

$$r = \sqrt{y^2 + x^2}$$

$$B_z = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \sin\theta}{r^2}$$

$$B_z = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{dl \cos\theta}{(y^2 + x^2)^{3/2}}$$

$$B_z = \frac{\mu_0 I x}{4\pi} \int_{-a}^a \frac{dl}{(y^2 + x^2)^{3/2}}$$

$$B_z = \frac{\mu_0 I x}{4\pi} \left[\frac{dl}{(x^2 + a^2)^{1/2}} \right]_{-a}^a$$

$$B_z = \frac{\mu_0 I}{4\pi x} \left[\frac{2a}{(x^2 + a^2)^{1/2}} \right]$$

$$(x^2 + a^2)^{1/2} \approx a$$

$$a \gg x$$

$$B_z = \frac{\mu_0 I}{2\pi x} \frac{a}{(a^2)^{1/2}}$$

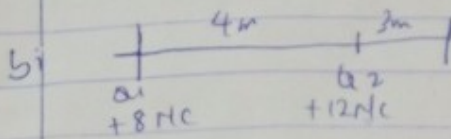
$$B_z = \frac{\mu_0 I}{2\pi x} \frac{x}{r}$$

$$B = \frac{\mu_0 I}{2\pi r}$$



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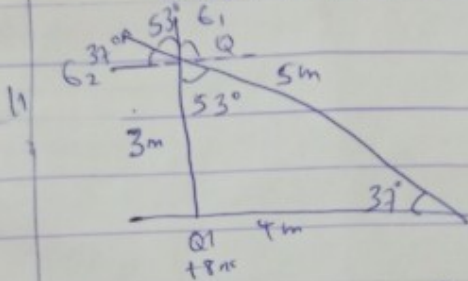
charge experienced by a charge in a electric field



$$G_1 = \frac{kQ_1}{r^2} = \frac{(9 \times 10^9)(8 \times 10^{-9})}{7^2} = 1.47 \text{ N/C}$$

$$G_2 = \frac{kQ_2}{r^2} = \frac{(9 \times 10^9)(12 \times 10^{-9})}{3^2} = 12 \text{ N/C}$$

$$G_{\text{net}} = 1.47 + 12 = 13.47 \text{ N/C}$$



$$G_{12} = \frac{kQ_1}{r^2} = \frac{(9 \times 10^9)(8 \times 10^{-9})}{5^2} = 2.88 \text{ N/C}$$

$$G_{22} = \frac{kQ_2}{r^2} = \frac{(9 \times 10^9)(12 \times 10^{-9})}{5^2} = 4.32 \text{ N/C}$$

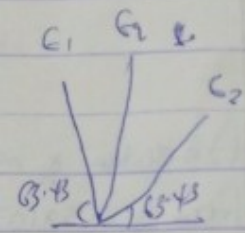
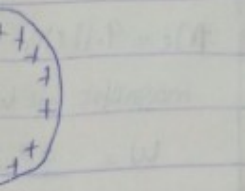
Vector	Angle	x-component	y-component
$G_1 = 2.88 \text{ N/C}$	90°	$2.88 \cos 90^\circ$ $= 0$	$2.88 \sin 90^\circ$ $= 2.88$
$G_2 = 4.32 \text{ N/C}$	37°	$4.32 \cos 37^\circ$ ≈ 3.45	$4.32 \sin 37^\circ$ ≈ 2.56
		$\Sigma F_x = 3.45 \text{ N/C}$	$\Sigma F_y = 5.44 \text{ N/C}$

Question 5

a) The Biot-Savart law is based on the following observations for the magnetic field $d\vec{B}$ at a point P associated with a length element dL of a wire carrying a steady current.

- 1) The vector $d\vec{B}$ is perpendicular to dL (which is the direction of the current) and to the unit vector \hat{r} directed from dL toward P.
- 2) The magnitude of $d\vec{B}$ is inversely proportional to r^2 , where r is the distance from dL to P.
- 3) The magnitude of $d\vec{B}$ is proportional to the current I and to the magnitude of the length element dL .

4) The magnitude of $d\vec{B}$ is proportional to $\sin \theta$, where θ is the angle between \hat{r} and dL . These observations are summarized in the mathematical expression known as Biot-Savart law.



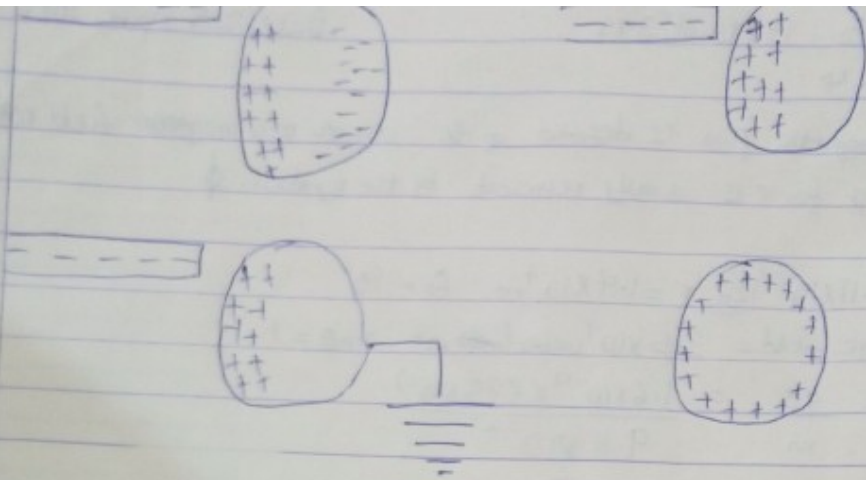
$d = 0.5$

$\theta = 2\alpha/d$
 $= 63.43^\circ$

$\frac{0.9 \times (8 \times 10^{-6})}{(1.5)^2}$

$\frac{7.2 \times 10^{-6}}{2.25} = 3.2 \times 10^{-6} \text{ C}$

The magnitude of \vec{E} is $E = \sqrt{E_x^2 + E_y^2} = \sqrt{(3.45)^2 + (5.44)^2} = 6.5 \text{ N/C}$



b) $q_1 + q_2 = 5 \times 10^{-5} \text{ C}$, $q_1 = 5 \times 10^{-5} - q_2$
 $F = \frac{k q_1 q_2}{r^2}$, $4 = \frac{9 \times 10^9 q_1 q_2}{2^2}$

$4 = 9 \times 10^9 \times (5 \times 10^{-5} - q_2) q_2$
 $4 = 4.5 \times 10^5 q_2 - 9 \times 10^9 q_2^2$
 $-9 \times 10^9 q_2^2 + 4.5 \times 10^5 q_2 - 4 = 0$

Using quadratic formula, $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$q_2 = \frac{-4.5 \times 10^5 \pm \sqrt{(4.5 \times 10^5)^2 - 4(-9 \times 10^9)(-4)}}{2(-9 \times 10^9)}$

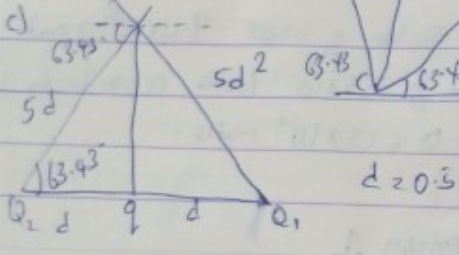
$q_2 = \frac{4.5 \times 10^5 \pm \sqrt{5.8 \times 10^{10}}}{-1.8 \times 10^9}$

$q_2 = \frac{-4.5 \times 10^5 \pm 2.41867 \times 10^5}{-1.8 \times 10^9}$

$q_2 = 1.56 \times 10^{-5} \text{ C or } 3.84 \times 10^{-5} \text{ C}$

$q_1 = 1.56 \times 10^{-5} \text{ C}$

$q_2 = 3.84 \times 10^{-5} \text{ C}$

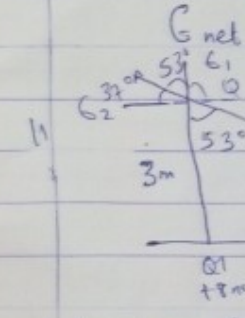


$\sqrt{5d^2} = d \sqrt{5}$, $\tan \theta = \frac{2d/d}{d/2}$
 $\tan^{-1}(2) = 63.43^\circ$

$G_1 = \frac{k q_1}{r_1^2} = \frac{9 \times 10^9 \times (8 \times 10^{-5})}{(\frac{d\sqrt{5}}{2})^2}$
 $= \frac{9 \times 10^9 \times 8 \times 10^{-5}}{(\frac{\sqrt{5}}{2})^2} = 57600 \text{ N/C}$

Question 2
 a) An electric field experience on a charge experiences

b) $G_1 = \frac{k q_1}{r^2}$
 $G_2 = \frac{k q_2}{r^2}$



$G_{12} = \frac{k q_1}{r^2}$
 $G_2 = \frac{k q_2}{r^2}$

Vector	Angle
$G_1 = 9 \text{ N/C}$	90°
$G_2 = 4.32 \text{ N/C}$	37°

The resultant $E = \sqrt{E_x^2 + E_y^2}$
 $= \sqrt{124.263}$



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Question 4

a) The magnetic flux is defined as the strength of a magnetic field represented by lines of force is usually represented by the symbol Φ

b) $m_e = 9.11 \times 10^{-31} \text{ kg}$, $r = 1.4 \times 10^{-7} \text{ m}$, $\theta = 90^\circ$
 magnetic field = $3.5 \times 10^{-1} \text{ weber/meter}^2$, $\sin\theta = 1$

$$w = \frac{qB}{m} = \frac{1.6 \times 10^{-19} \times (3.5 \times 10^{-1})}{9.11 \times 10^{-31}}$$

$$w = 6.115 \times 10^{10} \text{ rad/s}$$

c) An electron of mass $9.11 \times 10^{-31} \text{ kg}$ and charge $1.6 \times 10^{-19} \text{ C}$ in a motion in a magnetic field of $3.5 \times 10^{-1} \text{ Tesla}$ perpendicular with the field will have an angular frequency of $6.15 \times 10^{10} \text{ rad/s}$.

Question 1

Consider a negatively charged rubber rod brought near a neutral (uncharged) conducting sphere that is in no conducting path to ground as shown below. The repulsive force between the electrons in the rod and those in the sphere causes a redistribution of charges on the sphere so that some electrons move to the side of the sphere nearest the ~~negatively charged rod~~ ^{farthest away from the rod}. The region of the sphere nearest the negatively charged rod has an excess of positive charge because of the migration of electrons from this location. If a grounded conducting wire is then connected to the sphere, some of the electrons leave the sphere and travel to the earth. If the wire as to ground is then removed, the conducting sphere is left with an excess of induced positive charge. Finally, when the rubber rod is removed from the vicinity of the sphere the induced positive charge remains on the undergrounded sphere and becomes uniformly distributed over the surface of the sphere.

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