

DARE BENEDICT OLUBUKOLA

MECHANICAL ENGINEERING

19/ENG06/016

SERIAL NO.; 111

MAT 104 ASSIGNMENT (Mrs. Funmilayo Saka)

Integrate the following with respect to their variable;

1. $3te^{2t}$

Solution

$$\int 3te^{2t} dt$$

$$u = 3t, \quad dv = e^{2t}$$

$$\frac{du}{dt} = 3, \quad v = \frac{e^{2t}}{2}$$

$$\therefore \int u dv = uv - \int v du$$

$$\begin{aligned} \int 3te^{2t} dt &= 3t \left(\frac{e^{2t}}{2} \right) - \int \frac{e^{2t}}{2} \cdot 3 dt \\ &= \frac{3te^{2t}}{2} - \int \frac{3e^{2t}}{2} dt \end{aligned}$$

$$\therefore \int 3te^{2t} dt = \left[\frac{3te^{2t}}{2} - \frac{3e^{2t}}{4} \right] + C$$

2. $x^2 \sin x$

Solution

$$\int x^2 \sin x dx$$

$$u = x^2, \quad dv = \sin x$$

$$\frac{du}{dx} = 2x, \quad v = -\cos x$$

$$\therefore \int u dv = uv - \int v du$$

$$\begin{aligned} \int x^2 \sin x \, dx &= x^2(-\cos x) - \int -\cos x \cdot 2x \, dx \\ &= -x^2 \cos x + \int 2x \cos x \, dx \end{aligned}$$

$$\left[\begin{aligned} u &= 2x, \quad dv = \cos x \\ \frac{du}{dx} &= 2, \quad v = \sin x \\ \Rightarrow & 2x \sin x - \int 2 \sin x \\ &= 2x \sin x + 2 \cos x \end{aligned} \right.$$

$$\Rightarrow \int x^2 \sin x \, dx = -x^2 \cos x + 2x \sin x + 2 \cos x + C$$

$$= 2x \sin x - x^2 \cos x + 2 \cos x + C$$

$$= 2x \sin x - \cos x (x^2 - 2) + C$$

$$= 2x \sin x - (x^2 - 2) \cos x + C$$

3. $\sin 7x \cos 2x$

Solution

$$\int \sin 7x \cos 2x \, dx = \frac{1}{2} \left[\sin(A+B) + \sin(A-B) \right]$$

$\begin{matrix} \vee & \vee \\ A & B \end{matrix}$

$$= \frac{1}{2} \left[\sin(7x+2x) + \sin(7x-2x) \right]$$

$$= \frac{1}{2} \left[\sin 9x + \sin 5x \right]$$

$$\int \sin 7x \cos 2x \, dx = \frac{1}{2} \int \left[\sin 9x + \sin 5x \right]$$

$$\int \sin 7x \cos 2x dx = \frac{1}{2} \left[\frac{-\cos 9x}{9} - \frac{\cos 5x}{5} \right] + C$$

$$= \frac{-\cos 9x}{18} - \frac{\cos 5x}{10} + C$$

4. $\frac{(2x - 3x^2)}{1-x}$

Solution

$$\int \frac{(2x - 3x^2)}{1-x} dx$$

multiply through by -1

$$\Rightarrow \int \frac{(3x^2 - 2x)}{(x-1)} dx$$

$$x-1 \overline{) \begin{array}{r} 3x+1 \\ 3x^2-2x \\ \hline 3x^2-3x \end{array}}$$

$$x - 0$$

$$x - 1$$

$$1$$

$$\therefore \int \frac{(3x^2 - 2x)}{(x-1)} dx = \int (3x+1) dx + \int \frac{1}{x-1} dx$$

$$= \frac{3x^2}{2} + x + \ln(x-1) + C$$