

OLOGBOSERE ANTHONIA

MECHATRONICS

18/ENG05/049

ENG 234

1.

$$v = (4t - 3t^2) \text{ m/s}$$

$$\int v \cdot dt = s = 2t^2 - t^3 + C$$

When $s=0$ then $t=0$

$$\therefore 0 = 2(0)^2 - (0)^3 + C$$

$$C = 0$$

$$\therefore s = 2t^2 - t^3$$

At $t=4s$

$$s = 2(4)^2 - (4)^3$$

$$s = -32m$$

2.

$$v = (0.5t^3 - 8t) \text{ m/s}$$

$$a = \frac{dv}{dt} = (1.5t^2 - 8) \text{ m/s}^2$$

At $t=2s$

$$a = (1.5(2)^2 - 8) \text{ m/s}^2$$

$$= (6 - 8) \text{ m/s}^2$$

$$a = -2 \text{ m/s}^2$$

3.

$$a = (4t^2 - 2) \text{ m/s}^2$$

$$\int a = v = \frac{4t^3}{3} - 2t + C_1$$

$$\int v = s = \frac{4t^4}{12} - \frac{2t^2}{2} + C_1 t + C_2$$

$$s = \frac{t^4}{3} - t^2 + C_1 t + C_2$$

But $s = -2\text{m}$ when $t = 0\text{s}$

$$\therefore -2 = \frac{(0)^4}{3} - (0)^2 + C_1(0) + C_2$$

$$-2 = C_2$$

Then,

$$s = \frac{t^4}{3} - t^2 + C_1 t - 2$$

Also, $s = -20\text{m}$ when $t = 2\text{s}$

$$\therefore -20 = \frac{2^4}{3} - 2^2 + C_1(2) - 2$$

$$-20 = \frac{16}{3} - 4 + 2C_1 - 2$$

$$2C_1 = -20 + \frac{2}{3}$$

$$2C_1 = \frac{-58}{3}$$

$$C_1 = \frac{-29}{3}$$

Hence,

$$s = \frac{t^4}{3} - t^2 - \frac{29t}{3} - 2$$

At $t = 4\text{s}$

$$s = \frac{4^4}{3} - 4^2 - \frac{29(4)}{3} - 2$$

$$s = \frac{256}{3} - 16 - \frac{116}{3} - 2$$

$$s = \frac{86}{3}$$

$$s = 28.67\text{m}$$

4. $v = (20 - 0.05s^2)\text{ m/s}$

$$\frac{dv}{ds} = -0.1s$$

$$\text{but } a = v \left(\frac{dv}{ds} \right)$$

$$a = (20 - 0.05s^2)(-0.1s)$$

At $s = 15\text{m}$

$$a = (20 - 0.05(15)^2)(-0.1(15))$$

$$= (20 - 11.25)(-1.5)$$

$$= 8.75(-1.5)$$

$$= -13.125\text{ m/s}^2$$