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Computer Engineering

Reliability and Maintainability Coe 212

1. Solution

w_i = number of workers during i th month

D_i = demand for i th month

O_i = number made by over-time i th month

h_i, f_i = number of workers hired and fired respectively at the beginning of month i

x_i = number of carpets made during i th month

S_i = number of stored carpet at the end of i th month

All variables must be non negative

$$w_i, O_i, h_i, f_i, S_i \geq 0, i = 1, \dots, 12$$

Total carpets made per month

$$x_i = 20w_i + O_i$$

potential total number of workers at the start of each month $w_i = w_{i-1} + h_i - f_i$

number of carpets stored

$$S_i = S_{i-1} + x_i - d_i$$

Limits of overtime

$$O_i \leq b_{o,i}$$

To minimize the total cost which is the objective

Linear program

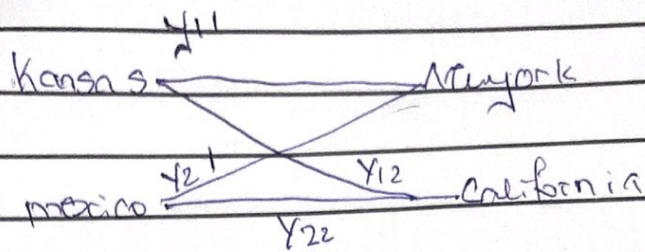
$$\min \sum_i 2000 w_i + 320 \sum_i h_i + 400 \sum_i A_i + 8 \sum_i s_i + 180 \sum_i f_i$$

Places	Cartoon
Kansas	15
Mexico	8

places	bags
New York	10
California	13

places	cost of shipping to New York
Kansas	2
Mexico	4

places	Cost of Shipping to California
Kansas	3
Mexico	1



Production Constraints

$$y_{11} + y_{12} \leq 15$$

$$y_{21} + y_{22} \leq 8$$

Consumers Constraints

$$y_{11} + y_{21} \leq 10$$

$$y_{12} + y_{22} \leq 13$$

Objective function

$$\begin{aligned} \text{Min } Z &= c_{11}y_{11} + c_{12}y_{12} + c_{21}y_{21} + c_{22}y_{22} \\ &= 2y_{11} + 3y_{12} + 4y_{21} + y_{22} \end{aligned}$$

A

Add slack

$$\text{Let } x_{11} = x_1$$

$$x_{12} = x_2$$

$$x_{21} = x_3$$

$$x_{22} = x_4$$

$$Z = 2x_1 + 3x_2 + 4x_3 + x_4$$

$$x_1 + x_2 + s_1 = 15$$

$$x_3 + x_4 + s_2 = 8$$

$$x_1 + x_3 + s_3 = 10$$

$$x_2 + x_4 + s_4 = 13$$

$$Z - 2x_1 - 3x_2 - 4x_3 - x_4 = 0$$

Iter	Basic	x_1	x_2	x_3	x_4	s_1	s_2	s_3	s_4	RHS	Ratio
0	Z	-2	-3	-4	-1	0	0	0	0	0	Ratio
	s_1	1	1	0	0	1	0	0	0	15	$15/1 = 15$
	s_2	0	0	1	1	0	1	0	0	8	$8/1 = 8$
	s_3	1	0	1	0	0	0	1	0	10	$10/1 = 10$
	s_4	0	1	0	1	0	0	0	1	13	$13/0 = \infty$

Most negative value from row is -4 hence we make

x_3 key column. Therefore row s_2 is our key row.

Iter	x_1	x_2	x_3	x_4	s_1	s_2	s_3	s_4	RHS	Ratio
1 (4th iter)	-2	-3	0	3	0	4	0	0	12	
	s_1	1	1	0	0	1	0	0	15	$15/1 = 15$
	s_2	0	0	1	1	0	1	0	8	$8/1 = 8$
$(s_3 - x_3)$	s_3	1	0	0	-1	0	-1	1	2	$2/0 = \infty$
	s_4	0	1	0	1	0	0	1	13	$13/1 = 13$

lowest Z value is -3

Iter	Basic Var	x_1	x_2	x_3	x_4	s_1	s_2	s_3	s_4	RHS	Ratio
202+20)	Z	-2	0	0	-6	0	4	0	3	71	
	s_1	1	0	0	-1	1	0	0	-1	2	$2/1=2$
	x_3	0	0	1	1	0	1	0	0	8	$8/0=0$
	s_2	1	0	0	-7	0	-1	1	0	2	$2/1=2$
	x_2	0	1	0	1	0	0	0	1	13	$13/0=0$

Since -2 is the lowest value

we pick x_1 key column

s_1 as key row

Iter	Basic Var	x_1	x_2	x_3	x_4	s_1	s_2	s_3	s_4	RHS	Ratio
302+20)	Z	0	0	0	4	2	4	0	1	15	
	x_1	1	0	0	-1	1	0	0	-1	2	
	x_3	0	0	1	1	0	1	0	0	8	
(s_2-x_1)	s_3	0	0	0	0	-1	-7	1	1	0	
	x_2	0	1	0	1	0	0	0	1	13	

Therefore - $x_1 = 2$

$x_2 = 13$

$x_3 = 8$

$x_4 = 0$

Hence Z_{min} (minimum cost) = 75