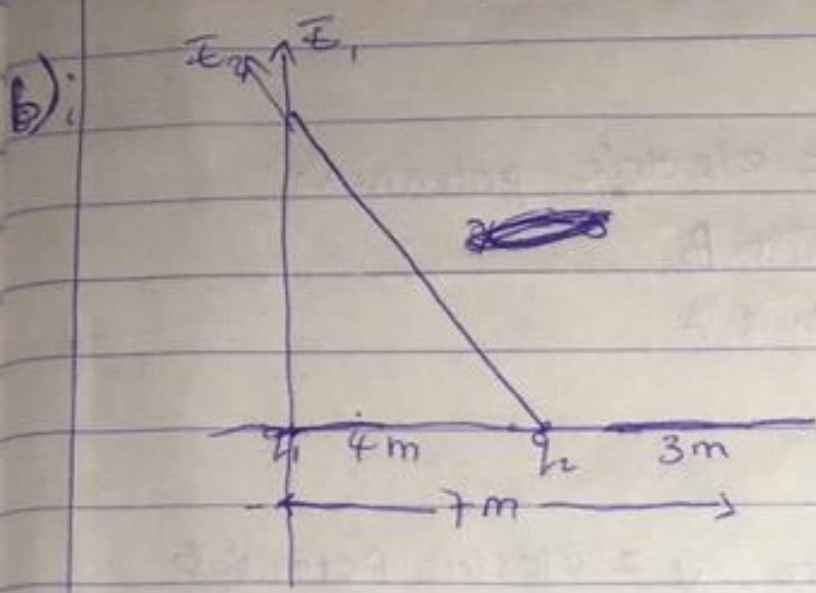


Section A.

29 An electric field is a region of space in which an electric charge will experience an electric force while electric field intensity is the force per unit charge ~~not~~ experienced by a charge in an electric field.

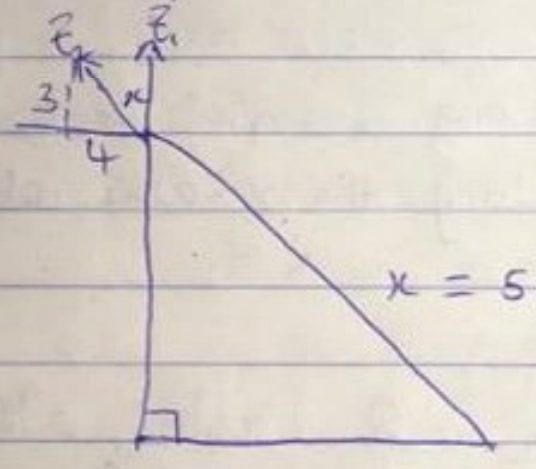


$$\vec{E}_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{4^2} = 1.469 \text{ N/C} \approx 1.5 \text{ N/C}$$

$$\vec{E}_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{3^2} = 12 \text{ N/C}$$

$$y = \vec{E}_{\text{net}} = \vec{E}_1 + \vec{E}_2 = (1.5 + 12) \text{ N/C} = 13.5$$

ii) \vec{E} at point A on the y axis at $y = 3\text{m}$ due to charge



$$c^2 = a^2 + b^2$$

$$c^2 = 4^2 + 3^2$$

$$c = 5$$

$$\vec{E}_1 = \frac{kQ_1}{r^2} = \frac{9 \times 10^9 \times 8 \times 10^{-9}}{3^2} = 8 \text{ N/C}$$

$$\vec{E}_2 = \frac{kQ_2}{r^2} = \frac{9 \times 10^9 \times 12 \times 10^{-9}}{5^2} = 4.32 \text{ N/C}$$

Vector	angle	x - comp	y - comp
$\vec{E}_1 = 8 \text{ N/C}$	90°	0 N/C	8 N/C
$\vec{E}_2 = 4.32$	36.87°	-3.45 N/C	2.59 N/C
		$\vec{E}_{fx} = -3.45 \text{ N/C}$	$\vec{E}_{fy} = 10.59 \text{ N/C}$

$$\vec{E}_{\text{net}} = \sqrt{E_{fx}^2 + E_{fy}^2}$$

$$= 11.12 \text{ N/C}$$

i) Volume charge density $\rho = \frac{dQ}{dv} = dQ = \rho dv$

ii) Surface charge density $\sigma = \frac{dQ}{dA} = dQ = \sigma dA$

iii) Linear charge density $\lambda = \frac{dQ}{dL} = dQ = \lambda dL$

b) Electrical Potential difference

• due to single point charge

$$V_B - V_A = \frac{Q}{4\pi\epsilon_0} \left[\frac{1}{r_B} - \frac{1}{r_A} \right]$$

where Q = point charge v = electric potential
 r_B = distance of Q to point B
 r_A = distance of Q to point A

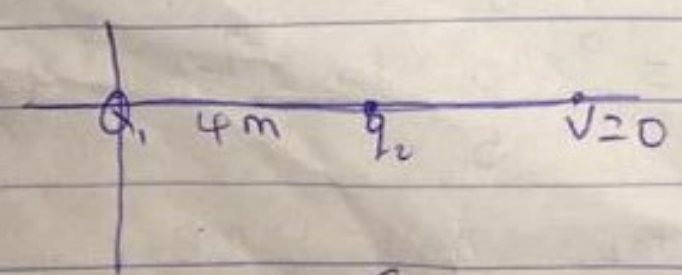
• due to several Point Charges

$$V_p = \frac{1}{4\pi\epsilon_0} \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right] \text{ where } v = \text{electric potential}$$

Q = point charge
 r = distance of Q .

C) Point charge, $Q_1 = 10\mu C$, $Q_2 = -2\mu C$ along x -axis $x=0$, $x=4m$ respectively. Find the position along the x -axis where $v=0$.

Solution



$$V_p = \frac{1}{4\pi\epsilon_0} \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right] \text{ recall } 1 = 9 \times 10^9$$

$$V_p = K \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$V_p = 9 \times 10^9 \times \left[\frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = 9 \times 10^9 \times \left[\frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} \right]$$

$$0 = \frac{10 \times 10^{-6}}{4+x} + \frac{-2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4+x} = \frac{2 \times 10^{-6}}{x}$$

$$10 \times 10^{-6} x = (4+x) (2 \times 10^{-6})$$

$$10 \times 10^{-6} x = 8 \times 10^{-6} + 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 10 \times 10^{-6} x - 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 8 \times 10^{-6} x$$

$$x = \frac{8 \times 10^{-6}}{8 \times 10^{-6}}$$

$$x = 1$$

∴ - position along the x-axis is 1m

where $v = 0$

$$v = k \left[\frac{Q_1}{r_1} + \frac{Q_2}{r_2} \right]$$

$$0 = \left[\frac{10 \times 10^{-6}}{4-x} + \frac{-2 \times 10^{-6}}{x} \right];$$

$$\frac{2 \times 10^{-6}}{x} = \frac{10 \times 10^{-6}}{4-x}$$

$$(4-x)(2 \times 10^{-6}) = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} - 2 \times 10^{-6} x = 10 \times 10^{-6} x$$

$$8 \times 10^{-6} = 10 \times 10^{-6} x + 2 \times 10^{-6} x$$

$$8 \times 10^{-6} = 12 \times 10^{-6} x$$

$$x = \frac{8 \times 10^{-6}}{12 \times 10^{-6}}$$

$$x = 0.67 \text{ m}$$

∴ position of $v = 0$ is 0.67m.

Section B

4a Magnetic flux is defined as the strength of the magnetic field which can be represented by line of forces. It is denoted as Φ .

$$\Phi = B \cdot dA$$

b $m_e = 9.11 \times 10^{-31} \text{ kg}$, $r = 1.4 \times 10^{-7} \text{ m}$; $B = 3.5 \times 10^{-1} \text{ W/m}^2$
 Cyclotron frequency = angular speed. $q = 1.6 \times 10^{-19}$

$$F_e = qVB = \frac{m_e v^2}{r}$$

$$m_e v = qBr$$

$$v = \frac{qBr}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1} \times 1.4 \times 10^{-7}}{9.11 \times 10^{-31}}$$

$$v = 8.61 \times 10^{-3} \text{ m/s}$$

$$\omega = \frac{v}{r} = \frac{qB}{m_e} = \frac{1.6 \times 10^{-19} \times 3.5 \times 10^{-1}}{9.11 \times 10^{-31}}$$

$$\omega = 6.14 \times 10^{10} \text{ s}^{-1}$$

c In 4b, we were given parameters; and we were asked to find the cyclotron frequency which is the same thing as angular speed is called cyclotron frequency because it is a frequency of an acceleration called cyclotron.

Recall $\omega =$ angular speed

$$\omega = \frac{qB}{m_e} \text{ Since cyclotron frequency} = \text{angular speed}$$

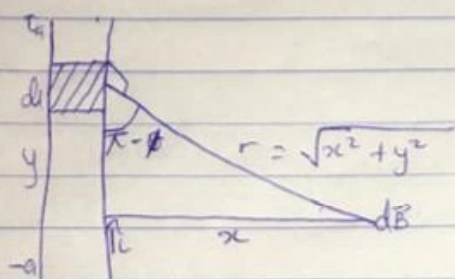
\neq which is the unit of a frequency dimensionally.

5a) Bio-savart law states that the magnetic field is directly proportional to the product permeability of free space (μ_0) the current (I), the change in length, the radius and is inversely proportional to square radius (r^2). Mathematically;

$$dB = \frac{\mu_0 I dl \sin \theta}{4\pi r^2}$$

where μ_0 (permeability of free space) = $4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$; r = radius
 dB = magnetic field, I = steady current, dl = length of wire unit is W/m^2 .

5) Magnetic field of a straight current carrying conductor



A section of a straight current carrying conductor.

Applying Bio-savart law, we find the magnitude of the field (dB) from the diagram,

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin \theta}{r^2}$$

$$\sin(\pi - \theta) = \sin \theta$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{r^2}$$

from the diagram $r^2 = x^2 + y^2$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin(\pi - \theta)}{x^2 + y^2} \quad \text{--- ①}$$

$$\text{But } \sin(\pi - \theta) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- ②}$$

Substitute ② into ①

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl}{(x^2 + y^2)^{3/2}}$$

$$dl = dy; \quad B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- (3)}$$

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi x} \left(\frac{2a}{(x^2 + a^2)^{1/2}} \right) \because (x^2 + a^2)^{1/2} = a = \infty$$

$$B = \frac{\mu_0 I}{2\pi a} = \frac{\mu_0 I}{2\pi r}$$