

1)  $x^2 \sin x \, dx$

$U = x^2 \quad du = 2x$   
 $\frac{du}{dx} = 2x \quad V = -\cos x$

$\int Udv = UV - \int Vdu$

$\int x^2 \sin x = (x^2)(-\cos x) - \int (-\cos x)(2x \, dx)$   
 $= -x^2 \cos x - \int -2x \cos x$

$U = -2x \quad du = \cos x$   
 $\frac{du}{dx} = -2 \quad V = \sin x$   
 $\int Udv = (-2x \sin x) - \int (\sin x)(-2 \, dx)$   
 $= -2x \sin x + 2 \cos x + C$

$\therefore \int x^2 \sin x = -x^2 \cos x + 2x \sin x + 2 \cos x + C$

2)  $3t e^{2t} \, dt$

$U = 3t \quad du = e^{2t}$   
 $\frac{du}{dt} = 3 \quad V = \frac{1}{2} e^{2t}$

$\int Udv = UV - \int Vdu$

$\int 3t e^{2t} = (3t)(\frac{1}{2} e^{2t}) - \int (\frac{1}{2} e^{2t})(3 \, dt)$   
 $= \frac{3t e^{2t}}{2} - \frac{3}{4} e^{2t} + C$

3)  $2x^2 \ln x \, dx$

$U = \ln x \quad du = \frac{1}{x}$   
 $\frac{du}{dx} = \frac{1}{x} \quad V = \frac{2x^3}{3}$

$\int Udv = UV - \int Vdu$

$\int 2x^2 \ln x = (\ln x)(\frac{2x^3}{3}) - \int (\frac{2x^3}{3})(\frac{1}{x} \, dx)$

DR. OYELAMI

$= \frac{2x^3 \ln x}{3} - \frac{2x^3}{9} + C$

4)  $\left( \frac{2x-3x^2}{1-x} \right)$

$= \frac{-3x^2+2x}{-x+1} = \frac{3x+1}{-x+1} \sqrt{-3x^2+2x}$   
 $\frac{-3x^2+3x}{-x+1}$   
 $\frac{-x}{-x+1}$   
 $\frac{-1}{-1}$

$\left( \frac{2x-3x^2}{1-x} \right) = \int (3x+1) \, dx + \int \frac{-1}{-x+1} \, dx$

$= \frac{3x^2}{2} + x + \ln(1-x) + C$