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Course: ENG 234 [Mechanics]

Assignment

1) $V = (4t - 3t^2) \text{ m/s}$ $t=0, S=0, t=4$

$$V = \frac{ds}{dt} = (4t - 3t^2)$$

$$\therefore \frac{ds}{dt} = (4t - 3t^2)$$

$$\int ds = \int_0^4 (4t - 3t^2) dt$$

$$S = \left[\frac{4t^2}{2} - \frac{3t^3}{3} \right]_0^4$$

$$S = [2t^2 - t^3]^4 - [2t^2 - t^3]^0$$

$$S = 2(4)^2 - (4)^3 - [0]$$

$$S = 32 - 64$$

$$S = -32 \text{ m} \quad \therefore S = 32 \text{ m left of the origin}$$

\therefore This means that the position of the particle is to the left of the origin.

2) $V = (0.5t^3 - 8t) \text{ m/s}$

$$a = \frac{dv}{dt}$$

$$a = \frac{d}{dt} (0.5t^3 - 8t)$$

$$a = (1.5t^2 - 8) \text{ m/s}^2$$

$$\text{at } t = 2 \text{ s}$$

$$= 1.5(2)^2 - 8$$

$$(1.5 \times 4) - 8$$

$$= -2 \text{ m/s}^2$$

\therefore This implies that the particle is decelerating.

$$a = (4t^2 - 2)$$

$$a = \frac{dv}{dt} = (4t^2 - 2)$$

$$\frac{dv}{dt} = (4t^2 - 2)$$

$$\int dv = \int (4t^2 - 2) dt$$

$$v = \left(\frac{4t^3}{3} - 2t + C_1 \right) \text{ m/s}$$

$$\therefore v = \frac{ds}{dt} = \left(\frac{4t^3}{3} - 2t + C_1 \right) \text{ m/s}$$

$$\frac{ds}{dt} = \left(\frac{4}{3}t^3 - 2t + C_1 \right)$$

$$\int ds = \int \left(\frac{4}{3}t^3 - 2t + C_1 \right) dt$$

$$s = \left(\frac{4t^4}{3 \times 4} - \frac{2t^2}{2} + C_1 t + C_2 \right) \text{ m}$$

$$s = \frac{1}{3}t^4 - t^2 + C_1 t + C_2$$

$$\text{At } t = 0 \text{ s, } s = -2 \text{ m}$$

$$s = \frac{1}{3}t^4 - t^2 + C_1 t + C_2 \quad s = \frac{1}{3}t^4 - t^2 + C_1 t + C_2$$

$$-2 = \frac{1}{3}(0)^4 - (0)^2 + C_1(0) + C_2$$

$$\therefore C_2 = -2$$

$$\text{At } t = 2, s = -20 \text{ m}$$

$$s = \frac{1}{3}t^4 - t^2 + C_1 t - 2$$

$$-20 = \frac{16}{3} - 4 + 2C_1 - 2$$

$$-20 = \frac{-2}{3} + 2C_1$$

$$2C_1 = -20 + \frac{2}{3}$$

$$2C_1 = -19.33$$

$$C_1 = \frac{-19.33}{2}$$

$$= -9.67$$

$$\therefore C_1 = -9.67$$

$$C_2 = -2$$

$$\therefore S = \frac{1}{3}t^3 - t^2 + C_1t + C_2$$

$$S = \frac{1}{3}t^3 - t^2 - 9.67t - 2$$

$$\text{At } t = 4s \quad S = ?$$

$$S = \frac{1}{3}(4)^3 - (4)^2 - 9.67(4) - 2$$

$$S = \frac{256}{3} - 16 - 38.6668 - 2$$

$$S = \frac{256}{3} - 56.6668$$

$$S = 28.667m$$

\therefore The possible The position of the particle is 28.67m

$$a = \frac{dv}{dt} = \frac{dv}{ds} \times \frac{ds}{dt}$$

$$= \frac{dv}{ds} \times v$$

$$\therefore a = v \frac{dv}{ds}$$

$$\frac{dv}{ds} = -0.15$$

$$\therefore a = (20 - 0.055^2)(-0.15)$$

$$\text{At } s = 15\text{m}$$

$$a = (20 - 0.05(15)^2)(-0.15(15))$$

$$a = (20 - 11.25)(-2.25)$$

$$a = -19.687 \text{ m/s}^2$$

$$a = -19.687 \text{ m/s}^2$$

\therefore The acceleration of the particle at $s = 15\text{m}$ is -19.687 m/s^2 implies that the particle is decelerating.