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EEF 322

$$1) \omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{(20 \times 10^{-3}) \times (5 \times 10^{-3})}}$$

$$= 100 \text{ k rad/s}$$

$$B = \frac{\omega_0}{Q} = \frac{1}{RC} = \frac{1}{100 \times (5 \times 10^{-3})}$$

$$= 2 \text{ k rad/s}$$

$$Q = \frac{\omega_0}{B} = \frac{100 \times 10^3}{2 \times 10^3} = 50$$

Since $Q \geq 10$

$$-\omega_1 = \omega_0 - B/2 = 100 \times 10^3 - \frac{2 \times 10^3}{2} = 99 \text{ k rad/s}$$

$$\omega_2 = \omega_0 + B/2 = 100 \times 10^3 + \frac{2 \times 10^3}{2} = 101 \text{ k rad/s}$$

ii) Input admittance:

$$Y = j\omega \cdot 0.1 + 1/10 + 1/2 + j\omega_2$$

$$= 0.1 + j\omega_0 + 1 + \frac{2 - j\omega_2}{4 + 4\omega^2}$$

at resonance

$$\text{Im}(Y) = 0$$

$$\omega_0 \cdot 0.1 = \frac{2\omega_0}{4 + \omega_0^2} = 0$$

$$\omega_0 = 2 \text{ rad/s}$$

$$3) \frac{20 + Z_0\omega}{j\omega} = \frac{400\omega}{20j\omega + 20\omega} - \frac{400\omega}{20j\omega + 20\omega}$$

$$+ \frac{(20j\omega - 20\omega)}{(20j\omega - 20000)}$$

$$= \frac{80000j\omega - 80000000}{-400j\omega - 4000000} + 100 \text{ mH}$$

At resonance of the imaginary part at $\omega = 0$

$$\frac{80000j\omega}{-400j\omega - 4000000} + j\omega[100 \times 10^{-3}]$$

$$= 800000\omega + [-40\omega^2] - 400000\omega$$

$$= 400000 - 40\omega^2 = 0$$

$$-40\omega^2 = -400000$$

$$\omega^2 = 10000$$

$$\omega = \sqrt{10000}$$

$$\omega = 100 \text{ rad/s}$$