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17/ENG05/030

MECHATRONICS ENGINEERING

ENG322 ASSIGNMENT

i) A parallel resonant circuit has $R = 100 \text{ k}\Omega$, $L = 20 \text{ mH}$, and $C = 5 \text{ mF}$. Calculate ω_0 , ω_1 , ω_2 , Q and B

Solution

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{(20 \times 10^{-3}) \times (5 \times 10^{-3})}}$$
$$= 100 \text{ Krad/s}$$

$$B = \frac{\omega_0}{Q} = \frac{1}{RC} = \frac{1}{100 \times (5 \times 10^{-3})}$$
$$= 2 \text{ Krad/s}$$

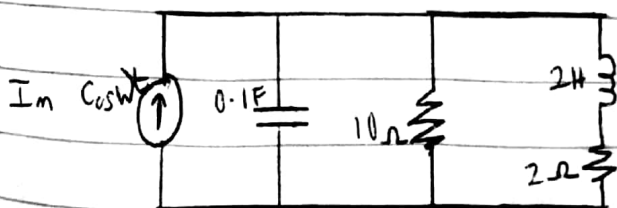
From the equations above we know that $\omega_0 = 100 \text{ Krad/s}$ and $B = 2 \text{ Krad/s}$

$$Q = \frac{\omega_0}{B} = \frac{100 \times 10^3}{2 \times 10^3} = \frac{100}{2} = 50$$

Since $Q \geq 10$

$$\omega_1 = \omega_0 - \frac{B}{2} = 100 \times 10^3 - \frac{2 \times 10^3}{2} = 99 \text{ Krad/s}$$
$$\omega_2 = \omega_0 + \frac{B}{2} = 100 \times 10^3 + \frac{2 \times 10^3}{2} = 101 \text{ Krad/s}$$

ii) Determine the resonant frequency of the circuit below:



The input admittance is

$$Y = j\omega 0.1 + \frac{1}{10} + \frac{1}{2 + j\omega 2}$$

$$= 0.1 + j\omega 0.1 + \frac{2 - j\omega 2}{4 + 4\omega^2}$$

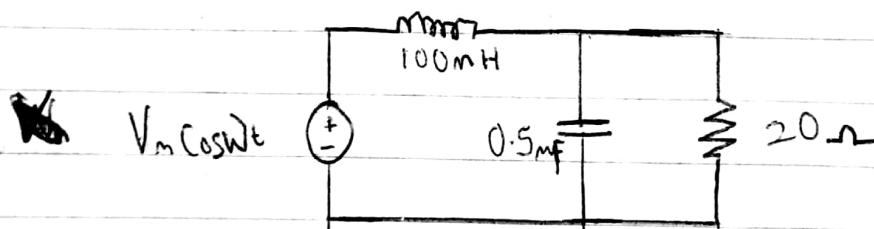
at Resonance

$$\text{Im}\{Y\} = 0$$

$$\omega_0 \cdot 0.1 = \frac{2\omega_0}{4 + \omega_0^2} = 0$$

$$\omega_0 = 2 \text{ rad/s}$$

3) Calculate the resonant frequency of the circuit below



Solution

$$20 + \frac{2000}{j\omega} = \frac{40000}{20j\omega + 2000} - \frac{40000}{20j\omega + 2000} + \frac{(20j\omega - 2000)}{(20j\omega - 2000)}$$

$$20 + \frac{2000}{j\omega}$$

$$= \frac{80000j\omega - 8000000}{-400j\omega - 4000000} + 100mH$$

At Resonance of the Imaginary part at $\omega = 0$
 $\frac{80,000 \text{ j}\omega}{-400 \text{ j}\omega - 4000000} + \text{j}\omega [100 \times 10^{-3}]$

$$= 800000 \omega + [-40\omega^2] - 4000000 \omega$$

$$= 400000 - 40\omega^2 = 0$$

$$-40\omega^2 = -400000$$

$$\omega^2 = 10000$$

$$\omega = \sqrt{10000}$$

$$\omega = 100 \text{ rad/s}$$