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Circuit Theory

i) Parameters.

$$R = 100k\Omega, L = 20mH, C = 5nF.$$

Conversion

$$R = 100 \times 10^3, L = 20 \times 10^{-3}H, C = 5 \times 10^{-9}$$
$$= 100000$$

$$a) \omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{20 \times 10^{-3} \times 5 \times 10^{-9}}}$$

$$= \frac{1}{\sqrt{100 \times 10^{-12}}} = \frac{1}{10 \times 10^{-6}}$$

$$= 10^{-1} \times 10^6$$

$$= 10^5$$

$$= 100k\text{rad/s.}$$

$$b) Q = \frac{R}{\omega_0 L} = \frac{100,000}{100 \times 10^5 \times 20 \times 10^{-3}}$$

$$= \frac{1}{20} \times 10^3$$

$$0.05 \times 10^3$$

$$= 50$$

$$\beta = \frac{\omega_0}{Q} = \frac{100 \times 10^3}{50} = 2000\text{rad/s} = 2k/s$$

$$\omega_i = \omega_0 - \frac{\beta}{2} = 100000 - \frac{2000}{2}$$

$$= 100000 - 1000$$

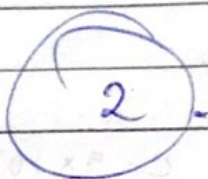
$$= 99,000 = 99k\text{rad/s.}$$

$$\omega_2 = \omega_0 + \frac{\beta}{2} = 100,000 + \frac{2000}{2}$$

$$= 100,000 + 1000$$

$$= 101,000 \text{ rad/s.}$$

$$= \text{101 Krad/s.}$$



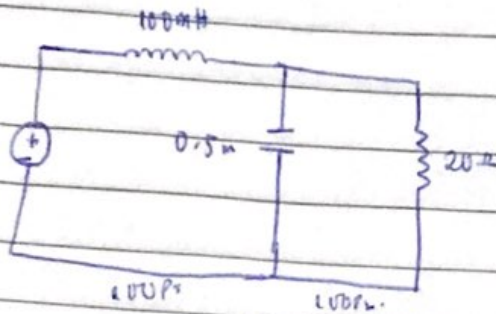
The input admittance is

$$Y = j\omega 0.1 + \frac{1}{10} + \frac{1}{2 + j\omega 2} = 0.1 + j\omega 0.1 + \frac{2 - j\omega 2}{4 + 4\omega^2}$$

At resonance, $\text{Im}(Y) = 0$ and

$$\omega 0.1 - \frac{2\omega}{4 + 4\omega^2} = 0 \Rightarrow \omega_0 = 2 \text{ rad/s.}$$

9/1/19



$$100\text{mH} = (100 \times 10^{-3})\text{H} \rightarrow L$$

$$0.5\text{mF} = (0.5 \times 10^{-3})\text{F} \rightarrow C$$

$$20\Omega \rightarrow R$$

$$(100 \times 10^{-3})j\omega\text{H}$$

$$(0.5 \times 10^{-3}) = 1/2000 - 2000/j\omega$$

$$20\Omega$$

From loop 2.

R//C

$$20 \times 2000$$

$$j\omega$$

i.e. Product.

$$20 + 2000$$

$$j\omega$$

sum.

$$\Rightarrow 40000$$

$$\Rightarrow \frac{40000 \times (20j\omega - 2000)}{20j\omega + 2000 (20j\omega + 2000)}$$

(cancellation)

$$\Rightarrow 800000j\omega - 80000000$$

$$-400j\omega - 4000000$$

$R = Z + (R/C)$ since the inductor is in series

$$80000j\omega - 80000000 + (100 \times 10^{-3})j\omega$$

$$-400j\omega - 4000000$$

at resonance $\text{Im}(R)$

$$= 800000j\omega + j\omega(100 \times 10^{-3})$$

$$-400j\omega - 4000000$$

$$400000\omega_0 + (-40\omega^2) - 400000j\omega_0$$

$$400000 - 40\omega^2 = 0$$

$$\omega^2 = 10000$$

$$\omega = 100 \text{ rad/s}$$