

15/02/2028
Ibomaye Sem John

Number 1

Objective function:

$$\text{Min } 2000 \sum_i z_i + 320 \sum_i h_i + 400 \sum_i f_i + 3 \sum_i s_i + 180 \sum_i y_i$$

Subject to:

$$x_i = 20z_i + y_i \quad ; \quad \text{total no. of Carpets made per month}$$

$$z_i = z_{i-1} + h_i - f_i \quad ; \quad \text{no. of workers at the beginning of each month}$$

$$s_i = s_{i-1} + x_i - d_i \quad ; \quad \text{no. of Carpets stored}$$

$$y_i \leq 6z_i \quad ; \quad \text{overtime limit}$$

$$z_0, y_i, x_i, h_i, f_i, s_i, s_0 \geq 0$$

when $i = 1, 2, 3, 4, \dots, 12$ and $z_0 = 30$

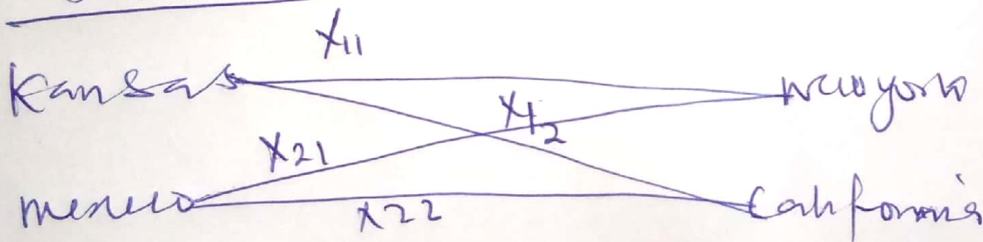
Number 2: Resolving the data into the tables below;

city	Cartons
Kansas	15
Mexico	8

city	Lags
Newyork	10
California	13

City	Cost to Shipping	
	Newyork	California
Kansas	2	3
Mexico	4	1

Solution:



Objective function:

$$\text{Min } Z = 2x_{11} + 3x_{12} + 4x_{21} + x_{22}$$

subject to:

$$\left. \begin{array}{l} x_{11} + x_{12} \leq 15 \\ x_{21} + x_{22} \leq 8 \end{array} \right\} \text{ production constraint}$$

$$\left. \begin{array}{l} x_{11} + x_{21} \leq 10 \\ x_{12} + x_{22} \leq 13 \end{array} \right\} \text{Consumption Constraint}$$

$$x_{11}, x_{12}, x_{21}, x_{22} \geq 0$$

The augmented matrix corresponding to this minimization problem is

$$\begin{array}{ccccc}
 x_{11} & x_{12} & x_{21} & x_{22} & r \\
 1 & 1 & 0 & 0 & 15 \\
 0 & 0 & 1 & 1 & 8 \\
 1 & 0 & 1 & 0 & 10 \\
 0 & 1 & 0 & 1 & 13 \\
 \hline
 2 & 3 & 4 & 1 & 0
 \end{array}$$

Taking the transpose of the matrix above

$$\begin{array}{cccc}
 y_{11} & y_{12} & y_{21} & y_{22} \\
 1 & 0 & 1 & 0 & 2 \\
 1 & 0 & 0 & 1 & 3 \\
 0 & 1 & 1 & 0 & 4 \\
 0 & 1 & 0 & 1 & 1 \\
 \hline
 15 & 8 & 10 & 13 & 0
 \end{array}$$

Thus the dual maximization problem is

$$Z = 15y_{11} + 8y_{12} + 10y_{21} + 13y_{22}$$

subject to:

$$y_{11} + y_{21} \leq 2$$

$$y_{11} + y_{22} \leq 3$$

$$y_{12} + y_{21} \leq 4$$

$$y_{12} + y_{22} \leq 1$$

Adding the slack variables to the constraints

$$y_{11} + y_{21} + s_1 \leq 2$$

$$y_{11} + y_{22} + s_2 \leq 3$$

$$y_{12} + y_{21} + s_3 \leq 4$$

$$y_{12} + y_{22} + s_4 \leq 1$$

	y_{11}	y_{12}	y_{21}	y_{22}	s_1	s_2	s_3	s_4	Constant
R_1	1	0	1	0	1	0	0	0	2
R_2	1	0	0	1	0	1	0	0	3
R_3	0	1	1	0	0	0	1	0	4
R_4	0	1	0	1	0	0	0	1	1
R_5	-15	-8	-10	-13	0	0	0	0	0

↑
most negative

$$2/1 = 2 \quad 1/0 = 0$$

$$3/1 = 3$$

$$4/0 = 0$$

$R_2 \rightarrow R_2 - R_1$
 $R_5 \rightarrow R_5 + 15R_1$
 $R_3 \rightarrow R_3$
 $R_4 \rightarrow R_4$

Applying this to the rows we have

	y_{11}	y_{12}	y_{21}	y_{22}	s_1	s_2	s_3	s_4		
R_1	1	0	1	0	1	0	0	0	1	2
R_2	0	0	-1	(1)	-1	1	0	0	1	1
R_3	0	1	1	0	0	0	1	0	1	4
R_4	0	1	0	1	0	0	0	1	-1	1
R_5	0	-8	5	-13	+15	0	0	0	1	+30

↑
most negative

- $2/0 = \text{undefined}$
- $1/1 = 1$
- $4/0 = \text{undefined}$
- $1/1 = 1$

- $R_4 \rightarrow R_4 - R_2$
- $R_5 \rightarrow R_5 + 13R_2$
- $R_1 \rightarrow R_1$ $R_3 \rightarrow R_3$
- $R_2 \rightarrow R_2$

	y_{11}	y_{12}	y_{21}	y_{22}	s_1	s_2	s_3	s_4		
R_1	1	0	1	0	1	0	0	0	1	2
R_2	0	0	-1	1	-1	1	0	0	1	1
R_3	0	(1)	1	0	0	0	1	0	1	4
R_4	0	1	1	0	1	-1	0	1	1	0
R_5	0	-8	-8	0	2	13	0	0	1	43

$$2/0 = \text{undefined}$$

$$1/0 = \text{undefined}$$

$$4/1 = 4$$

$$0/1 = 0$$

$$R_4 \rightarrow R_4 - R_3$$

$$R_5 \rightarrow R_5 + 8R_3$$

$$R_1 \rightarrow R_1$$

$$R_2 \rightarrow R_2$$

$$R_3 \rightarrow R_3$$

	y_{11}	y_{12}	y_{21}	y_{22}	s_1	s_2	s_3	s_4	
R_1	1	0	1	0	1	0	0	0	12
R_2	0	0	-1	1	-1	1	0	0	1
R_3	0	(1)	1	0	0	0	1	0	4
R_4	0	0	0	0	1	-1	-1	1	-4
R_5	0	0	0	0	2	13	8	0	75

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x_{11} x_{12} x_{21} x_{22}

Therefore :

$$x_{11} = 2 //$$

$$x_{12} = 13 //$$

$$x_{21} = 8 //$$

$$x_{22} = 0 //$$

$$\text{and lastly } \min Z = 75 //$$