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Fluid mechanics

Question;

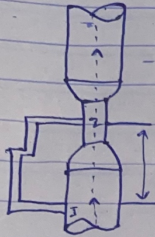
Given; Sp. gravity = 0.8, $D_1 = 150\text{mm} = 0.15\text{m}$; $D_2 = 75\text{mm} = 0.075\text{m}$

$Z_2 - Z_1 = 150\text{mm} = 0.15\text{m}$ $Q_{act} = 40\text{ liter/sec} = 0.04\text{ m}^3/\text{s}$ $C_d = 0.96$

Pressure difference ($P_1 - P_2$);

$$A_1 = \frac{\pi}{4} d^2 = \frac{\pi}{4} \times 0.15^2 = 0.01767\text{ m}^2$$

$$A_2 = \frac{\pi}{4} d^2 = \frac{\pi}{4} \times (0.075)^2 = 0.00442\text{ m}^2$$



$$Q_{act} = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}, \text{ we got}$$

$$0.04 = 0.96 \times \frac{0.01767 \times 0.00442}{\sqrt{(0.01767)^2 - (0.00442)^2}} \times \sqrt{2 \times 9.81 \times h}$$

$$h = \left(\frac{0.4}{0.96 \times 0.004565 \times 4.429} \right)^2$$

$$= 4.247\text{m}$$

$$\text{Also, } h = \left(\frac{P_1}{\rho g} + Z_1 \right) - \left(\frac{P_2}{\rho g} + Z_2 \right)$$

$$4.247 = \left(\frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) + (Z_1 - Z_2)$$

$$= \left(\frac{P_1 - P_2}{\rho g} \right) - 0.15$$

$$(P_1 - P_2) = \rho g (4.247 + 0.15)$$

$$= (0.8 \times 1000 \times 9.81) (4.247 + 0.15) \text{ N/m}^2$$

$$= 34.51 \text{ kN/m}^2$$

Question 2;

Diameter at inlet, $D_1 = 300\text{mm} = 0.3\text{m}$

Diameter at throat $D_2 = 0.15\text{m}$

Area of inlet $A_1 = \frac{\pi}{4} \times 0.3^2 = 0.07\text{m}^2$

Area at throat $= \frac{\pi}{4} \times 0.15^2 = 0.01767\text{m}^2$

specific gravity of heavy liquid (mercury) in U-tube manometer $S_H = 13.6$

S.G of liquid flowing through pipe $S_p = 0.9$

Reading of differential manometer $h = 250\text{mm} = 0.25\text{m}$

The differential 'h' is given by;

$$h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right)$$
$$= 0.20 \left[\frac{13.6}{0.9} - 1 \right] = 3.53 \text{ m of oil}$$

i) Discharge of oil

$$Q = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 + A_2^2}} \times \sqrt{2gh}$$

$$Q = 0.98 \times \frac{0.07 \times 0.001767}{\sqrt{0.07^2 + 0.001767^2}} \times \sqrt{2 \times 9.81 \times 3.53}$$

$$= 0.1489 \text{ m}^3/\text{s}$$

$$ii) h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right) = 3.53$$

$$\frac{P_1 - P_2}{\rho} = 3.53$$

$$P_1 - P_2 = (9.81) \times 0.9 \times 3.53$$

$$= 33.8 \text{ kN/m}^2$$