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17/ENG06/014

MECHATRONICS ENGINEERING

EEE 322 ELECTRIC CIRCUIT II

i, A parallel resonant circuit has $R = 100 \text{ k}\Omega$, $L = 20 \text{ mH}$ & $C = 5 \text{ nF}$
Calculate ω_0 , ω_1 , ω_2 , Q & B

$$\rightarrow \omega_0 = \frac{1}{\sqrt{LC}} = \frac{1}{\sqrt{(20 \times 10^{-3}) \times (5 \times 10^{-9})}} = 100 \text{ krad s}^{-1}$$

$$\rightarrow B = \frac{\omega_0}{Q} = \frac{1}{RC} = \frac{1}{100 \times (5 \times 10^{-9})} = 2 \text{ krad s}^{-1}$$

From above, $\omega_0 = 100 \text{ krad s}^{-1}$ & $B = 2 \text{ krad s}^{-1}$

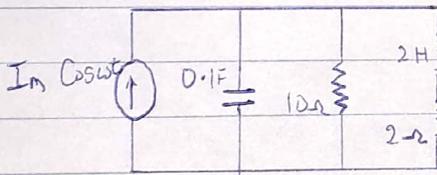
$$\therefore Q = \frac{\omega_0}{B} = \frac{100 \times 10^3}{2 \times 10^3} = 50$$

Since $Q \geq 10$

$$\rightarrow \omega_1 = \omega_0 - \frac{B}{2} = 100 \times 10^3 - \frac{2 \times 10^3}{2} = 99 \text{ krad s}^{-1}$$

$$\rightarrow \omega_2 = \omega_0 + \frac{B}{2} = 100 \times 10^3 + \frac{2 \times 10^3}{2} = 101 \text{ krad s}^{-1}$$

ii, Determine the resonant frequency of the circuit below



The input admittance is; $Y = j\omega 0.1 + \frac{1}{10} + \frac{1}{2 + j\omega 2}$

$$= 0.1 + j\omega 0.1 + \frac{2 - j\omega 2}{4 + 4\omega^2}$$

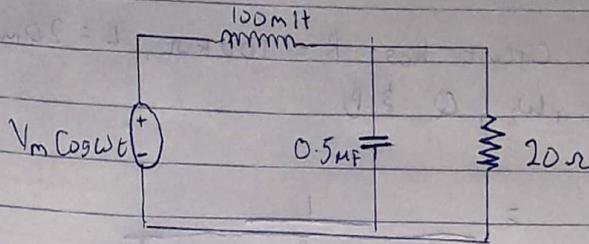
At Resonance

$$I_m(Y) = 0$$

$$\omega_0 0.1 = \frac{2\omega_0}{4 + \omega_0^2} = 0$$

$$\omega_0 = 2 \text{ rad/s}^{-1}$$

iii, Calculate the resonant frequency of the circuit below



$$\begin{aligned} \frac{20 + \frac{2000}{j\omega}}{20 + \frac{2000}{j\omega}} &= \frac{40000 + 001 - 40000}{20j\omega + 2000} + \frac{(20j\omega - 2000)}{(20j\omega - 2000)} \\ &= \frac{80000j\omega - 8000000}{-400j\omega - 4000000} + 100 \text{ mH} \end{aligned}$$

At resonance of the imaginary part = 0 at $\omega = 0$

$$\frac{80,000j\omega}{-400j\omega - 4000000} + \frac{j\omega(100 \times 10^{-3})}{-400j\omega - 4000000} = 0$$

$$\begin{aligned} -400j\omega - 4000000 &= 80 \times 10^3 \\ &= 800000\omega + [-40\omega^2] - 4000000\omega \end{aligned}$$

$$= 400000\omega - 40\omega^2 = 0 \Rightarrow \omega = \omega \leftarrow$$

$$-40\omega^2 = -400000$$

$$\omega^2 = \frac{-400000}{-40} = 10000$$

$$\omega = \sqrt{10000} = 100 \text{ rad/s}^{-1}$$

