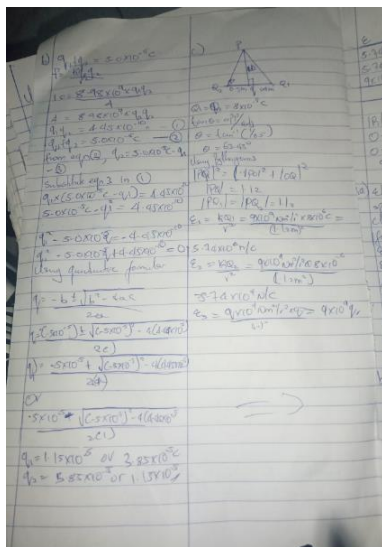
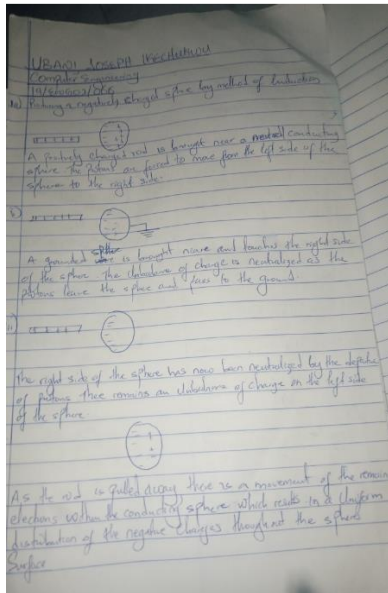


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Computer Engineering



$\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$
 $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \frac{x\hat{i} + y\hat{j} + z\hat{k}}{r}$
 $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^3} (x\hat{i} + y\hat{j} + z\hat{k})$
 $\vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^3} \vec{r}$

An electric field can be defined as the force per unit charge, mathematically its magnitude can be measured in N/C.

$E = \frac{F}{q}$
 $E = \frac{1.47 \times 10^6}{1} = 1.47 \times 10^6 \text{ N/C}$

b) $\vec{E}_1 = k \frac{q}{r^2} \hat{r}_1 = k \frac{q}{(4\pi\epsilon_0)^{-1} \frac{1}{\epsilon_0} r^2} \hat{r}_1 = \epsilon_0 k \frac{q}{r^2} \hat{r}_1$
 $\vec{E}_2 = k \frac{q}{r^2} \hat{r}_2 = \epsilon_0 k \frac{q}{r^2} \hat{r}_2$
 $\vec{E} = \vec{E}_1 + \vec{E}_2 = \epsilon_0 k \frac{q}{r^2} (\hat{r}_1 + \hat{r}_2)$

Magnetic field of a straight wire carrying current.

$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{\phi}$

a) Magnetic field at a point P on the surface of the wire. The magnetic field is perpendicular to the surface of the wire.

b) Magnetic field at a point P inside the wire.

$\vec{B} = \frac{\mu_0 I r}{2\pi R^2} \hat{\phi}$

c) Magnetic field at a point P outside the wire.

$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{\phi}$

d) Magnetic field at a point P on the axis of the wire.

$\vec{B} = 0$

Using vector calculus

$$\frac{\partial A_z}{\partial x} = \frac{\mu_0 I}{2\pi} \frac{1}{r^2} \frac{\partial r}{\partial x}$$

Special case becomes

$$B = \frac{\mu_0 I}{2\pi} \frac{1}{r^2} \frac{\partial r}{\partial x}$$

$$B = \frac{\mu_0 I}{2\pi} \frac{1}{r^2} \frac{x}{r}$$

when the length of the conductor is long and is comparable to the distance from point P, we consider it infinitely long. That is when $d \ll r$ or $r \gg d$

where $r = \sqrt{x^2 + d^2} \approx x$ as $d \rightarrow 0$

$$B = \frac{\mu_0 I}{2\pi r}$$

This defines the magnetic field of the wire B near a long straight current carrying conductor.