

1) A parallel resonant circuit has $R = 100 \text{ k}\Omega$, $L = 20 \text{ mH}$, and $C = 5 \text{ nF}$. Calculate ω_0 , ω_1 , ω_2 , Q and B .

Solution:

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{20 \times 10^{-3} \times 5 \times 10^{-9}}}$$

$$= 100000 \text{ rad/s}$$

$$= 100 \text{ Krad/s}$$

$$Q = \frac{R}{\omega_0 L} = \frac{100 \times 10^3}{100 \times 10^3 \times 20 \times 10^{-3}}$$

$$= 50$$

$$B = \frac{\omega_0}{Q} = \frac{100 \times 10^3}{50} = 2000 \text{ rad/s} = 2 \text{ Krad/s}$$

Since $Q \geq 10$

$$\omega_1 = \omega_0 - \frac{B}{2} = 100000 - \frac{2000}{2}$$

$$\omega_1 = 99000 \text{ rad/s}$$

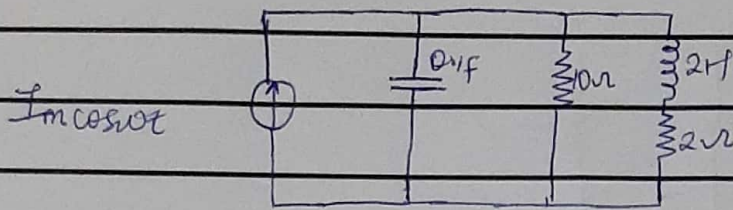
$$= 99 \text{ Krad/s}$$

$$\omega_2 = \omega_0 + \frac{B}{2} = 100000 + \frac{2000}{2}$$

$$\omega_2 = 101000 \text{ rad/s}$$

$$= 101 \text{ Krad/s}$$

v) Determine the resonant frequency of the circuit below



Solution.

$$X_C = \frac{1}{2\pi f_c} = \frac{1}{\omega_0} = \frac{1}{j\omega_0 \cdot 1}$$

$$X_L = 2\pi f L = \omega L = j\omega R$$

$$\frac{1}{Z} = Y = \frac{1}{X_C} + \frac{1}{R} + \frac{1}{X_C + R}$$

$$= j\omega_0 \cdot 1 + \frac{1}{10} + \frac{1}{j\omega_0 2 + 2}$$

$$= 0.1 + j\omega_0 \cdot 1 + \left[\frac{1}{2 + j\omega_0 2} \times \frac{2 - j\omega_0 2}{2 - j\omega_0 2} \right]$$

$$= 0.1 + j\omega_0 \cdot 1 + \frac{2 - j\omega_0 2}{4 + 4\omega_0^2}$$

at resonance, Imaginary of admittance = 0

$$\omega_0 \cdot 1 + \frac{2\omega_0}{4 + 4\omega_0^2} = 0$$

$$\omega_0 \cdot 1 \cdot \frac{(4 + 4\omega_0^2) + 2\omega_0}{4 + 4\omega_0^2} = 0$$

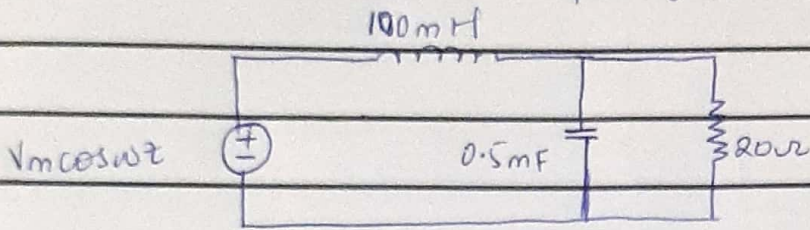
$$0.4\omega_0 + 0.4\omega_0^3 + 2\omega_0 = 0$$

$$0.4\omega_0^3 - 1.6\omega_0 = 0$$

solving quadratically

$$\omega_0 = \underline{\underline{2 \text{ rad/s}}} \quad \text{frequency can't be -ve.}$$

iii) Calculate the resonant frequency of the circuit below.



Solution

$$X_C = \frac{1}{2\pi f C} = \frac{1}{\omega C} = \frac{1}{j\omega 0.0005}$$

$$X_L = 2\pi f L = \omega L = j\omega 0.1$$

$$Z = X_L + \left(\frac{X_C \cdot R}{X_C + R} \right)$$

$$Z = j\omega 0.1 + \left[\frac{20 \times \frac{1}{j\omega 0.0005}}{\frac{1}{j\omega 0.0005} + 20} \right]$$

$$Z = j\omega 0.1 + \left[\frac{20}{j\omega 0.0005 + 20} \right] = \frac{20(j\omega 0.0005 + 1)}{j\omega 0.0005}$$

$$Z = j\omega 0.1 + \left[\frac{20}{j\omega 0.0005} \times \frac{j\omega 0.0005 + 1}{j\omega 0.0005 + 1} \right]$$

$$Z = j\omega 0.1 + \left[\frac{20}{1 + j\omega 0.01} \right]$$

rationalizing $\frac{20}{1 + j\omega 0.01} \times \frac{1 - j\omega 0.01}{1 - j\omega 0.01}$

$$\frac{20 - j\omega 0.2}{1 + 0.0001\omega^2}$$

$$Z = j\omega 0.1 + \frac{20 - j\omega 0.2}{1 + 0.0001\omega^2}$$

$$Z = \frac{j\omega 0.1 + 20}{1 + 0.0001\omega^2} - \frac{j\omega 0.2}{1 + 0.0001\omega^2}$$

$$Z = \frac{20}{1 + 0.0001\omega^2} + j\omega 0.1 - \frac{j\omega 0.2}{1 + 0.0001\omega^2}$$

$$Z = \frac{20}{1 + 0.0001\omega^2} + \left[\frac{j\omega 0.1 - \frac{j\omega 0.2}{1 + 0.0001\omega^2}}{1 + 0.0001\omega^2} \right]$$

At resonance Imaginary (Z) = 0

$$\frac{\omega_0 0.1 - \omega_0 0.2}{1 + 0.0001\omega_0^2} = 0$$

$$\frac{\omega_0 0.1(1 + 0.0001\omega_0^2) - \omega_0 0.2}{1 + 0.0001\omega_0^2} = 0$$

$$\omega_0 0.1 + 0.00001\omega_0^3 - \omega_0 0.2 = 0$$

$$0.00001\omega_0^3 - 0.1\omega_0 = 0$$

Solving using quadratic equation

$$\omega_0 = 100 \text{ rad/s}$$

frequency can't be negative