

Circuit theory assignment

$$① R = 100k\Omega = 100 \times 10^3$$

$$L = 20mH = 20 \times 10^{-3} H$$

$$C = 5nF = 5 \times 10^{-9} F$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{20 \times 10^{-3} \times 5 \times 10^{-9}}} = 100000 = 100 \text{ Krad/s}$$

$$Q = \frac{R}{\omega_0 L} = \frac{100 \times 10^3}{100 \times 10^3 \times 20 \times 10^{-3}} = 50$$

$$B = \frac{\omega_0}{Q} = \frac{100 \times 10^3}{50} = 2 \text{ Krad/s}$$

$$\omega_1 = \frac{\omega_0 - B}{2} = \frac{100 \times 10^3 - 2 \times 10^3}{2} = 99 \text{ Krad/s}$$

$$\omega_2 = \frac{\omega_0 + B}{2} = \frac{100 \times 10^3 + 2 \times 10^3}{2} = 101 \text{ Krad/s}$$

$$\frac{20 + \frac{2000}{j\omega}}{j\omega} = \frac{40000}{20j\omega + 2000} \quad \text{or} \quad \frac{40000}{20j\omega + 2000} \cdot \frac{(20j\omega - 2000)}{(20j\omega - 2000)}$$

$$\frac{20 + \frac{2000}{j\omega}}{j\omega} \Rightarrow \text{Resolving}$$

$$\frac{-80,000j\omega - 800,000 + 100000j}{-400j\omega - 400,000}$$

At resonance Imaginary part at  $\omega = 0$

$$\frac{80,000j\omega + j\omega(100 \times 10^3)}{-400j\omega - 400,000}$$

$$\frac{80000\omega + (100 \times 10^3)\omega}{-400\omega - 400,000}$$

$$\Rightarrow 80000\omega + (-400\omega^2) - 400000\omega$$

$$\Rightarrow 400000 - 400\omega^2 = 0$$

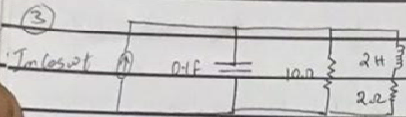
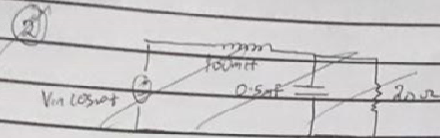
$$400\omega^2 = 400000$$

$$\omega^2 = \frac{400000}{400}$$

$$\omega^2 = 1000$$

$$\omega = \sqrt{1000}$$

$$\omega = 100 \text{ rad/s}$$



The input admittance is

$$Y = j\omega \cdot 0.1 + \frac{1}{10} + \frac{1}{2 + j\omega}$$

$$= 0.1 + j\omega \cdot 0.1 + \frac{2 - j\omega}{4 + 4\omega^2}$$

At resonance,

$$\text{Im}(Y) = 0$$

$$\omega \cdot 0.1 - \frac{2\omega}{4 + 4\omega^2} = 0$$

$$\omega = 2 \text{ rad/s}$$

