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MECHATRONICSS ENGINEERING

MATRIC NO: 18/ENG05/002

FLUID MECHANICS ASSIGNMENT

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Mechatronics Engineering

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Question 1

Data given

Specific gravity = 0.8

$d_1 = 150\text{mm} = 0.15\text{m}$

$d_2 = 75\text{mm} = 0.075\text{m}$

$z_1 - z_2 = 150\text{mm} = 0.15\text{m}$

$Q_{\text{actual}} = 140\text{ litres/s} = 0.04\text{m}^3/\text{s}$

$C_d = 0.96$

$P_1 - P_2 = ?$

Solution

$$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi (0.15)^2}{4} = 0.01767\text{m}^2$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{\pi (0.075)^2}{4} = 0.00442\text{m}^2$$

$$Q_{\text{actual}} = C_d \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$0.04 = 0.96 \times 0.01767 \times 0.00442 \times \frac{\sqrt{2 \times 9.81 \times h}}{\sqrt{0.01767^2 - 0.00442^2}}$$

$$0.04 = 0.96 \times 0.004565 \times 4.429\sqrt{h}$$

$$h = \left(\frac{0.04}{0.96 \times 0.004565 \times 4.429} \right)^2, h = 4.247\text{m}$$

$$h = \left(\frac{P_1}{\rho g} + z_1 \right) - \left(\frac{P_2}{\rho g} + z_2 \right)$$

$$4.247 = \left(\frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) + (z_1 - z_2)$$

$$4.247 = \left(\frac{P_1 - P_2}{\rho g} \right) - 0.15, P_1 - P_2 = \rho g (4.247 + 0.15)$$

$$P_1 - P_2 = (0.8 \times 1600 \times 9.81) (4.247 + 0.15)$$

$$P_1 - P_2 = 7848 \times 4.397 = 34507.7\text{N/m}^2$$

$$P_1 - P_2 = 34507.7\text{N/m}^2$$

Question 2

Data given

$$D_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$D_2 = 150 \text{ mm} = 0.15 \text{ m}$$

$$A_1 = \frac{\pi d^2}{4} = \frac{\pi (0.3)^2}{4} = 0.07 \text{ m}^2$$

$$A_2 = \frac{\pi d^2}{4} = \frac{\pi (0.15)^2}{4} = 0.01767 \text{ m}^2$$

Specific gravity of heavy fluid (mercury)
 $S_{hl} = 13.6$.

Specific gravity of oil = 0.9 = S_p

Reading of differential manometer,
 $y = 250 \text{ mm} = 0.25 \text{ m}$.

$$h = y \left(\frac{S_{hl}}{S_p} - 1 \right), \quad h = 0.25 \left(\frac{13.6}{0.9} - 1 \right)$$

$$h = 3.53 \text{ m of oil.}$$

① Discharge of oil

$$Q_{\text{actual}} = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2gh}$$

$$Q = 0.98 \times \frac{0.07 \times 0.01767}{\sqrt{0.07^2 - 0.01767^2}} \times \sqrt{2 \times 9.81 \times 3.53}$$

$$= \frac{0.001212}{0.0677} \times 8.32 = 0.1489 \text{ m}^3/\text{s}$$

$\therefore Q$, Discharge of oil = $0.1489 \text{ m}^3/\text{s}$.

② (ii) $P_1 - P_2 = ?$

$$h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right)$$

$$z_1 - z_2 = 300 \text{ mm} = 0.3 \text{ m}$$

$$3.53 = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) - 0.3$$

$$\left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) = 3.53 + 0.3$$

$$P_1 - P_2 = \rho g (3.53 + 0.3)$$

QUESTION 2 SOLUTION CONTINUATION

Question

Solution Continuation

$$P_1 - P_2 = (9.81 \times 0.9) (3.83)$$

$$P_1 - P_2 = 8.829 \times 3.83$$

$$P_1 - P_2 = 33.82 \text{ kN/m}^2$$

∴ Pressure difference between the entrance section and throat section is 33.82 kN/m^2