

Atkingbahon Clavefami
 Computr Engineering
 Matric No : 19ENG021004

1 $3te^{2t}$

Solution

Let $u = 3t$ and $dv = e^{2t}$

$$\frac{du}{dt} = 3$$

$$du = 3dt$$

$$v = \frac{e^{2t}}{2}$$

Using $UV - \int v du = \int u dv$

$$= 3t \left(\frac{e^{2t}}{2} \right) - \int \frac{e^{2t}}{2} \times 3dt$$

$$3t \left(\frac{e^{2t}}{2} \right) - \frac{1}{2} \int 3e^{2t} dt$$

$$3t \left(\frac{e^{2t}}{2} \right) - \frac{1}{2} \times \frac{3e^{2t}}{2}$$

$$\left[\frac{3}{2} te^{2t} - \frac{3e^{2t}}{4} \right] + C //$$

2 $\int x^2 \sin x$

Let $u = x^2$ and $dv = \sin x$

$$\frac{du}{dx} = 2x \text{ and } v = -\cos x$$

Using $UV - \int v du$

$$= (x^2)(-\cos x) - \int (-\cos x)(2x dx)$$

$$= -x^2 \cos x - \int -2x \cos x dx$$

~~$2x$~~ Let $u = -2x$ and $dv = \cos x$

$$(-2x) \sin x - \int (\sin x)(-2) dx$$

$$-2x \sin x - (-2) \int \sin x dx$$

at $t = 1$

$$\frac{d^2y}{dx^2} = 6(1) - 1$$
$$= 6 - 1$$
$$= 5$$

at $(1, 2)$ there is minimum point

2 $2y^2 - 5x^4 - 2 - 7y^3 = 0$

$$\frac{d}{dx} (2y^2) - \frac{d}{dx} (5x^4) - \frac{d}{dx} (2) - \frac{d}{dx} (7y^3) = 0$$
$$4y \frac{dy}{dx} - 20x^3 - 21y^2 \frac{dy}{dx} = 0$$

$$4y \frac{dy}{dx} - 21y^2 \frac{dy}{dx} = 20x^3$$

$$\frac{dy}{dx} = \frac{20x^3}{4y - 21y^2}$$

3 $4x^2 + 2xy^3 - 5y^2 = 0$

$$\frac{d}{dx} (4x^2) + \frac{d}{dx} (2xy^3) - \frac{d}{dx} (5y^2) = 0$$

$$8x + 2y^3 + 2x3y^2 \frac{dy}{dx} - 10y \frac{dy}{dx} = 0$$

$$2x3y^2 \frac{dy}{dx} - 10y \frac{dy}{dx} = 8x + 2y^3$$

$$\frac{dy}{dx} = \frac{8x + 2y^3}{2x3y^2 - 10y}$$

when $x = 1$ and $y = 2$

$$\frac{dy}{dx} = \frac{8(1) + 2(2)^3}{2(1)3(2)^2 - 10(2)} = \frac{24}{6} = 6$$