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Sp of gravity: 0.8

$D_1 = 0.15\text{m}$ $D_2 = 0.075\text{m}$ $Z_2 - Z_1 = 0.15\text{m}$ $Q = 0.04\text{m}^3/\text{s}$ $C_d = 0.96$

Pressure difference ($P_1 = P_2$)

$$A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767\text{m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.075^2}{4} = 0.00442\text{m}^2$$

$$Q = \frac{C_d \times A_1 A_2 \times \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$0.04 = \frac{0.96 \times 0.01767 \times 0.00442 \times \sqrt{2 \times 9.81 \times h}}{\sqrt{0.01767^2 - 0.00442^2}}$$

$$0.04 = \frac{0.96 \times 0.004565 \times 4.429 \sqrt{h}}{2}$$
$$h = \left(\frac{0.04}{0.96 \times 0.004565 \times 4.429} \right)^2 = 4.247\text{m}$$

$$h = \left(\frac{P_1}{\rho} + Z_1 \right) - \left(\frac{P_2}{\rho} + Z_2 \right)$$

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + (Z_1 - Z_2)$$

$$4.247 = \left(\frac{P_1 - P_2}{\rho} \right) - 0.15$$

$$4.247 + 0.15 = \frac{P_1 - P_2}{\rho}$$

$$(4.247 + 0.15) \rho = P_1 - P_2$$

$$P_1 - P_2 = (0.8 \times 1000 \times 9.81)(4.247 + 0.15)$$

$$P_1 - P_2 = 34.5\text{KN/m}^2$$

$$2) D_1 = 0.3 \text{ m}$$

$$\text{Area of inlet } A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.07 \text{ m}^2$$

$$\text{Diameter of throat } D_2 = 0.15 \text{ m}$$

$$\text{Area of throat } = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

$$S_{he} = 13.6 \quad (\text{of mercury})$$

$$S_p = 0.9 \quad (\text{of liquid})$$

$$y = 0.25 \text{ m}$$

The differential h is then given by:

$$h = \left(\frac{P_1}{\rho} + Z_1 \right) - \left(\frac{P_2}{\rho} + Z_2 \right)$$

$$= y \left(\frac{S_{he}}{S_p} - 1 \right) = 0.25 \left(\frac{13.6}{0.9} - 1 \right) = 3.53 \text{ m of Oil}$$

a) Discharge of oil (Q)

Applying the formula

$$Q = C_d \times A_1 A_2 \times \frac{\sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = 0.98 \times 0.07 \times 0.01767 \times \frac{\sqrt{2 \times 9.81 \times 3.53}}{\sqrt{0.07^2 - 0.01767^2}}$$

$$Q = 0.1489 \text{ m}^3/\text{s}$$

b) Pressure difference

$$h = \left(\frac{P_1}{\rho} + Z_1 \right) - \left(\frac{P_2}{\rho} + Z_2 \right) = 3.53$$

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) - (Z_1 - Z_2) = 3.53$$

$$Z_2 - Z_1 = 300 \text{ mm}$$

$$Z_2 - Z_1 = 0.3 \text{ m}$$

$$\left(\frac{P_1 - P_2}{\rho} \right) - 0.3 = 3.53$$

$$\left(\frac{P_1 - P_2}{\rho} \right) = 3.53 + 0.3$$

$$\left(\frac{P_1 - P_2}{w} \right) = 3.83$$

$$P_1 - P_2 = 3.83w$$

$$P_1 - P_2 = 3.82 \times 9.81 \times 0.9$$
$$= 33.8 \text{ kN/m}^2$$