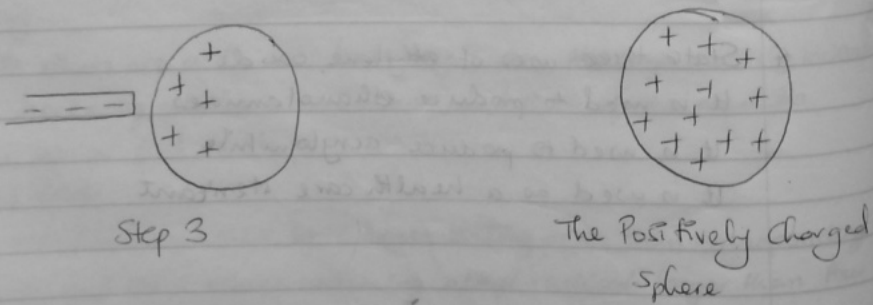
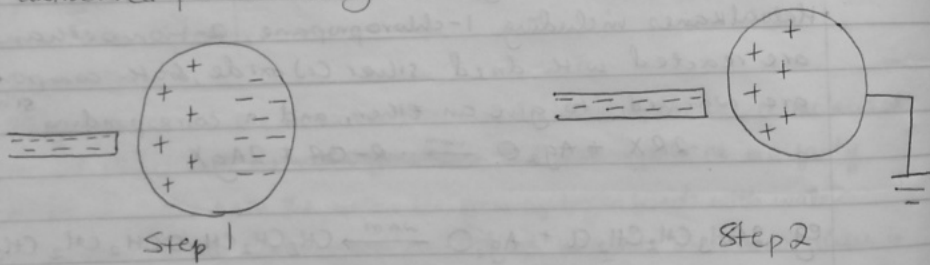


PRODUCTION OF CHARGES BY INDUCTION

This is the process by which objects obtain charges without contact. If a negatively charged rod is brought near a neutral insulated conducting sphere, the repulsive force between the electrons in the rod and those in the sphere causes a redistribution of charges on the sphere. The electrons on the side closest to the rod move away, to the side farthest from the rod. The result is that the side closest to the negatively charged rubber rod is dominated by positive charges. A grounded conducting wire is then connected to the sphere and most of its electrons move into the earth. The wire is removed, leaving the sphere with an excess of positive charges. Lastly, the negatively charged rubber rod is removed leaving the sphere with uniformly distributed positive charges.



1b Let the two charges be $= q_1$ and q_2
Sum of the charges $(q_1 + q_2) = 5.0 \times 10^{-5} \text{ C}$
Repelling force $(F) = 1.0 \text{ N}$
Distance $(r) = 2.0 \text{ m}$; $r^2 = 4.0 \text{ m}$

Recall: $F = \frac{kq_1q_2}{r^2}$

$$1.0 \text{ N} = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times q_1 q_2}{4.0 \text{ m}}$$

$$4.0 \text{ Nm} = 9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times q_1 q_2$$

$$q_1 q_2 = \frac{4.0 \text{ Nm}}{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2}} = 4.44 \times 10^{-10} \text{ C}^2$$

Recall =

$$x^2 - (\text{sum of roots})x + (\text{product of roots}) = 0$$

where; product of roots $= q_1 q_2$; sum of roots $= q_1 + q_2 = 5.0 \times 10^{-5} \text{ C}$

$$x^2 - (5.0 \times 10^{-5} \text{ C})x + (4.44 \times 10^{-10} \text{ C}^2) = 0$$

$$x^2 - 3.887 \times 10^{-5} \text{ C}x + 4.44 \times 10^{-10} \text{ C}^2 = 0$$

$$x(x - 3.887 \times 10^{-5} \text{ C}) + 1.113 \times 10^{-5} \text{ C}(x + 3.989 \times 10^{-5} \text{ C}) = 0$$

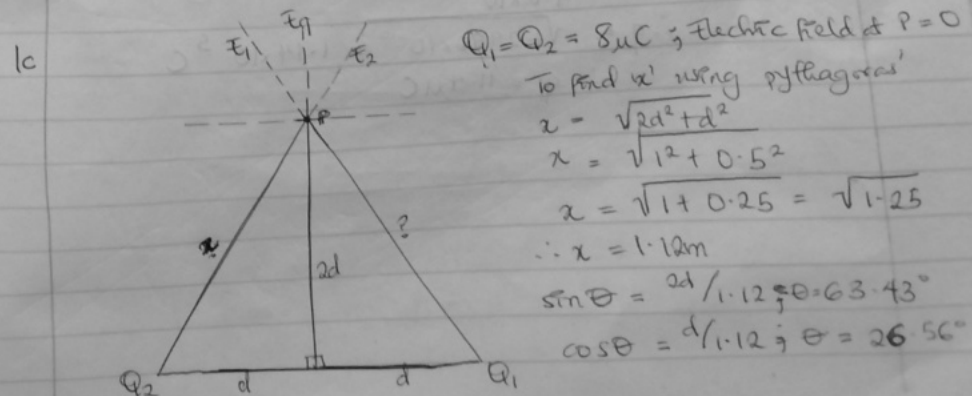
But $3.887 \times 10^{-5} \text{ C}$ and $3.989 \times 10^{-5} \text{ C}$ are approx. equal

\therefore Using $3.887 \times 10^{-5} \text{ C}$

The roots are: $3.89 \times 10^{-5} \text{ C}$ and $1.11 \times 10^{-5} \text{ C}$

where the roots of the equation is the charges.

\therefore The charges are $+3.89 \times 10^{-5} \text{ C}$ and $+1.11 \times 10^{-5} \text{ C}$



$$E = \frac{kq}{r^2}$$

$$Q_1 = Q_2 \text{ Note: } E_1 = E_2$$

$$E_1 = E_2 = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 8 \times 10^{-6} \text{ C}}{1.12 \text{ m}^2} = 5.74 \times 10^4 \text{ NC}^{-1}$$

$$\therefore E_1 = E_2 = 5.74 \times 10^4 \text{ NC}^{-1}$$

$$E_q = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times q}{1^2} = 9 \times 10^9 \text{ NC}^{-1} \therefore E_q = 9 \times 10^9 q \text{ NC}^{-1}$$

FORCES	Angles	X-component	Y-component
$5.74 \times 10^4 \text{ NC}^{-1}$	63.43°	$5.74 \times 10^4 \cos 63.43 = +2.57 \times 10^4$	$5.74 \times 10^4 \sin 63.43 = 5.13 \times 10^4$
$5.74 \times 10^4 \text{ NC}^{-1}$	63.43°	$5.74 \times 10^4 \cos 63.43 = -2.57 \times 10^4$	$5.74 \times 10^4 \sin 63.43 = 5.13 \times 10^4$
$9 \times 10^9 q \text{ NC}^{-1}$	90°	$9 \times 10^9 q \cos 90^\circ = 0$	$9 \times 10^9 q \sin 90^\circ = 9.0 \times 10^9 q$
		$\Sigma x = 0 \text{ NC}$	$\Sigma y = 1.026 \times 10^5 \text{ NC}^{-1} + 9.0 \times 10^9 q$

$$E_q = \sqrt{\Sigma x^2 + \Sigma y^2} = \sqrt{(0)^2 + [(1.026 \times 10^5)^2 + (9.0 \times 10^9 q)^2]}$$

$$= \sqrt{1.053 \times 10^{10} + (9.0 \times 10^9 q)^2}$$

$$\text{But } E_q = 0$$

$$\therefore 0 = \sqrt{1.053 \times 10^{10} + (9.0 \times 10^9 q)^2}$$

$$0 = 1.053 \times 10^{10} + (9.0 \times 10^9 q)^2$$

$$(9.0 \times 10^9 q)^2 = -1.053 \times 10^{10}$$

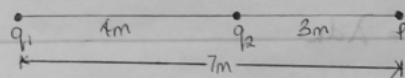
$$\therefore q^2 = \frac{-1.053 \times 10^{10}}{9.0 \times 10^9} = -1.2996 \times 10^{-10}$$

$$\therefore q = \sqrt{-1.2996 \times 10^{-10}} = 1.14 \times 10^{-5} \text{ C}$$

$$\therefore q = 11.4 \mu\text{C}$$

2a) Electric field is the region of space in which an electric charge will experience an electric force while electric field intensity also known as electric field strength is defined as the force per unit charge; it is the magnitude of electric field.

$$\text{bi } q_1 = 8 \text{ nC } \quad q_2 = 12 \text{ nC}$$

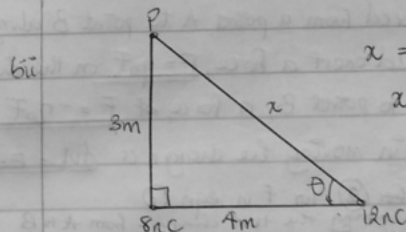


$$E_1 = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 8 \times 10^{-9} \text{ C}}{7^2} = 1.469 \text{ NC}^{-1}$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 12 \times 10^{-9} \text{ C}}{3^2} = 12 \text{ NC}^{-1}$$

$$E_{\text{net}} = E_1 + E_2 = 1.469 \text{ NC}^{-1} + 12 \text{ NC}^{-1} = 13.469 \text{ NC}^{-1}$$

$$\therefore E_{\text{net}} = 13.5 \text{ NC}^{-1}$$



$$x = \sqrt{3^2 + 4^2}$$

$$x = \sqrt{9 + 16} = \sqrt{25} \text{ m}$$

$$\therefore x = 5 \text{ m}$$

$$\theta = \sin^{-1}(3/5) = 36.9^\circ$$

$$E_1 = \frac{kq_1}{r^2} = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 8 \times 10^{-9} \text{ C}}{3^2} = 8 \text{ NC}^{-1}$$

$$E_2 = \frac{kq_2}{r^2} = \frac{9 \times 10^9 \text{ Nm}^2 \text{ C}^{-2} \times 12 \times 10^{-9} \text{ C}}{5^2} = 4.32 \text{ NC}^{-1}$$

Vector	Angle	X-Component	Y-component
8 NC^{-1}	90°	$8 \text{ NC}^{-1} \cos 90 = 0 \text{ NC}^{-1}$	$8 \sin 90 = 8 \text{ NC}^{-1}$
4.32 NC^{-1}	36.9°	$4.32 \cos 36.9 = 3.45 \text{ NC}^{-1}$	$4.32 \sin 36.9 = 2.60 \text{ NC}^{-1}$
		$\Sigma x = 3.45 \text{ NC}^{-1}$	$\Sigma y = 10.60 \text{ NC}^{-1}$

$$\Sigma_{\text{net}} = \sqrt{\Sigma F_x^2 + \Sigma F_y^2}$$

$$\Sigma_{\text{net}} = \sqrt{3.45^2 + 10.60^2} = \sqrt{124.2625}$$

$$\Sigma_{\text{net}} = 11.147 \text{ NC}^{-1} \approx 11.5 \text{ NC}^{-1}$$

3a Volume Charge Density

$$\rho = \frac{dQ}{dV} \rightarrow dQ = \rho dV$$

Surface Charge Density

$$\sigma = \frac{dQ}{dA} \rightarrow dQ = \sigma dA$$

Linear Charge Density

$$\lambda = \frac{dQ}{dl} \rightarrow dQ = \lambda dl$$

3b ELECTRIC POTENTIAL DIFFERENCE

The electric potential difference between two points in an electric field is the work done per unit charge against electrical forces when a charge is transported from one point to the other. It is a scalar quantity and measured in volts (V) or Joules per coulomb (J/C). In an electric field, supposed a test charge " q_0 " is moved from a point A to point B along an arbitrary path. The electric field would exert a force, $F = q_0 E$ on the charge. For " q_0 " to move from a point A to point B, a force of $F = -q_0 E$ has to be exerted on it. The work done in moving the charge is $dW = F \cdot dh$.

Recall: $F = -q_0 E$ --- (2) substituting for (2) for F in eqn (1)
 $dW = -q_0 E \cdot dh$ \therefore Total work done of moving the test charge from A to B

$$W_{CA \rightarrow B} = -q_0 \int_A^B E dh \rightarrow (4)$$

From the definition of Electrical Potential Difference

$$V_B - V_A = \frac{W_{CA \rightarrow B}}{q_0} \rightarrow (5)$$

Substitute equation (4) in (5)

$$V_B - V_A = \frac{-q_0 \int_A^B E dh}{q_0} \rightarrow (6)$$

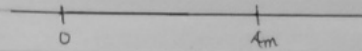
$$\Delta V = \frac{W_{CA \rightarrow B}}{q_0} = \frac{W_{CA \rightarrow B}}{q_0} = \frac{W_{CA \rightarrow B}}{q_0}$$

$$\therefore V_B - V_A = \frac{\Delta V}{q_0} = \frac{W_B - W_A}{q_0}$$

Diagram 1

$$Q_1 = 10 \mu C$$

$$Q_2 = -2 \mu C$$



$$V = \frac{1}{4\pi\epsilon_0} \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$\text{When } V = 0; 0 = 9 \times 10^9 \text{ Nm}^2 \text{C}^{-2} \left[\frac{10 \times 10^{-6}}{r_1} + \frac{-2 \times 10^{-6}}{r_2} \right]$$

$$\frac{0}{9 \times 10^9 \text{ Nm}^2 \text{C}^{-2}} = \left(\frac{10 \times 10^{-6}}{r_1} + \frac{-2 \times 10^{-6}}{r_2} \right) \Rightarrow \frac{10 \times 10^{-6}}{r_1} = \frac{2 \times 10^{-6}}{r_2}$$

$$2r_1 = 10r_2; r_1 = 5r_2$$

Recall the diagram above;

The position along the x-axis where $V = 0$ is 5m from $Q_1 = 10 \mu C$ and 1m from $Q_2 = -2 \mu C$

4 Magnetic Flux refers to the number of magnetic lines of force passing through a given closed surface which is the magnetic field. It is what generates the field around a magnetic material. Its S.I unit is Weber (Wb)

b) $m = 9.11 \times 10^{-31} \text{ kg}$, $r = 1.4 \times 10^{-7} \text{ m}$, $\theta = 90^\circ$, $B = 3.5 \times 10^{-4} \text{ T}$, $v = 3 \times 10^8 \text{ ms}^{-1}$

$$F = qvB \sin \theta = \frac{mv^2}{r}$$

$$q = \frac{mv^2}{vB \sin \theta} = \frac{9.11 \times 10^{-31} \text{ kg} \times 3 \times 10^8 \text{ ms}^{-1} \times 3 \times 10^8 \text{ ms}^{-1}}{3 \times 10^8 \text{ ms}^{-1} \times 3.5 \times 10^{-4} \text{ T} \times 1.4 \times 10^{-7} \text{ m} \times \sin 90}$$

$$q = \frac{2.733 \times 10^{-22} \text{ kgms}^{-2}}{4.9 \times 10^{-8}} = 5.578 \times 10^{-15} \text{ C}$$

$$\omega = \frac{qB}{m_e} = \frac{5.578 \times 10^{-15} \text{ C} \times 3.5 \times 10^{-4} \text{ T}}{9.11 \times 10^{-31} \text{ kg}} = 2.14 \times 10^{15} \text{ rad/s}$$

$$\therefore \omega = 2.14 \times 10^{15} \text{ rad/s}$$

d) Electrons exhibit uniform circular motion. The acceleration, thus, is centripetal

e) acceleration v^2/r [$F_B = qvB = mv^2/r$]. The angular speed is $\omega = v/r$.

Substituting adequately, the angular speed (also cyclotron frequency) is $2.14 \times 10^{15} \text{ rad/s}$. The electron circulates at this angular speed in the type of accelerator called a cyclotron.