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181SC1031016  
COMPUTER ENGINEERING  
ENG 252

$$\frac{dy}{dt} = ky$$

$$dy = kdt$$

$$\int \frac{dy}{y} = \int kdt$$

$$\ln y = kt + c$$

$$y = e^{kt+c}$$

$$y = e^{kt} \times e^c$$

$$y = e^{kt} \times y_0$$

$$= y = y_0 e^{kt} \text{ for case A}$$

The initial number of bacteria at  $t=0$  is 50

$$50 = y_0 e^{k(0)}$$

$$50 = y_0 \cdot 1$$

$$\therefore y_0 = 50$$

The number of bacteria at  $t=9$  hrs is  $50 \times 3 = y$

$$\therefore y = 50 e^{k(9)}$$

$$y = 150$$

$$150 = 50 e^{9k}$$

$$e^{9k} = 150/50 \Rightarrow e^{9k} = 3$$

$$9k = \ln 3$$

$$9k = 1.0986$$

$$k = \frac{1.0986}{9}$$

9

$$k = 0.122$$

$$y = 50 e^{0.122(9t)}$$

For case B

$$g = g_0 e^{kt}$$

The initial number at  $t=0$  is 150

$$\therefore 150 = g_0 e^{k(0)}$$

$$150 = g_0 \cdot 1$$

$$\therefore g_0 = 150$$

The number of bacteria at  $t=9$  hrs is  $150 \times 3 = 450$

$$\therefore 450 = 150 e^{k(9)}$$

$$e^{9k} = \frac{450}{150}$$

$$e^{9k} = 3$$

$$9k = \ln 3$$

$$9k = \ln 0.986$$

$$k = \frac{1.0986}{9}$$

$$k = 0.122$$

$$\therefore g = 150 e^{0.122(t)}$$

$\therefore$  For case B

$$g(t) = 150 e^{0.122(t)}$$

commandwindow

clearvars

clc

closeall

FOR CASE A

t := (0..15)

$$y(t) := 50 \cdot e^{0.122(t)}$$

t =

0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

y(t) =

50
56.488
63.817
72.098
81.453
92.022
103.962
117.451
132.691
149.908
169.359
191.334
216.161
244.209
275.896
311.694

FOR CASE B

$$g(t) := 150 \cdot e^{0.122(t)}$$

t =

0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

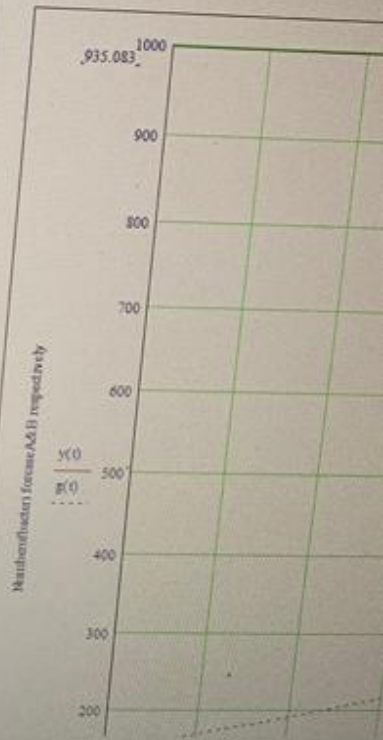
g(t) =

150
169.463
191.452
216.293
244.358
276.065
311.885
352.354
398.073
449.725
508.078
574.003
648.483
732.626
827.687
935.083

t := (0..15)

$$y(t) := 50 \cdot e^{0.122(t)}$$

$$g(t) := 150 \cdot e^{0.122(t)}$$



Press F1 for help.

$g(t) = 150 \cdot e^{0.122t}$

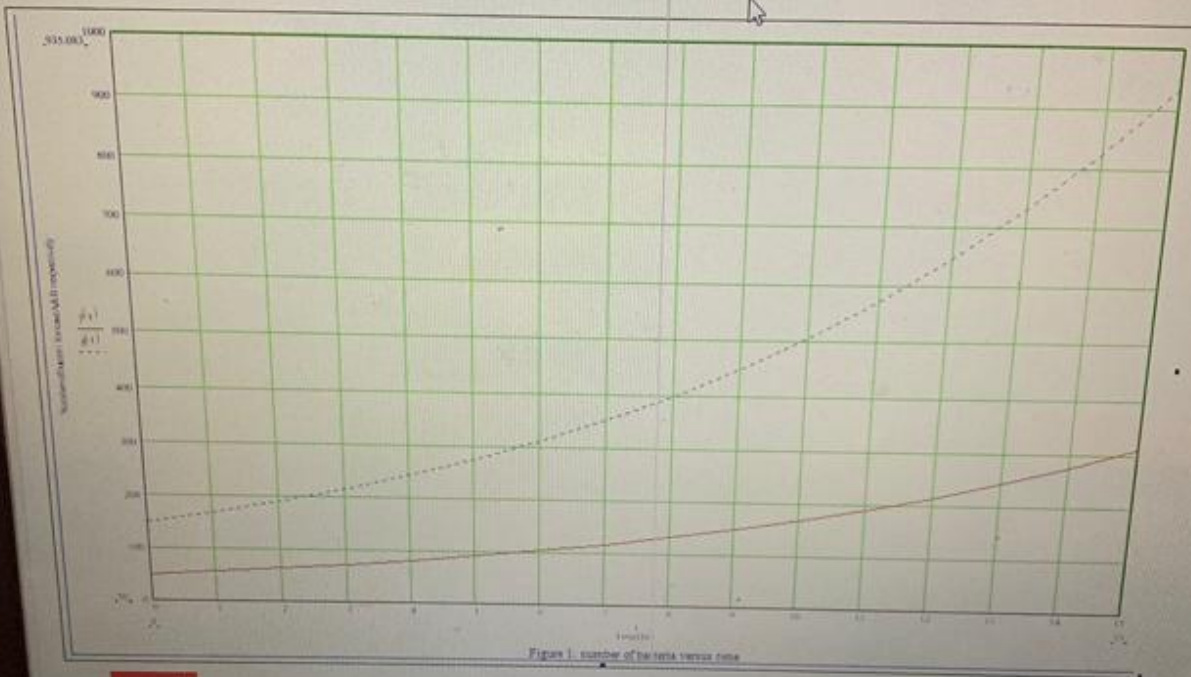


Figure 1. number of bacteria versus time

RED CASE I  
BLUE CASE II

Press F1 for help.

