

MECHATRONICS

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1) length of conical tube = 2m

$$V_1 = 5 \text{ m/s} \quad V_2 = 2 \text{ m/s}$$

Pressure head of smaller end = 2.5m

$$\text{Loss of head} = 0.35 \frac{(V_1 - V_2)^2}{2g}$$

$$\text{Loss of head} = \frac{0.35 (5 - 2)^2}{2 \times 9.81} = 0.160 \text{ m}$$

$$h_L = 0.160 \text{ m}$$

The pressure at larger end = P_2/w

Applying Bernoulli's eqn for conical tube

$$\frac{P_1}{w} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{w} + \frac{V_2^2}{2g} + z_2 + K_L$$

$$z_1 = 2 \text{ m} \quad z_2 = 0 \text{ m}$$

$$2.5 + \frac{5^2}{(9.81)^2} + 2 = \frac{P_2}{w} + \frac{2^2}{(9.81)^2} + 0 + 0.160$$

$$\Rightarrow 2.5 + 1.27 + 2 = \frac{P_2}{w} + 0.203 + 0.160$$

$$5.77 = \frac{P_2}{w} + 0.363$$

$$\frac{P_2}{w} = 5.77 - 0.363$$

$$\frac{P_2}{w} = 5.41 \text{ m}$$

Head at larger end = 5.41 m

2) $d_1 = 20 \text{ cm} = 0.2 \text{ m}$ inlet

$$A_1 = \frac{\pi \times (0.2)^2}{4} = 0.03142 \text{ m}^2$$

$d_2 = 10 \text{ cm} = 0.1 \text{ m}$ (throat)

$$A_2 = \frac{\pi \times (0.1)^2}{4} = 0.00785 \text{ m}^2$$

Vacuum pressure = 30 cm Hg = 0.3 m Hg

$Q = ?$

$$h_1 = \frac{P_1}{\rho g} = \frac{176580}{9.81 \times 1000} = 18 \text{ m}$$

$$h_2 = \frac{P_2}{w} = -0.3 \text{ m of mercury} \\ = -0.3 \text{ m} \times 13.6 = -4.08 \text{ m of water}$$

N/B

$$C_d = 0.98$$

$$P_1 = 17.658 \text{ N/cm}^2$$

$$= \frac{17.658}{10^{-4}}$$

$$= 176580 \text{ N/m}^2$$

$$h = \frac{P_1}{\rho g} - \frac{P_2}{\rho g}$$

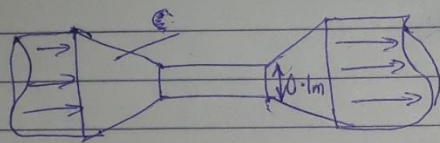
$$= 18 - (-4.08) = 22.08 \text{ m}$$

$$Q = C_d A_1 A_2 \sqrt{2gh} / \sqrt{A_1^2 - A_2^2}$$

$$Q = \frac{0.98 \times 0.03142 \times 0.00785 \times \sqrt{2 \times 9.81 \times 22.08}}{\sqrt{0.03142^2 - 0.00785^2}}$$

$$Q = 2.42 \times 10^{-4} \times \sqrt{433.21} / \sqrt{9.26 \times 10^{-4}}$$

$$Q = 5.037 \times 10^{-3} / 0.0304 = 0.166 \text{ m}^3/\text{s}$$



$$3) d_0 = 15 \text{ cm} = 0.15 \text{ m}$$

$$d_1 = 30 \text{ cm} = 0.30 \text{ m}$$

$$A_0 = \frac{(0.15)^2}{4} = 0.0177 \text{ m}^2$$

$$h = \gamma \left(\frac{y}{\rho g} - 1 \right) = 0.9 \left(\frac{13.6}{0.9} - 1 \right)$$

$$h = 7.05 \text{ m}$$

$$Q = \frac{C_d A_0 \times A_1 \sqrt{2gh}}{\sqrt{A_1^2 - A_0^2}}$$

$$Q = \frac{0.64 \times 0.0177 \times 0.07 \times \sqrt{2 \times 9.81 \times 7.05}}{\sqrt{0.07^2 - 0.0177^2}}$$

$$Q = 9.326 \times 10^{-3} / 0.068 = 0.137 \text{ m}^3/\text{s}$$

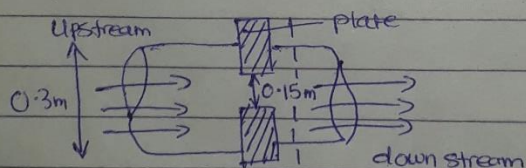
$$C_d = 0.64$$

$$S_g \text{ of } 0.1 = 0.9$$

Reading of differential manometer

$$y = 50 \text{ cm Hg}$$

$$= 0.5 \text{ m Hg}$$



4) Reading from manometer = 170 mmHg = 0.17 mHg

Specific gravity of mercury is 13.6

Specific gravity of sea water = 1.026

$$h = y \left(\frac{\rho_m}{\rho_f} - 1 \right)$$

$$h = 0.17 \left(\frac{13.6}{1.026} - 1 \right)$$

$$h = 0.17 (12.26)$$

$$h = 2.084 \text{ m}$$

$$V = \sqrt{2gh} = \sqrt{2 \times 9.81 \times 2.084}$$
$$= \sqrt{40.89}$$
$$= 6.39 \text{ m/s}$$

5) Actual flow rate = 5 dm³/min = 5 l/min

a) P = 15 bar Speed = 1700 rpm Displacement = 10 cc/rev

$$\text{Torque} = 15 \text{ Nm} \quad \text{Volumetric efficiency} = \frac{\text{Theoretical flow}}{\text{Actual flow}} \times 100$$

Theoretical flow = Displacement \times Speed

$$\text{but } 10 \text{ cm}^3/\text{rev} = 10 \times 10^{-3} = 0.01 \text{ /rev}$$

$$\text{Theoretical flow} = 0.01 \times 1700 = 17 \text{ l/min}$$

$$\text{Volumetric efficiency} = \frac{5}{17} \times 100 = 0.294 \times 100 = 29.4\%$$

$$\text{b) Fluid power} = \frac{\text{Pressure} \times \text{Actual flow}}{600} = \frac{15 \times 5}{600} = 0.125 \text{ kW}$$

$$\text{c) Shaft power} = \frac{\text{fluid power}}{\text{efficiency of pump}} = \frac{125}{0.294} = 425.17 \text{ W}$$

General/overall efficiency = Volumetric efficiency \times hydraulic/mechanical efficiency

$$\text{Hydraulic efficiency} = \frac{\text{Theoretical torque}}{\text{Actual torque}}$$

$$\text{Theoretical torque} = \frac{10 \times 55}{20 \times 3.142} = 2.39 \text{ Nm}$$

$$\text{Hydraulic efficiency} = \frac{2.39}{15} = 0.16$$

$$\text{Overall efficiency} = 0.294 \times 0.16 \times 100 = 4.7\%$$