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MECHANICAL ENGINEERING  
18/ENG06/021

(I) Diameter at Inlet  $D_1 = 300\text{mm} = 0.3\text{m}$   
Area of Inlet  $A_1 = \frac{\pi}{4} \times 0.3^2 = 0.07\text{m}^2$

Diameter at throat  $D_2 = 150\text{mm} = 0.15\text{m}$   
Area at throat  $A_2 = \frac{\pi}{4} \times 0.15^2 = 0.01767\text{m}^2$

$s_p$   
Specific gravity of heavy liquid (mercury) in u-tube  
manometer  $s_1 = 13.6$

Specific gravity of liquid (oil) flowing through pipe  $s_p = 0.9$

Reading of differential manometer,  $g = 250\text{mm} = 0.25\text{m}$

The differential 'h' is given by

$$h = \left( \frac{P_1}{\rho} + z_1 \right) - \left( \frac{P_2}{\rho} + z_2 \right)$$
$$= g \left[ \frac{s_w}{s_p} - 1 \right] = 0.25 \left[ \frac{13.6}{0.9} - 1 \right]$$
$$= 3.53\text{m of oil}$$

I. Discharge of oil Q:

Using the relation

$$Q = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$\therefore Q = 0.98 \times \frac{0.07 \times 0.01767}{\sqrt{0.07^2 - 0.01767^2}} \times \sqrt{2 \times 9.81 \times 3.53}$$
$$= \frac{0.00212}{0.0677} \times 8.32 = 0.1489\text{m}^3/\text{s}$$

(II) Pressure difference between entrance throat sections

$$\left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + (z_1 - z_2) = 3.53$$

If  $z_2 - z_1 = 0.3\text{m}$

$$\therefore \left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) - 0.3 = 3.53$$

2. Specific gravity = 0.8

$$D_1 = 50 \text{ mm} = 0.05 \text{ m}$$

$$D_2 = 75 \text{ mm} = 0.075 \text{ m}$$

$$Z_1 - Z_2 = 150 \text{ mm} = 0.15 \text{ m}$$

$$\rho = 800 \text{ kg/m}^3 = 0.8 \times 1000 \text{ kg/m}^3$$

$$A_1 = \frac{\pi d^2}{4} = \frac{\pi (0.05)^2}{4}$$

$$A_1 = 0.1767$$

$$A_2 = \frac{\pi d^2}{4} = \frac{\pi (0.075)^2}{4}$$

$$A_2 = 4.4178 \times 10^{-2}$$

$$Q_{out} = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$= 0.04 = 0.96 \times \frac{0.1767 \times 0.0442}{\sqrt{0.1767^2 - 0.0442^2}} \times \sqrt{2 \times 9.81 \times h}$$

$$\therefore h = \left( \frac{0.04}{0.96 \times 0.004565 \times 9.429} \right)^2 = 4.247 \text{ m}$$

$$h = \left[ \frac{P_1}{\omega} + z_1 \right] - \left[ \frac{P_2}{\omega} + z_2 \right]$$

$$4.247 = \left( \frac{P_1}{\omega} - \frac{P_2}{\omega} \right) + (z_1 - z_2)$$

$$= \left( \frac{P_1 - P_2}{\rho g} \right) - 0.15$$

$$\text{or } (P_1 - P_2) = \rho g (4.247 + 0.15)$$

$$= (800 \times 9.81) (4.247 + 0.15) \text{ N/m}^2$$

$$= 34.51 \text{ kN/m}^2$$