

Name: Lidoh Imeh Victoria

Dept: Petroleum Engineering

Matric No: 19/EN607/022

Lecturer's Name: Mr Joseph Temitayo Okuntola

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### Questions

1) Find the equation of the tangent at the point (1, 0) on the circle

$$x^2 + y^2 - 5x - y + 4 = 0$$

#### Solution

$$x^2 + y^2 + 2gx + 2fy + c = 0$$

$$g = -\frac{5}{2}, 2gx = -5x, 2fy = -y, f = -\frac{1}{2}$$

So, the centre of the circle is  $(\frac{5}{2}, \frac{1}{2})$

$$m_1 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\frac{1}{2} - 0}{\frac{5}{2} - 1}$$

$$m_1 = \frac{1/2}{3/2} = \frac{1}{3}$$

By tangent  $m_1 m_2 = -1$   $m_2 = -3$

Hence eqn is  $y - y_1 = m(x - x_1)$

$$y - 0 = -3(x - 1)$$

$$y = -3x + 3$$

2) Find the equation of the tangent at the point (1, 0) on the circle  
 $x^2 + y^2 - 12x - 12y + 47 = 0$

#### Solution

$$2gx = -12x \quad 2fy = -12y \quad g = -6 \quad f = -6$$

Centre of circle  $\Rightarrow (6, 6)$

$$m_1 = \frac{y_2 - y_1}{x_2 - x_1} \Rightarrow \frac{6 - 0}{6 - 1} \quad m_1 = 6/5$$

$$m_1 m_2 = -1 \quad m_2 = -5/6 \quad \text{eqn} \Rightarrow y - y_1 = m_2(x - x_1)$$

$$y - 0 = -5/6(x - 1) \quad y = -5/6x + 5/6$$

3) Find the equation of the tangent at the point (1, 0) on the circle  
 $x^2 + y^2 - 8x + 14y + 40 = 0$

#### Solution

$$2gx = -8x \quad g = -4 \quad 2fy = 14y \quad f = 7$$

Centre of circle (4, 7)

$$m_1 = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-7}{3}$$

$$m_2 = \frac{3}{7}$$

$$\text{equ } y - 0 = \frac{3}{7} (x - 1)$$

$$y = \frac{3}{7}x - \frac{3}{7}$$