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CIVIL ENGINEERING

FLUID MECHANICS (ENG 214)

1) Given Sp of gravity 0.8, D_1 = 150mm = 0.15m, D_2 = 75mm = 0.075m
$Z_2 - Z_1$ = 150mm = 0.15m, Q = 40 lit/sec = 0.04 m^3/s, cd = 0.96

Pressure Difference $(P_1 - P_2)$

$$A_1 = \frac{\pi D^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.017767 m^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.075^2}{4} = 0.00442 m^2$$

$$Q = \frac{C_d \times A_1 A_2 \times \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$0.04 = \frac{0.96 \times 0.01767 \times 0.00442 \times \sqrt{2 \times 9.81 \times h}}{\sqrt{0.017767^2 - 0.00442^2}}$$

$$0.04 = 0.96 \times 0.004565 \times 4.429\sqrt{h}$$

$$h = \left(\frac{0.04}{0.96 \times 0.004565 \times 4.429}\right)^2 = 4.247m.$$

$$h = \left(\frac{P_1}{w} + Z_1\right) - \left(\frac{P_2}{w} + Z_2\right)$$

$$h = \left(\frac{P_1}{w} - \frac{P_2}{w}\right) + \left(Z_1 + Z_2\right)$$

$$4.247 = \left(\frac{P_1 - P_2}{\rho g}\right) - 0.15$$

$$4.247 = \left(\frac{P_1 - P_2}{g}\right) - 0.15 \qquad 4.247 + 0.15 = \frac{P_1 - P_2}{g}$$

$$(4.247 + 0.15)\rho g = P_1 - P_2$$

$$P_1 - P_2 = (0.8 \times 1000 \times 9.81)(4.247 + 0.15)$$

$$P_1 - P_2 = 34.51 KN/m^2.$$

2) Diameter of inlet D_1 = 800mm = 0.3m

Area of inlet $A_1 = \frac{\pi \times D_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.07m^2$

Diameter of throat D_2 = 150mm = 0.15m

Area of of inlet $A_2 = \frac{\pi D_2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767m^2$

Specific gravity of heavy liquid (mercury) in U tube venometer

$S_h = 13.6$

Specific gravity of liquid (oil) flowing through pipe sp = 0.9

Reading of differential manometer, y = 250mm = 0.25m

The differential "h" is given by:

$$h = \left(\frac{P_1}{w} + Z_1\right) - \left(\frac{P_2}{w} + Z_2\right)$$

$$= y\left[\frac{S_h}{S_p} - 1\right] = 0.25\left[\frac{13.6}{0.9} - 1\right] = 3.53m \text{ of oil.}$$

A) Discharge of oil Q

using the relation

$$Q = \frac{C_d \times A_1 A_2 \times \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.98 \times 0.07 \times 0.01767 \times \sqrt{2 \times 9.81 \times 3.53}}{\sqrt{0.07^2 - 0.01767^2}}$$

$$Q = 0.1489 \; m^3/s$$

(B) Pressure difference between entrance and that first section $P_1 - P_2$, we all know that:

$$h = \left(P_1/w + Z_1\right) - \left(P_2/w + Z_2\right) = 3.53$$

$$h = \left(\frac{P_1}{w} - \frac{P_1}{w}\right) - (Z_1 - Z_2) = 3.53$$

$$Z_2 - Z_1 = 300mm = 0.3m$$

$$\left(\frac{P_1 - P_2}{w}\right) = 0.3 = 3.53$$

$$\frac{P_1 - P_2}{w} = 3.53 + 0.3$$

$$= 3.83$$

$$P_1 - P_2 = 3.83w$$

$$P_1 - P_2 = 3.82 \times 9.81 \times 0.9$$

$$= 33.8 \ KN/m^2.$$