

② Diameter of inlet  $D_1 = 300\text{mm} = 0.3\text{m}$   
 Area of inlet  $A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.3^2}{4} = 0.0707\text{m}^2$

Diameter of inlet  $D_2 = 150\text{mm} = 0.15\text{m}$   
 Area of inlet  $A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767\text{m}^2$

Specific gravity of heavy liquid (mercury) in U-tube manometer  $S_H = 13.6$   
 Specific gravity of liquid flowing through pipe  $S_L = 0.9$

Reading of differential manometer  $y = 250\text{mm} = 0.25\text{m}$

The differential head  $h$  is given by

$$h = \left( \frac{P_1}{\rho} + z_1 \right) - \left( \frac{P_2}{\rho} + z_2 \right)$$

$$= y \left( \frac{S_H}{S_L} - 1 \right) = 0.25 \left( \frac{13.6}{0.9} - 1 \right) = 3.53\text{m of oil.}$$

③ Discharge of oil

Using the relation

$$Q = \frac{C_d A_1 A_2 \sqrt{2gh}}{\sqrt{A_1^2 - A_2^2}}$$

$$Q = \frac{0.98 \times 0.07 \times 0.01767 \times \sqrt{2 \times 9.81 \times 3.53}}{\sqrt{0.07^2 - 0.01767^2}} = 0.1489\text{m}^3/\text{s}$$

④ Pressure difference b/w entrance & throat section

$$h = \left( \frac{P_1}{\rho} + z_1 \right) - \left( \frac{P_2}{\rho} + z_2 \right) = 3.53$$

$$h = \left( \frac{P_1}{\rho} - \frac{P_2}{\rho} \right) - (z_1 - z_2) = 3.53$$

$$z_2 = z_1 = 300\text{mm} = 0.3\text{m}$$

$$\left( \frac{P_1 - P_2}{\rho} \right) - 0.3 = 3.53$$

$$\frac{P_1 - P_2}{\rho} = 3.53 + 0.3$$

$$\frac{P_1 - P_2}{\rho} = 3.83 \quad \therefore P_1 - P_2 = 3.83\rho$$

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Mechanical Engineering

Fluid Mechanics (ENR 214)

Assignment

Given or find  $Q$  given  $Q$  &  $D_1 = 150 \text{ mm} = 0.15 \text{ m}$ ,  $P_2 = 50 \text{ mm} = 0.05 \text{ m}$

$Z_2 - Z_1 = 90 \text{ mm} = 0.09 \text{ m}$ ,  $\rho = 1000 \text{ kg/m}^3$ ,  $C_d = 0.96$

Pressure difference ( $P_1 - P_2$ )

$$A_1 = \frac{\pi D_1^2}{4} = \frac{\pi \times 0.15^2}{4} = 0.01767 \text{ m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi \times 0.05^2}{4} = 0.00196 \text{ m}^2$$

$$Q = C_d \times A_1 \times A_2 \times \sqrt{2gh}$$

$$0.04 = \frac{0.96 \times 0.01767 \times 0.00196 \times \sqrt{2 \times 9.81 \times h}}{\sqrt{0.01767^2 - 0.00196^2}}$$

$$0.04 = 0.96 \times 0.004585 \times 4.425h$$

$$h = \left( \frac{0.04}{0.96 \times 0.004585 \times 4.425} \right)^2 = 4.247 \text{ m}$$

$$h = \left( \frac{P_1}{\rho g} + Z_1 \right) - \left( \frac{P_2}{\rho g} + Z_2 \right)$$

$$h = \left( \frac{P_1}{\rho g} - \frac{P_2}{\rho g} \right) + (Z_1 - Z_2)$$

$$4.247 = \left( \frac{P_1 - P_2}{\rho g} \right) - 0.15$$

$$4.247 + 0.15 = \frac{P_1 - P_2}{\rho g}$$

$$(4.247 + 0.15) \times \rho g = P_1 - P_2$$

$$P_1 - P_2 = (0.8 \times 1000 \times 9.81)(4.247 + 0.15)$$

$$P_1 - P_2 = 34.51 \text{ kN/m}^2 //$$