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Electrical Engineering

Fluid Mechanics - Assignment 1

f. Diameter of inlet of $P_1 = 30 \text{ mm} = 0.03 \text{ m}$

$$\text{Area of inlet } A_1 = \frac{\pi}{4} \times 0.03^2 = 0.0007 \text{ m}^2$$

Diameter of throat $D_2 = 10 \text{ mm} = 0.01 \text{ m}$

$$\therefore \text{Area of throat } A_2 = \frac{\pi}{4} \times 0.01^2 = 0.0000785 \text{ m}^2$$

Specific gravity of heavy liquid (mercury) in tube manometer $s_k = 13.6$

Specific gravity of liquid (oil) flowing through pipe $s_f = 0.9$

Reading of differential manometer $h = 258 \text{ mm} = 0.258 \text{ m}$

\Rightarrow the differential head is given by:

$$h = \left[\frac{P_1}{\rho} + z_1 \right] - \left[\frac{P_2}{\rho} + z_2 \right] = \frac{g}{\rho} \left[\frac{s_k - 1}{s_f} \right] = 0.258 \left[\frac{13.6 - 1}{0.9} \right]$$

$$= 3.55 \text{ m of oil}$$

Discharge of oil, Q :

Using the equation,

$$Q = \frac{C_d \times A_2 \times \sqrt{2gh}}{\sqrt{1 - \left(\frac{A_2}{A_1}\right)^2}}$$

$$Q = 0.98 \times \frac{0.0000785 \times \sqrt{2 \times 9.81 \times 3.55}}{\sqrt{1 - \left(\frac{0.0000785}{0.0007}\right)^2}}$$

$$Q = \frac{0.000212 \times 3.62}{0.997}$$

$$\therefore Q = 0.189 \text{ m}^3/\text{s}$$

a. Pressure difference between entrance and throat section 1-2

$$h = \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) \left(\frac{1}{u} \right) = 3.53$$

$$\text{But } u = 30 \text{ mm} = 0.03 \text{ m}$$

$$\therefore \left(\frac{P_1}{\rho} - \frac{P_2}{\rho} \right) 0.03 = 3.53$$

$$\therefore P_1 - P_2 = (\rho g h) \times 0.1 \times 3.83$$

$$= 35.8 \text{ KN/m}^2$$

9. Pressure difference (P_1, P_2):

$$A_1 = \frac{\pi d_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

$$A_2 = \frac{\pi d_2^2}{4} = \frac{\pi \times (0.075)^2}{4} = 0.00442 \text{ m}^2$$

$$C_{\text{out}} = C_d \times \frac{A_1 A_2}{\sqrt{A_1^2 - A_2^2}} \times \sqrt{2g h}$$

$$0.04 = \frac{0.96 \times 0.01767 \times 0.00442 \times \sqrt{2 \times 9.81 \times h}}{\sqrt{0.01767^2 - 0.00442^2}}$$

$$\therefore h = \left(\frac{0.04}{0.96 \times 0.004565 + 4.429} \right) = 4.247 \text{ m}$$

$$\therefore \text{Also } h = \left(\frac{P_1}{\rho g} + z_1 \right) - \left(\frac{P_2}{\rho g} + z_2 \right)$$

$$4.247 = \left(\frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) (z_1 - z_2)$$

$$(P_1 - P_2) = \rho g (4.247 + 0.15)$$

$$= (0.8 \times 1000 \times 9.81) (4.247 + 0.15)$$

$$= 34.51 \text{ KN/m}^2$$