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compute

i) Initial temp = 10°C $T_b = 20^{\circ}\text{C}$ @ 5 mins

$$\frac{dT}{dt} \propto (T - T_a) \quad \text{Actual} = 25^{\circ}\text{C} \quad T_a = \text{Actual temperature}$$
$$\frac{dT}{dt} = -k(T - T_a)$$
$$\frac{dT}{dt} = -k(T - 25)$$

collecting like terms

$$\frac{dT}{(T - 25)} = -k dt$$

Integrating both sides

$$\ln(T - 25) = -kt + C$$
$$\therefore T - 25 = e^{-kt + C} \quad \text{where } e^C = A$$
$$T - 25 = e^{-kt} \cdot e^C$$
$$T - 25 = A e^{-kt}$$
$$T = A e^{-kt} - 25$$

at initial conditions $t = 0$, $T = 10^{\circ}\text{C}$

$$10 = A e^0 - 25$$

$$A = 35$$

$$T = 35 e^{-kt} - 25$$

at $T = 20^{\circ}\text{C}$ $t = 5$ mins

$$20 = 35 e^{5k} - 25$$

$$e^{5k} = \frac{45}{35}$$

$$5k = \ln\left(\frac{45}{35}\right)$$

$$k = \frac{0.25}{5}$$

$$k = 0.05$$

$$T = 35e^{0.05t} - 25$$

$$T = 24.9 \text{ at } t = ?$$

$$24.9 = 35e^{0.05t} - 25$$

$$49.9 = 35e^{0.05t}$$

$$e^{0.05t} = 49.9/35$$

$$e^{0.05t} = \ln(1.426)$$

$$0.05t = \ln(1.426)$$

$$T = 7.1 \text{ minutes}$$



