

Uba Chikama Raphael

18/ENR-06/066

Mechanical Engineering

ENG 214

Question 1

A 300mm x 150mm Venturimeter is provided a vertical pipeline carrying oil of specific gravity 0.9 flow being upward. The difference in elevation of the throat section and entrance section of the venturimeter is 300mm. The differential U-tube mercury manometer shows gauge deflection of 250mm. Calculate, (a) The discharge of oil and (b) The pressure difference between the entrance section and the throat section. Take the C_d coefficient of meter as 0.98 and specific gravity of mercury as 13.6.

Solution to Question 1

Diameter of inlet (D₁) = 300mm = 300 × 10⁻³ = 0.3m

$$\text{Area } (A_1) = \frac{\pi d^2}{4} = \frac{\pi (0.3)^2}{4} = 0.070695 \text{ m}^2$$

$$\text{Area } (A_2) = \frac{\pi d^2}{4} = \frac{\pi (0.15)^2}{4} = 0.01767 \text{ m}^2$$

Diameter of throat (D₂) = 150mm = 150 × 10⁻³ = 0.15m.

Let section (1) represent inlet and section 2 represent throat

Then Z₂ - Z₁ = 300mm = 0.3m; Specific gr of oil = 0.9,

Specific gr of mercury = 13.6 Reading of diff Manometer x = 250mm = 0.25m

$$\text{Differential head } h \text{ is given by } h = \left(\frac{P_1}{\rho g} + Z_1 \right) - \left(\frac{P_2}{\rho g} + Z_2 \right)$$
$$= x \left[\frac{S_y}{S_o} - 1 \right] = 0.25$$

$$\left[\frac{13.6}{0.9} - 1 \right] = 3.5277 \text{ m of oil}$$

i The discharge Q of oil = C_d × A₁ × a₂ × √2gh

$$= \frac{C_d \times A_1 \times a_2}{\sqrt{a_1^2 - a_2^2}} \times \sqrt{2gh}$$

$$= \frac{0.98 \times 0.070695 \times 0.01767}{\sqrt{(0.070695)^2 - (0.01767)^2}} \times \sqrt{2 \times 9.81 \times 3.5277}$$

$$= \frac{0.224197037 \times 10^{-3} \times 8.39196}{0.0684511} = 0.14879 \text{ m}^3/\text{s}$$

$$= 148.79 \text{ litres}$$

11. Pressure difference between entrance and throat section

$$h = \left(\frac{P_1}{\rho g} + z_1 \right) - \left(\frac{P_2}{\rho g} + z_2 \right) =$$

$$3.5277 \quad \text{Recall } z_2 - z_1 = 0.3$$

$$\therefore \left(\frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) - 0.3 = 3.5277$$

$$\therefore \frac{P_1}{\rho g} - \frac{P_2}{\rho g} = 3.5277 + 0.3 = \underline{3.8277 \text{ m of oil}}$$

Question 2

A vertical Venturimeter carries a liquid of relative density 0.8 and has inlet and throat diameters of 150mm and 75mm respectively. The pressure connection at the throat is 50mm above that at the inlet. If the actual flow rate of flow is 40 litres/sec and the C.d = 0.96, calculate the pressure difference between inlet and throat in N/m^2

Solution of Question 2

$$\text{Specific gravity} = 0.8 \quad D_1 = 150\text{mm} = 0.15\text{m}$$

$$z_1 = 150\text{mm} = 0.15\text{m} \quad D_2 = 75\text{mm} = 0.075\text{m}$$

$$z_2 = 75\text{mm} = 0.075\text{m} \quad Q_{\text{act}} = 40 \text{ litres/sec} = 0.04 \text{ m}^3/\text{sec}$$

$$C_d = 0.96$$

$$\text{Pressure difference } (P_1 - P_2) A_1 = \frac{\pi d^2}{4} = \frac{\pi \times (0.15)^2}{4} = 0.01767 \text{ m}^2$$

$$A_2 = \frac{\pi d^2}{4} = \frac{\pi \times (0.075)^2}{4} = 0.00442 \text{ m}^2$$

$$Q.d = \frac{C_d \times A_1 \times A_2 \times \sqrt{2gh}}{A_1^2 - A_2^2}$$

$$0.04 = \frac{0.96 \times 0.01767 \times 0.00442 \times \sqrt{2 \times 9.81 \times h}}{(0.01767)^2 - (0.00442)^2}$$

$$h = \frac{0.04 \times 0.96 \times 0.004565 \times 4.4297^2}{0.004565 \times 4.4297^2}$$

$$h = 4.2747 \text{ m}$$

$$4.2747 = \left(\frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) + (z_1 - z_2) - \left(\frac{P_1 - P_2}{\rho g} \right) = 0.15$$

$$\begin{aligned} P_1 = P_2 &= \rho g (4.247 + 0.15) \\ (0.8 \times 1000 \times 9.81) (4.247 + 0.15) \text{ N/m}^2 \\ &= \underline{\underline{34.51 \text{ kN/m}^2}} \end{aligned}$$