

The Danielle

Dentistry

College of Medicine and Health Sciences

100 Level

19/MT1509/009.

Physics 102 assignment.

Section 18

(2) Electric field

(4) Magnetic flux.

The magnetic flux is defined as the strength of magnetic field represented by lines of force. It is usually represented by the symbol ϕ

(b)

(5) The Biot - Savart law

\vec{dB} at a point P associated with a length element \vec{dl} of a wire carrying a steady current I

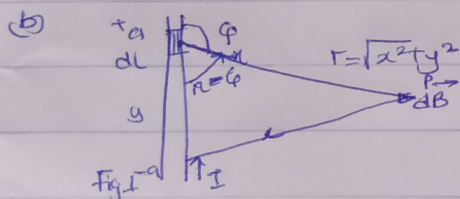


Fig 1: A section of a straight current carrying conductor.

Applying the biot - savart law, we find magnitude of the field dB

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \sin \phi}{r^2}$$

$$\sin(\pi - \phi) = \sin \theta$$

$$\therefore B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \sin(\pi - \phi)}{r^2}$$

∴ from the diagram, $r^2 = x^2 + y^2$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a \frac{dl \sin(\pi - \phi)}{x^2 + y^2} \quad \text{--- (x)}$$

But $\sin(\pi - \phi) = \frac{x}{\sqrt{x^2 + y^2}} = \frac{x}{(x^2 + y^2)^{1/2}} \quad \text{--- (xx)}$

substituting (xx) into (x)

$$B = \frac{\mu_0 I}{4\pi} \int_a^a dl \frac{x}{(x^2 + y^2)(x^2 + y^2)^{1/2}}$$

$$B = \frac{\mu_0 I}{4\pi} \int_a^a dl \frac{x}{(x^2 + y^2)^{3/2}}$$

recall $dl = dy$

$$B = \frac{\mu_0 I}{4\pi} \int_{-a}^a \frac{1}{(x^2 + y^2)^{3/2}} dy \quad \text{--- (xxx)}$$

using special integrals

$$\int \frac{dy}{(x^2 + y^2)^{3/2}} = \frac{1}{x^2} \frac{y}{(x^2 + y^2)^{1/2}}$$

Equation (xxx) becomes

$$B = \frac{\mu_0 I x}{4\pi} \left[\frac{y}{x^2 + (x^2 + y^2)^{1/2}} \right]_{-a}^a$$

$$B = \frac{\mu_0 I x}{4\pi} \left(\frac{2a}{x^2 + (x^2 + a^2)^{1/2}} \right)$$

When $B = \frac{\mu_0 I}{4\pi x} \left[\frac{2a}{(x^2 + a^2)^{1/2}} \right]$

when the length $2a$ of the conductor is very great in comparison to its distance x from point P , we consider it infinitely long. That is when a is much larger than x

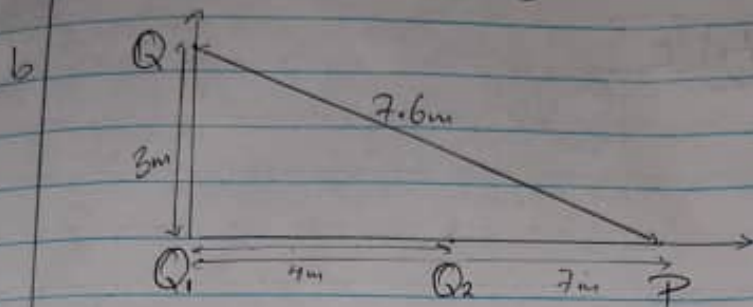
$$(x^2 + a^2)^{1/2} \approx a, \text{ as } a \gg x$$

$$\therefore B = \frac{\mu_0 I}{2\pi x}$$

In physical situation, we have axial symmetry about the y -axis. Thus at all points in a circle of radius r , around the conductor, the magnitude of B

$$B = \frac{\mu_0 I}{2\pi r}$$

2 Electric field is a region around a charge in which it exerts electrostatic force on another charges while electric field intensity is the strength of electric field at any point in space.



where $Q_1 = 8 \text{ nC}$
 $Q_2 = 12 \text{ nC}$

Recall $E = kq/r^2$

$$E_1 = \frac{[9 \times 10^9 \text{ Nm}^2/\text{C}^2] \cdot [8 \times 10^{-9} \text{ C}]}{[7.0 \text{ m}]^2}$$

$$E_1 = 1.47 \text{ N/C}$$

$$E_2 = \frac{[9 \times 10^9 \text{ Nm}^2/\text{C}^2] \cdot [12 \times 10^{-9} \text{ C}]}{[3.0 \text{ m}]^2}$$

$$E_2 = 12 \text{ N/C}$$

Vector	Angle	X Component	Y Component
$E_1 = 1.47 \text{ N/C}$	0°	$E_{1x} = 1.47 \cos 0^\circ$ $E_{1x} = 1.47 \text{ N/C}$	$E_{1y} = 1.47 \sin 0^\circ$ $E_{1y} = 0$
$E_2 = 12 \text{ N/C}$	0°	$E_{2x} = 12 \cos 0^\circ$ $= 12 \text{ N/C}$	$E_{2y} = 12 \sin 0^\circ$ $E_{2y} = 0$
		$\sum E_x = 13.47 \text{ N/C}$	$\sum E_y = 0$

3) Volume charge density, $\rho = q/v$
 where ρ is volume charge density
 q is electric charge
 v is volume

2) Surface charge density, $\sigma = q/A$
 where σ is surface charge density
 q is electric charge
 A is Area

1) Linear charge density, $\lambda = q/l$
 where λ is linear charge density
 q is electric charge
 l is length

b) Electric Potential Difference
 this can be defined as the difference in electric potential (v) between the final and the initial position when work is done upon a charge to change its potential energy in equilibrium

$$\Delta V = V_B - V_A = \frac{\text{Work}}{\text{Charge}} = \frac{\Delta PE}{\text{Charge}}$$

where $1V = 1 \frac{J}{C}$
 Unit of potential difference are Volts per Coulomb given the name Volt (V) after Alessandro Volta.

4

$$F_{ind} = \sqrt{F_x^2 + F_y^2}$$

$$= \sqrt{(13.47)^2 + (20)^2}$$

$$= \sqrt{181.4109}$$

$$F_{ind} = \underline{13.47 \text{ N}} / c$$