NAME: John Tisan

MATRIC NO: 18/SCI01/044

QUESTIONS

1). Explain with 2 examples what you understand by linear transformation.

2). Given a linear transformation of a matrix operator A on a vector x, compute T(x) if A=(1,9,3), (-2,6,7), (0, -1,3) and

x= 1

4

-8

3). Define completely with mathematical examples what you understand by Rank of a matrix.

SOLUTION

1. A linear transformation is a unction from one vector space to another that respects the underlying (linear) structure of each vector pace. It is also known as a linear operator or map.

Examples

(a.) The **expected value** of a random variable(which is in fact a function, and a member of a vector space)

E(X + Y) = E(x) + E(Y) and E[aX] = aE[X].

(b.) An identity map on any module is a linear transformation.

2.
$$\begin{pmatrix} 1 & 9 & 3 \\ -2 & 6 & 7 \\ 0 & -1 & 3 \end{pmatrix} X = \begin{pmatrix} 1 \\ 4 \\ -8 \end{pmatrix}$$
$$T(x) = A(x)$$
$$T(x) = 1 \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix} + \begin{pmatrix} 9 \\ 6 \\ -1 \end{pmatrix} - 8 \begin{pmatrix} 3 \\ 7 \\ 3 \end{pmatrix}$$

$$\begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix} + \begin{pmatrix} 36 \\ 24 \\ -4 \end{pmatrix} + \begin{pmatrix} -24 \\ -56 \\ -24 \end{pmatrix}$$
$$= \begin{pmatrix} 13 \\ -34 \\ -28 \end{pmatrix}$$
 Hence, the transformation of
$$\begin{pmatrix} 1 \\ 4 \\ -8 \end{pmatrix}$$

3. The rank of a matrix is defined as the maximum number of linearly independent column vector in the matrix or maximum number of linearly independent roe vector in the matrix. Example

A= 1 -3 6
4 0 2
8 5 1
(i.) RANK OF A

$$|A| = \begin{vmatrix} 1 & -3 & 6 \\ 4 & 0 & 2 \\ 8 & 5 & 1 \end{vmatrix}$$

= 1 $\begin{vmatrix} 0 & 2 \\ 5 & 1 \end{vmatrix} -(-3) \begin{vmatrix} 4 & 2 \\ 8 & 1 \end{vmatrix} + 6 \begin{vmatrix} 4 & 0 \\ 8 & 5 \end{vmatrix}$
= 1(0 - 10) +3(4-16) +6(20-0)
= -10 - 36 + 120
= 74
Since $|A| \neq 0$, The Rank of A is 3

Since
$$|A| \neq 0$$
, The Rank of A is 3

Note: But if the determinant of the matrix is equal to 0 then we delete arrow and column of the 3 x 3 matrix forming a 2 x 2 matrix then we find the determinant of the matrix. If we get an answer not equal to 0 then the matrix of rank 2