

ASSIGNMENT 3

1. Given $\mu = 0.9 \text{ Ns/m}^2$, $\rho = 1260 \text{ kg/m}^3$, $L = 65 \text{ m}$, $D = 10 \text{ mm} = 0.01 \text{ m}$,

$$q = 180 \text{ lt/min} = 0.003 \text{ m}^3/\text{s}$$

a. From continuity equation

$$q = A \cdot u$$

$$\text{where } A = \frac{\pi D^2}{4} = \frac{\pi \times (0.01)^2}{4} = 7.855 \times 10^{-5} \text{ m}^2$$

$$\therefore u = \frac{q}{A} = \frac{0.003}{7.855 \times 10^{-5}} = 38.19 \text{ m/s}$$

$$\therefore Re = \frac{\rho u D}{\mu} = \frac{1260 \times 38.19 \times 0.01}{0.9} = 534.66$$

Because $Re < 2000$, the flow is laminar

$$\text{b. } \Delta P = \frac{32 \mu u L}{D^2} = \frac{32 \times 0.9 \times 38.19 \times 65}{(0.01)^2} = \frac{71491.68}{0.0001} = 7.15 \times 10^8 \text{ N/m}^2$$

2. Given $\mu = 800 \text{ cp} = 0.8 \text{ Ns/m}^2$, $G = 0.85$, $\rho = 850 \text{ kg/m}^3$,

$$dp = 2000 \times 10^3 \text{ N/m}^3, D = 65 \text{ mm} = 0.065 \text{ m}, L = 95 \text{ m}$$

$$\text{a. } A = \frac{\pi D^2}{4} = \frac{\pi \times (0.065)^2}{4} = 3.319 \times 10^{-3} \text{ m}^2$$

$$\frac{dp}{dx} = \frac{-2000 \times 10^3}{95} = -21.05 \times 10^3$$

Rate of flow, $Q = A \cdot u$

$$\text{Where } u = \frac{-1dp}{8\mu dx} R^2$$

$$= \left(\frac{-1}{8 \times 0.8} \right) (-21.05 \times 10^3)(0.0325)^2 = 3.474 \text{ m/s}$$

$$\therefore Q = 3.474 \times 3.319 \times 10^{-3} = 0.0115 \text{ m}^3/\text{s}$$

b. Centre line velocity = u_{\max}

$$\text{But, } u_{\max} = 2 \times u$$

$$= 2 \times 3.474 = 6.948 \text{ m/s}$$

c. Total frictional drag, f_D

$$f_D = \tau_0 \pi D L$$

$$\text{Where } \tau_0 = \frac{-\partial p r}{\partial x} = 21.05 \times 10^3 \times \frac{0.0325}{2}$$

$$\tau_0 = 342.0625 \text{ N/m}^2$$

$$\therefore f_D = 342.0625 \times \pi \times 0.065 \times 95 = 6636.645 \text{ N} \approx 6.637 \text{ kN}$$

d. Power required to maintain flow

$$P = f_D \times u$$

$$= 6636.645 \times 3.474$$

$$P = 23055.7 \text{ Watts}$$

$$P = 23 \text{ kW}$$

e. Velocity gradient at the pipe wall

$$\tau_0 = \frac{\mu \partial u}{\partial y} @ y = 0$$

$$\therefore \frac{\partial u}{\partial y} = \frac{\tau_0}{\mu} = \frac{342.0625}{0.8} = 427.584 \text{ s}^{-1}$$

f. Velocity and shear stress 60mm from wall

$$u = \frac{-1 \partial p}{4 \mu \partial x} (R^2 - r^2)$$

$$\text{but } y = R - r \text{ and } y = 60 \text{ mm} = 0.06 \text{ m}$$

$$\therefore 0.06 = 0.065 - r$$

$$r = 0.005$$

$$\therefore u = \frac{-1}{(4 \times 0.8)} (-21.05 \times 10^3) (0.065^2 - 0.005^2)$$

$$u = 27.628 \text{ m/s}$$

The shear stress can be found as;

$$\frac{\tau}{r} = \frac{\tau_0}{R}$$

$$\therefore \tau = \frac{r \times \tau_0}{R} = \frac{0.005 \times 342.0625}{0.065} = 26.3125 \text{ N/m}^2$$