3.5 \times 10^{-1} \text{ T}$

Angular speed $\rightarrow \omega = \frac{v}{r} = \frac{qB}{m}$

$$\text{Substituting } \omega = \frac{v}{r} = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}} = 622.22 \text{ r}^{-1}$$

Cyclotron frequency = angular speed, cyclotron frequency is equal to 622.22 having a unit as r^{-1} which is equal to the unit of frequency dimensionally.

b. Biot-Savart Law states that the magnetic field is directly proportional to the product permeability of free space (μ_0), the current (I), the charge in length, the radius is inversely proportional to the square of radius (r^2). It can be represented mathematically

$$\text{as } dB = \frac{\mu_0}{4\pi} \frac{I d\mathbf{l} \times \mathbf{r}}{r^2}$$

$\mu_0 = \text{constant}$. Called permeability of free space

$$\mu_0 = 4\pi \times 10^{-7} \frac{\text{N}}{\text{A}^2}, \text{ the unit of } B \text{ is } \text{Wb/m}^2$$

magnetic field of a straight current carrying conductor.

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{q \sin \theta}{r^2}$$

Since $(\pi - \theta) = \sin \theta$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{d(\sin(\pi - \theta))}{r^2}$$

$r^2 = x^2 + y^2$ (Pythagoras's theorem).

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{(\mu_0 I \sin(\pi - \theta) - \theta)}{x^2 + y^2}$$

$$\text{But } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad -2$$

Sub 2 into 1

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \cdot x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

Recall that $dl = dy = B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \cdot x}{(x^2 + y^2)^{3/2}}$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{\mu_0 I x}{4\pi} \int_a^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad (3)$$

Using special integrals:

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

Equation 3 becomes

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]$$

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right]$$

$$B = \frac{\mu_0 I}{4\pi x} \left[\frac{2a}{(x^2 + a^2)^{1/2}} \right]$$

When the length $2a$ of the conductor is very great in comparison to its distance x from point P , we consider it infinitely long. That is when a is much larger than x ,

$$(x^2 + a^2)^{1/2} = a$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

In a physical situation, we have axial symmetry about the y -axis. Thus, at all points in a circle of radius r , around the conductor, the magnitude of B is $B = \frac{\mu_0 I}{2\pi r}$

Equation (1) defines the magnitude of the magnetic field of flux density B in a long straight current carrying conductor.