

Mechatronics Engineering

1 $x^2 \sin x$

$u = x^2$

$v = \sin x$

$\frac{du}{dx} = 2x$

$\frac{dv}{dx} = -\cos x$

$$\int u dv = uv - \int v du$$

$$= -x^2 \cos x - \int -\cos x \cdot 2x dx$$

$$= -x^2 \cos x - \int -2x \cos x dx$$

$u = -2x$ $v = \sin x$

$\frac{du}{dx} = -2$ $\frac{dv}{dx} = \cos x$

~~$\int -2x \cos x dx$~~

$$= -2x \sin x - \int \sin x dx$$

$$= -2x \sin x + \cos x$$

$\therefore -x^2 \cos x - 2x \sin x + \cos x + C$

(2) $\int 3te^{2t} dt = \left[\frac{3}{2} te^{2t} - \frac{3e^{2t}}{4} \right] + C$

(3) $\int 2x^2 \ln x dx = \left[\frac{2}{3} x^3 (\ln x - \frac{1}{3}) \right] + C$

(4) $\int \frac{12x - 3x^2}{(1-x)^2} dx$

$$= -x + 1 + \frac{3x+1}{-3x^2+2x}$$

$$= -x + 1 + \frac{-3x^2+3x}{-3x^2+2x}$$

$$= -x + 1 + \frac{-x}{-x+1}$$

$$= -1$$

$$\int (3x+1) dx + \int \left(\frac{-1}{x+1} \right) dx$$

$$\frac{3x^2}{2} + x - \ln(-x+1) + c$$