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18/ENG04/057

Electrical Engineering

ENG 214 - Fluid mechanics

1) Given Sp of gravity 0.8, $D_1 = 150\text{mm} = 0.15\text{m}$

$D_2 = 95\text{mm} = 0.095\text{m}$, $Z_2 - Z_1 = 150\text{mm} = 0.15\text{m}$

$Q = 4.4\text{lit/sec} = 0.04\text{m}^3/\text{s}$, $C_d = 0.96$

Pressure difference ($P_1 - P_2$)

$$A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767\text{m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.095^2}{4} = 0.00442\text{m}^2$$

$$Q = C_d \times A_1 A_2 \times \sqrt{2gh}$$
$$\sqrt{A_1^2 - A_2^2}$$

$$0.04 = 0.96 \times \frac{(0.01767 \times 0.00442)}{\sqrt{0.01767^2 - 0.00442^2}} \times \sqrt{2 \times 9.81 \times h}$$

$$0.04 = 0.96 \times 0.004565 \times 4.429 \sqrt{h}$$

$$h = \left(\frac{0.04}{0.96 \times 0.004565 \times 4.429} \right)^2$$

$$h = 4.247\text{m}$$

$$h = \left(\frac{P_1}{\rho} + Z_1 \right) - \left(\frac{P_2}{\rho} + Z_2 \right)$$

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) - (Z_1 - Z_2)$$

$$4.247 = \left(\frac{P_1 - P_2}{\rho} \right) - 0.15$$

$$4.247 + 0.15 = \left(\frac{P_1 - P_2}{\rho} \right)$$

$$(4.247 + 0.15) \rho = P_1 - P_2$$

$$P_1 - P_2 = (0.8 \times 1000 \times 9.81) (4.247 + 0.15)$$

$$P_1 - P_2 = 34.51\text{kN/m}^2$$

$$2) D_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$D_2 = 150 \text{ mm} = 0.15 \text{ m}$$

$$A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.07 \text{ m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.0177 \text{ m}^2$$

Specific gravity of heavy liquid (mercury) in U-tube manometer $S_{ac} = 13.6$

Specific gravity of liquid (oil) $s_p = 0.9$

$$y = 250 \text{ mm} = 0.25 \text{ m}$$

$$h = \left(\frac{P_1}{w} + z_1 \right) - \left(\frac{P_2}{w} + z_2 \right)$$

$$= y \left(\frac{S_{ac}}{s_p} - 1 \right) = 0.25 \left[\frac{13.6}{0.9} - 1 \right]$$

$$= 3.53 \text{ m}$$

2i) Discharge of oil Q

$$Q = \frac{c_d \times A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$Q = \frac{0.98 \times 0.07 \times 0.0177}{\sqrt{0.07^2 - 0.0177^2}} \times \sqrt{2 \times 9.81 \times 3.53}$$

$$Q = 0.149 \text{ m}^3/\text{s}$$

$$z_2 - z_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$\left(\frac{P_1}{w} - \frac{P_2}{w} \right) - 0.3 = 3.53$$

$$\frac{P_1 - P_2}{w} = 3.53 + 0.3$$

$$\frac{P_1 - P_2}{w} = 3.83$$

$$P_1 - P_2 = 3.83w$$

$$P_1 - P_2 = 3.83 \times (9.81 \times 0.9)$$

$$P_1 - P_2 = 33.8 \text{ kN/m}^2$$