

Hydrostatika
 14/05/2016
 chemical engineering

$$1. A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.075^2}{4} = 0.00442$$

$$Q = C_d \times A_1 \cdot A_2 \times \frac{\sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$0.04 = 0.96 \times 0.01767 \times 0.00442 \times \frac{\sqrt{2 \times 9.81 \times h}}{\sqrt{0.01767^2 - 0.00442^2}}$$

$$0.04 = 0.96 \times 0.004565 \times 4.429 \sqrt{h}$$

$$h = \left(\frac{0.04}{0.96 \times 0.004565 \times 4.429} \right)^2 = 4.247 \text{ m}$$

$$h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right)$$

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + (z_1 - z_2)$$

$$4.247 = \left(\frac{P_1 - P_2}{\rho} \right) + 0.15$$

$$(4.247 + 0.15) \rho = P_1 - P_2$$

$$(4.247 + 0.15) \rho = P_1 - P_2$$

$$P_1 - P_2 = (0.8 \times 1000 \times 9.81) (4.247 + 0.15)$$

$$P_1 - P_2 = 34.51 \text{ kPa}$$

$$3. D_1 = 0.3 \text{ m} \quad A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.07 \text{ m}^2$$

$$D_2 = 0.15 \text{ m} \quad A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

S.g of mercury = 13.6

Differential 'h' is given by

$$h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right)$$

$$= \gamma \left(\frac{\rho_{\text{oil}}}{\rho_{\text{sp}}} - 1 \right) = 0.25 \left(\frac{8.6}{0.9} - 1 \right) = 3.53 \text{ m of oil}$$

a. Discharge of oil

$$Q = C_d \times A_1 A_2 \times \sqrt{2gh} \\ \sqrt{A_1^2 - A_2^2}$$

$$Q = \frac{0.98 \times 0.07 \times 0.07767 \times \sqrt{2 \times 9.81 \times 3.53}}{\sqrt{0.07^2 - 0.07767^2}} \\ = 0.1489 \text{ m}^3/\text{s}$$

b. Pressure difference between entrance and throat at section $P_1 - P_2$

$$h = \left(\frac{P_1}{\rho} + z_1 \right) - \left(\frac{P_2}{\rho} + z_2 \right) = 3.53$$

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) + (z_1 - z_2) = 3.53$$

$$z_2 - z_1 = 0.3 \text{ m}$$

$$\left(\frac{P_1 - P_2}{\rho} \right) - 0.3 = 3.53$$

$$\frac{P_1 - P_2}{\rho} = 3.83$$

$$P_1 - P_2 = 3.83 \times 9.81 \times 0.9 \\ = 33.8 \text{ kN/m}^2$$

