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Biomedical Engineering

18/ENG08/015

ENGN 214 (fluid mechanics) Assignment

1. Relative density = 0.8

Inlet diameter  $d_1 = 150\text{mm} = 150 \times 10^{-3}\text{m}$

Throat "  $d_2 = 75\text{mm} = 75 \times 10^{-3}\text{m}$

$$Q_{\text{od}} = 40\text{L/sec} = 0.04\text{m}^3/\text{sec}$$

$$C_d = 0.96$$

$$r_2 - r_1 = 150\text{mm} = 0.15\text{m}$$

$$A_1 = \frac{\pi d_1^2}{4} = \pi \times (150 \times 10^{-3})^2$$

$$= 0.0177\text{m}^2$$

$$A_2 = \frac{\pi d_2^2}{4} = \pi \times (75 \times 10^{-3})^2$$

$$= 4.419 \times 10^{-3}\text{m}^2$$

$$Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q \sqrt{A_1^2 - A_2^2} = C_d A_1 A_2 \sqrt{2gh}$$

$$\sqrt{2gh} = \frac{Q \sqrt{A_1^2 - A_2^2}}{C_d A_1 A_2}$$

$$2gh = \left( \frac{Q \sqrt{A_1^2 - A_2^2}}{C_d A_1 A_2} \right)^2$$

$$h = \frac{\left( \frac{Q \sqrt{A_1^2 - A_2^2}}{C_d A_1 A_2} \right)^2}{2g}$$

$$h = \left\{ \frac{0.04 \sqrt{(0.0177)^2 - (4.419 \times 10^{-3})^2}}{0.96 \times 0.0177 \times 4.419 \times 10^{-3}} \right\}^2 \frac{1}{2 \times 9.81}$$

$$h = \left( \frac{6.853799 \times 10^{-4}}{7.50876 \times 10^{-5}} \right) \frac{1}{2 \times 9.81}$$

$$\frac{(9.130)^2}{2 \times 9.81} = \frac{83.3561}{19.62}$$

$$= 4.24 \text{ m}$$

Then

$$h = \left( \frac{P_1}{\rho_1} + Z_1 \right) - \left( \frac{P_2}{\rho_2} + Z_2 \right)$$

$$h = \left( \frac{P_1}{\rho_1} - \frac{P_2}{\rho_2} + (Z_1 - Z_2) \right)$$

$$4.24 = \frac{P_1 - P_2}{\rho} + (Z_1 - Z_2)$$

$$\frac{P_1 - P_2}{\rho} = 4.24 + (Z_2 - Z_1)$$

$$\frac{P_1 - P_2}{\rho} = (4.24 + 0.15)$$

$$\frac{P_1 - P_2}{\rho} = 4.39$$

$$P_1 - P_2 = 4.39 \times \rho$$

$$P_1 - P_2 = 4.39 \times (0.8 \times 9.81 \times 1000)$$

$$P_1 - P_2 = 4.39 \times 7848$$

$$P_1 - P_2 = 34452.72 \text{ N/m}^2$$

2. Inlet  $d_1 D_1 = 300 \text{ mm} = 300 \times 10^{-3} \text{ m}$   $A_1 = 0.07069 \text{ m}^2$

Throat  $d_2 D_2 = 150 \text{ mm} = 150 \times 10^{-3} \text{ m}$   $A_2 = 0.0177 \text{ m}^2$

ShL of mercury = 13.6  $C_d = 0.98$

S.P of 0.6 = 0.9

Differential manometer = 250 mm = 0.25 m

$$h \cdot \left( \frac{S.L}{S.P} - 1 \right)$$

$$h = \left( \frac{13.6}{0.9} - 1 \right) y$$

$$h = (14.11) \times 0.25$$

$$h = 3.528 \text{ m}$$

$$Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.98 \times 0.07069 \times 0.0177 \times \sqrt{2 \times 9.81 \times 3.528}}{\sqrt{(0.07069^2 - 0.0177^2)}}$$

$$Q = \frac{0.0102}{0.0689}$$

$$Q = 0.149 \text{ m}^3/\text{s}$$

$$h = \left( \frac{P_1}{\omega} + Z_1 \right) - \left( \frac{P_2}{\omega} + Z_2 \right)$$

$$3.528 = \left( \frac{P_1}{\omega} - \frac{P_2}{\omega} \right) - (Z_1 - Z_2)$$

$$3.528 + (Z_2 - Z_1) = \left( \frac{P_1}{\omega} - \frac{P_2}{\omega} \right)$$

$$\text{Recall, } Z_2 - Z_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$(3.528 + 0.3) = \left( \frac{P_1 - P_2}{\omega} \right)$$

$$\frac{P_1 - P_2}{\omega} = 3.828$$

$$P_1 - P_2 = 3.828 \times \omega$$

$$\text{Recall, } \omega = 9.81 \times 0.9$$

$$P_1 - P_2 = 3.828 \times 9.81 \times 0.9$$

$$P_1 - P_2 = 33.79 \text{ kN/m}^2$$