

1. Point (1,0)

Equation of the circle $x^2 + y^2 - 5x - y + 4 = 0$
 $\frac{dy}{dx} (2y-1) = 5-2x$

$$\frac{dy}{dx} = \frac{5-2x}{2y-1}$$

when $x=1, y=0$

$$m = \frac{5-2(1)}{2(0)-1}$$

$$= \frac{5-2}{0-1}$$

$$= \frac{3}{-1}$$

$$= -3$$

$$y - y_1 = m(x - x_1)$$

$$y - 0 = -3(x - 1)$$

$$y = -3x + 3 \text{ (equation of the tangent)}$$

2. Point (1,0)

Equation of the circle: $x^2 + y^2 - 12x - 12y + 47 = 0$

$$2x + 2y \frac{dy}{dx} - 12 - 12 \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} (2y-12) = 12-2x$$

$$\frac{dy}{dx} = \frac{12-2x}{2y-12}$$

$$\frac{dy}{dx} = \frac{6-x}{y-6}$$

When $x=1, y=0$

$$m = \frac{6-1}{0-6}$$

$$= \frac{5}{-6}$$

$$y - y_1 = m(x - x_1)$$

$$y - 0 = -5/6(x - 1)$$

$$y = -5/6x + 5/6$$

$$6y = -5x + 5 \quad (\text{equation of the tangent})$$

3. Point (1,0)

$$\text{Equation of the circle } x^2 + y^2 - 8x + 14y + 40 = 0$$

$$2x + 2y \frac{dy}{dx} - 8 + 14 \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} (2y + 14) = 8 - 2x$$

$$\frac{dy}{dx} = \frac{8 - 2x}{2y + 14}$$

$$\text{when } x = 1, y = 0$$

$$m = \frac{8 - 2(1)}{2(0) + 14}$$

$$= \frac{8 - 2}{0 + 14}$$

$$= \frac{6}{14} = \frac{3}{7}$$

$$\text{W/F } y - y_1 = m(x - x_1)$$

$$y - 0 = 3/7(x - 1)$$

$$y = 3/7x - 3/7$$

$$\cancel{7y = 3x - 3} \quad 7y = 3x - 3$$

(equation of the tangent)