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Assignment Section A

a) Charging By Induction

Electrical charges can be obtained on an object without touching it, by a process called electrostatic induction. Consider a positively charged rubber rod brought near a neutral (uncharged) conducting ~~or positively charged rubber~~ rod sphere that is insulated so that there is no conducting path to ground. The repulsive force between the electrons in the rod and those in the sphere causes a redistribution of charges on the sphere so that some electrons move to the side of the sphere furthest away from the rod. The region of the sphere nearest the negatively charged rod has an excess of positive charge because of the migration of electrons away from this location. If a grounded conducting wire is then connected to the sphere, some of the electrons leave the sphere and travel to the earth. If the wire to ground is then removed, the conducting sphere is left with an excess of induced positive charge. Finally, when the rubber rod is removed from the vicinity of the sphere the induced positive charge remains on the ungrounded sphere and becomes uniformly distributed ~~and~~ over the surface of the sphere.

$$1b) \quad q_1 + q_2 = 5 \times 10^{-5} \text{ C}$$

$$F = 1 \text{ N}$$

$$r = 2$$

$$q_1 + q_2 = 5 \times 10^{-5} \text{ C}$$

$$F = \frac{k q_1 q_2}{r^2}$$

$$q_1 q_2 = F \left(\frac{r^2}{k} \right)$$

$$q_1 q_2 = \left(\frac{1}{9 \times 10^9} \right)$$

$$q_1 q_2 = 4 \times 10^{-10}$$

$$9 \times 10^9$$

$$q_1 q_2 = 4.44 \times 10^{-10} \text{ C}^2$$

$$q_1 + q_2 = 5 \times 10^{-5}$$

$$q_2 = 5 \times 10^{-5} - q_1$$

$$q_1 = (5 \times 10^{-5} - q_1) = 4.44 \times 10^{-10}$$

$$5 \times 10^{-5} q_1 - q_1^2 = 4.44 \times 10^{-10}$$

$$q_1 - (5 \times 10^{-5}) q_1 + 4.44 \times 10^{-10} = 0$$

Using Almighty formula

$$q_1, q_2 = \frac{(5 \times 10^{-5}) \pm \sqrt{(5 \times 10^{-5})^2 - 4.44 \times 10^{-10}}}{2}$$

$$= 1.6 \times 10^{-6} \text{ C}$$

$$q_1 = 3.84 \times 10^{-5} \text{ C}, q_2 = 1.16 \times 10^{-5} \text{ C}$$

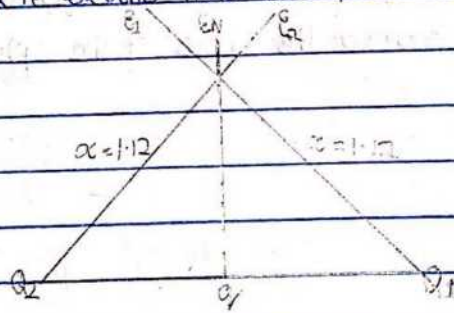
$$q_1 + q_2 = 5.0 \times 10^{-5}$$

$$3.84 \times 10^{-5} + 1.16 \times 10^{-5} = 5.0 \times 10^{-5} \text{ C}$$

10) $Q_1 = Q_2 = 8 \mu\text{C}$

$d = 0.5 \text{ m}$

determine Q if electric field at a point P is zero



$$E_1 = \frac{kq_1}{r_1^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2} = 57397.95918$$

$$E_2 = \frac{kq_2}{r_2^2} = \frac{9 \times 10^9 \times 8 \times 10^{-6}}{(1.12)^2} = 57397.95918$$

$$E_0 = \frac{kq}{r^2} = \frac{9 \times 10^9 \times q}{1} = 9 \times 10^9 q$$

Vector	Angle	X-component	Y-component
E_1	63.4	$E_1 \cos \theta$ -2570.045785	5132.262839
E_2	63.4	2570.045785	5132.262839
E_{net}	98	$E_1 \cos \theta \rightarrow 0$ $E_x = 0$	$9 \times 10^9 a$ $E_y = 10264.52568$

$$\text{magnitude} = \sqrt{(E_x)^2 + (E_y)^2}$$

$$E_x = \sqrt{(0)^2 + (10264.52568)^2}$$

Since $E = 0$

$$0 = 9 \times 10^9 a + 10264.52568 \quad \text{(making a subject of formula)}$$

$$a = \frac{-10264.52568}{9 \times 10^9} \quad \therefore q = 1.140502853 \times 10^{-6}$$

$$\therefore q = -11.4 \mu\text{C}$$

3a)

D Volume charge density, $\rho = \frac{dq}{dv} \rightarrow dq = \rho dv$

1) Surface charge density, $\sigma = \frac{dq}{dA} \rightarrow dq = \sigma dA$

1) Linear charge density, $\lambda = \frac{dq}{dL} \rightarrow dq = \lambda dL$

$$3b) \quad dW = F \cdot dl \quad \dots \dots \text{equ (1)}$$

$$F = -q_0 E \quad \dots \dots \text{equ (2)}$$

Substituting equation (2) in (1) yields

$$dW = -q_0 E \cdot dl \quad \dots \dots \text{equ (3)}$$

Total work done in moving the test charge from A to B is

$$W_{CA \rightarrow B)Aq} = -q_0 \int_A^B E \cdot dl \quad \dots \dots \text{(4)}$$

From the ~~same~~ definition of electric potential difference it follows that

$$V_B - V_A = \frac{W_{CA \rightarrow B)AS}}{q_0} \quad \dots \dots \text{(5)}$$

Putting equation 4 into 5 yields

$$V_B - V_A = \int_A^B E \cdot dl \quad \dots \dots \text{(6)}$$

Section B

4) A magnetic ~~field~~ flux is defined as the strength of the magnetic field which can be represented by the lines of the forces. It is represented by the symbol Φ . Mathematically given as $\Phi = B \cdot C \cdot A$

$$4b) \quad m = 9 \times 10^{-31} \text{ kg}$$

$$r = 1.4 \times 10^{-7} \text{ m}$$

$$B = 3.5 \times 10^{-1} \text{ weber/meter}^2$$

Cyclotron frequency = Angular Speed

$$\omega = \frac{v}{r} = \frac{\alpha B}{m}$$

$$\omega = \frac{\alpha B}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9 \times 10^{-31}}$$

$$\omega = 6.222222222 \dots 2222 \text{ T}^{-1}$$

tc: In the question we were given parameters such as

i) mass of Electron

ii) A radius of $1.4 \times 10^{-7} \text{ m}$

iii) magnetic field of 3.5×10^{-1} weber/metre square and you are asked to find the cyclotron frequency and it is the same as angular speed is given as

$$\omega = \frac{v}{r} = \frac{qB}{m}$$

$$\text{Substituting we have } \omega = \frac{v}{r} = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

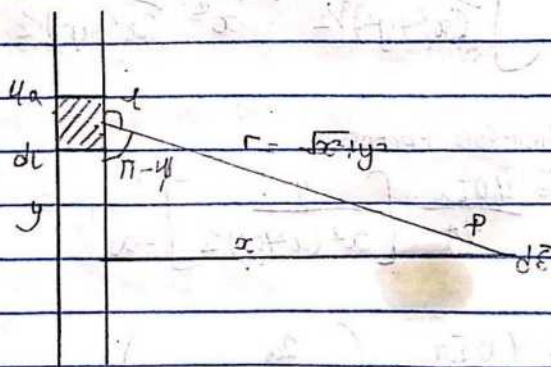
$$\frac{qB}{m} = 6222222222.2222 \text{ T}^{-1}$$

So since cyclotron frequency is equal to angular speed the cyclotron frequency is equal to $= 6222222222.2222 \text{ T}^{-1}$, here a unit ω which is equal to the unit of frequency dimensionally.

5: The Biot - Savart law states that the magnetic field is directly proportional to the ~~product~~ permeability of free space (μ_0), the current (I), the change in length, the radius and inversely proportional to the square of radius (r^2). It can be represented mathematically by ~~$\vec{dB} = \frac{\mu_0 I dx}{4\pi r^2}$~~

$$dB = \frac{\mu_0 I dx}{4\pi r^2}$$

5b)



Applying the Biot-Savart law, we find the magnitude of the field \vec{dB}

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dx \sin \theta}{r^2}$$

$$\sin(\pi - \theta) = \sin \theta$$

$$\therefore B = \frac{40I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{r^2}$$

from the diagram, $r^2 = x^2 + y^2$ (Pythagoras theorem)

$$B = \frac{40I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{x^2 + y^2} \quad \text{--- (1)}$$

$$\text{But } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- (2)}$$

Substituting equation 2 into 1, we have

$$B = \frac{40I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{40I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

Recall $dl = dy$

$$B = \frac{40I}{4\pi} \int_{-a}^a \frac{x}{(x^2 + y^2)^{3/2}} dy$$

$$B = \frac{40Ix}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- (3)}$$

using Special Integrals :-

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

Equation 3 therefore becomes -

$$B = \frac{40Ix}{4\pi} \left[\frac{y}{x^2 (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{40Ix}{4\pi} \left(\frac{2a}{x^2 (x^2 + a^2)^{1/2}} \right)$$

$$B = \frac{40I}{4\pi x} \left(\frac{2a}{x^2 + a^2)^{1/2}} \right)$$

When the length $2a$ of the conductor is very great in comparison to its distance x from point P, we consider it infinitely long. That is when a is much larger than x .

$$(x^2 + a^2)^{1/2} \approx a, \text{ as } a \rightarrow \infty$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

In a physical situation, we have axial symmetry about the y -axis, Thus and all points in a circle of radius r , around the conductor. The magnitude of B is:

$$B = \frac{\mu_0 I}{2\pi r} \quad \text{--- (ii)}$$

Equation (ii) defines the magnitude of the magnetic field of flux density B near a long straight current conductor.