

NAME: ERASI EBI FOME  
 DEPARTMENT: COMPUTER ENGINEERING  
 MATRIKNO: 19/ENGG020105  
 Course: MATH 104

1.  $3te^{2t}$

Let  $u = 3t$

$\frac{du}{dt} = 3$

$du = 3dt$

2.  $dy = e^{2t}$

$\int dy = \int 3e^{2t}$

$y = \frac{3e^{2t}}{2}$

Using  $uv - \int v du = \int u dv$

$= \frac{3t}{2} \left( \frac{e^{2t}}{2} \right) - \int \frac{e^{2t}}{2} \times 3 dt$

$= \frac{3t}{2} \left( \frac{e^{2t}}{2} \right) - \frac{1}{2} \int 3e^{2t} dt$

$= \frac{3t}{2} \left( \frac{e^{2t}}{2} \right) - \frac{1}{2} \times \frac{3e^{2t}}{2} + C$

$\left[ \frac{3te^{2t}}{2} - \frac{3e^{2t}}{4} \right] + C$

3.  $\int x^2 \sin x$

Let  $u = x^2$  &  $v = \sin x$

$\frac{du}{dx} = 2x$  &  $v = -\cos x$

Using  $uv - \int v du$

$(x^2)(-\cos x) - \int (-\cos x)(2x dx)$

$= -x^2 \cos x - \int -2x \cos x dx$

Let  $u = 2x$  &  $dv = \cos x$

$\frac{du}{dx} = 2$  &  $v = \sin x$

$$\begin{aligned}
 & (-2x)(\sin x) - \int (\sin x)(-2) dx \\
 & - 2x \sin x - (-2) \int \sin x dx \\
 & - 2x \sin x - (-2)(-\cos x) + C \\
 & - 2x \sin x - 2 \cos x + C \\
 & \int x^2 \sin x = -x^2 \cos x - 2x \sin x - 2 \cos x + C
 \end{aligned}$$

3.  $\int \sin 7x \cos 2x$

let  $A = 7x$ ,  $B = 2x$

$$\int \sin 7x \cos 2x = \frac{1}{2} [\sin(7x+2x) + \sin(7x-2x)]$$

$$\int \sin 7x \cos 2x = \frac{1}{2} [\sin 9x + \sin 5x]$$

$$= \frac{1}{2} \left[ \int \frac{\sin 9x}{9} + \frac{\sin 5x}{5} \right]$$

$$= \frac{-\cos 9x}{18} - \frac{\cos 5x}{10} + C$$

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$$\frac{2x-3x^2}{1-x}$$

$$\frac{2x-3x^2}{1-x} = \frac{2x-3x^2}{1-x}$$

$$\frac{2x-3x^2}{1-x} = \frac{2x-3x^2}{1-x}$$

$$\frac{-x^2+x^3}{-x^3}$$

$$\int (2x - x^2) dx + \int \frac{x^3}{1-x} dx$$
$$= \frac{2x^2}{2} - \frac{x^3}{3} + x^3 \ln(1-x) + C$$