

Maths 102

Mechanical Engineering.

$$A = 3i + 4j - 6k, B = 5i - 11j + 2k, C = 7i - 7j + k$$

$$(1) A \cdot C + B \cdot C$$

$$A \cdot C = (3i + 4j - 6k) \cdot (7i - 7j + k)$$

$$= 21 + (-28) + (-6)$$

$$= -13$$

$$B \cdot C = (5i - 11j + 2k) \cdot (7i - 7j + k)$$

$$= 35 + 77 + 2$$

$$= 114$$

$$A \cdot C + B \cdot C = -13 + 114 = 101$$

$$(2) (A - B) \cdot C$$

$$A - B = 3i + 4j - 6k$$

$$- 5i - 11j + 2k$$

$$= -2i + 15j - 8k$$

$$(A - B) \cdot C = (-2i + 15j - 8k) \cdot (7i - 7j + k)$$

$$= -14 + (-105) + (-8)$$

$$= -127$$

$$(3) A \cdot (B \times C) =$$

$$= \begin{vmatrix} i & j & k \\ 3 & 4 & -6 \\ 5 & -11 & 2 \\ 7 & -7 & 1 \end{vmatrix}$$

$$= 3 \begin{vmatrix} -11 & 2 \\ -7 & 1 \end{vmatrix} + 4 \begin{vmatrix} 5 & 2 \\ 7 & 1 \end{vmatrix} - 6 \begin{vmatrix} 5 & -11 \\ 7 & -7 \end{vmatrix}$$

$$= 3 [(-11 \times 1) - (-7 \times 2)] + 4 [(5 \times 1) - (7 \times 2)] - 6 [(-7 \times 5) - (-11 \times 7)]$$

$$= 3 [3] + 4 [-9] - 6 [42]$$

$$= 9 + 36 - 252$$

$$= -207$$