

If $A = 3i + 4j - 6k$, $B = 5i - 11j + 2k$, $C = 7i - 7j + k$ Find

1) $A \cdot C + B \cdot C$

2) $(A - B) \cdot C$

3) $A \cdot (B \times C)$

Solu

1) $A \cdot C = (3i + 4j - 6k) \cdot (7i - 7j + k)$
 $A \cdot C = 3i + 7i + 4j - 7j - 6k + k$
 $= 10i - 3j - 5k$

$B \cdot C = (5i - 11j + 2k) \cdot (7i - 7j + k)$
 $B \cdot C = 5i + 7i - 11j - 7j + 2k + k$
 $= 12i - 4j + 3k$

$A \cdot C + B \cdot C$

$10i - 3j - 5k + 12i - 4j + 3k$
 $10i - 12i - 3j - 4j - 5k + 3k$
 $= -2i - 7j - 2k$

2) $(A - B) \cdot C$

$3i + 4j - 6k - 5i - 11j + 2k$
 $3i + 5i + 4j - 11j - 6k + 2k$
 $8i - 7j - 4k \cdot C$

$8i - 7j - 4k \times 7i - 7j + k$
 $8i + 7i - 7j - 7j - 4k + k$
 $15i - 14j - 3k$

$$3) A \cdot (B \times C)$$

$$(B \times C) = 12i + 4j + 13k$$

$$= 3i + 4j - 6k \times (12i + 4j + 13k)$$
$$3i - (2i - 4j) - 4j - 6k + 13k$$
$$-9i + j = 7k$$